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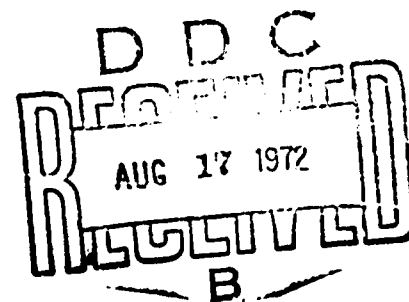
# NAVAL SHIP RESEARCH AND DEVELOPMENT CENTER

Bethesda, Md. 20034



## THE STRUCTURAL BEHAVIOR OF GLASS PRESSURE HULLS

by  
K. Nishida



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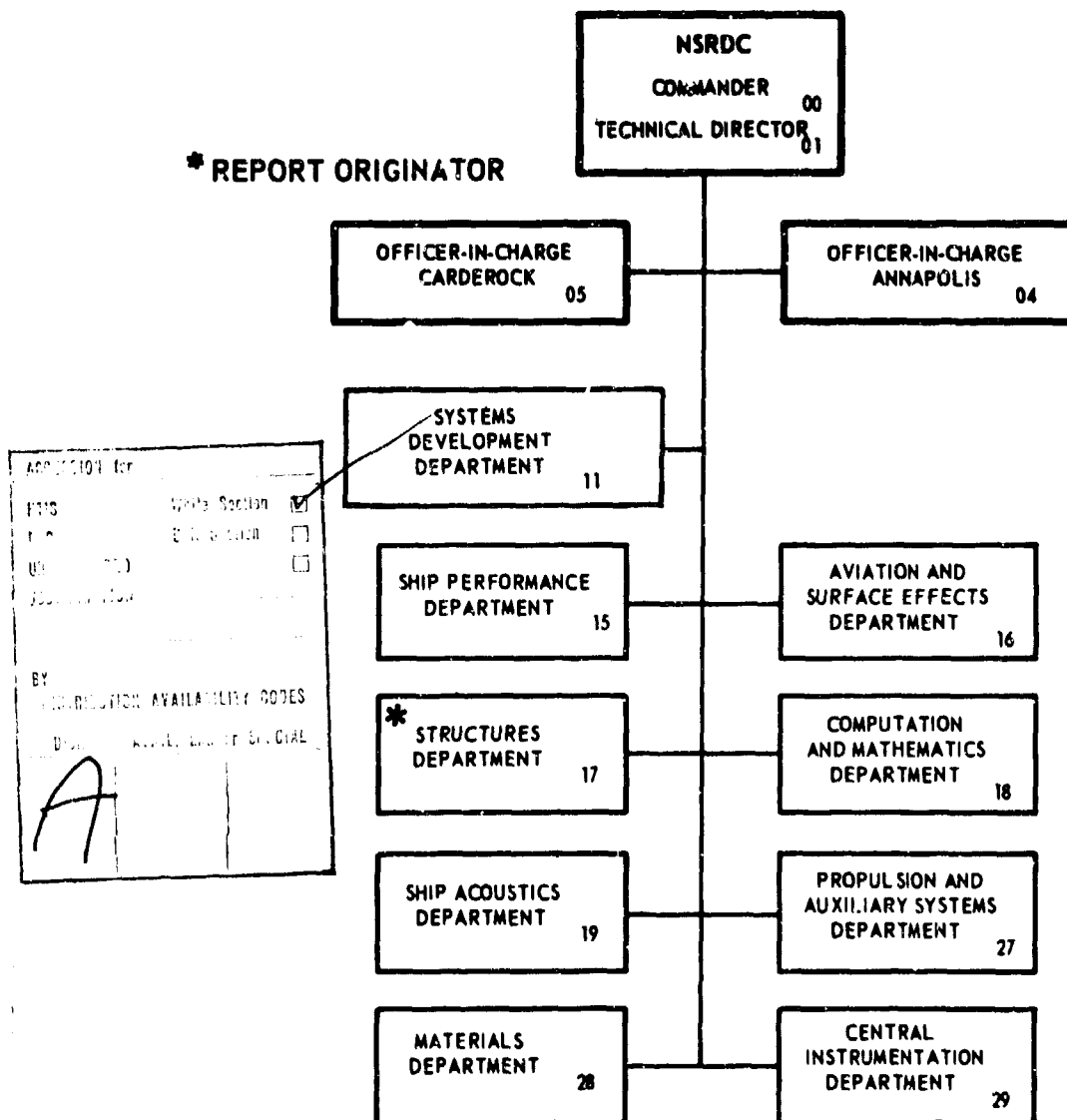
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A report on glass pressure vessels for deep submergence is presented. Emphasis is on the structural response of spherical and hemispherical glass shells under external hydrostatic and cyclic pressure. Results of earlier programs are reviewed. A computerized analysis trading off the variables in the joint problem is presented. Final joint geometries are discussed and data on chemically strengthened glass hemispherical shells with equatorial joint rings under fatigue conditions are presented. The results indicate relatively efficient ( $W/D = 0.5$ ), small pressure vessels of chemically strengthened glass are practical for unmanned noncritical applications to 20,000 ft. Nine 10-inch diameter chemically strengthened glass hemispherical shells of PPG 1080 glass with overall weight to displacement ratios of 0.5 survived at least 3000 cycles to 20,000 ft. Each hemisphere was then subjected to a proof test to 30,000 ft. Although this data is encouraging, substantial effort is necessary before glass structures can be applied in critical conditions even on the present small scale.

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PRESSURE HULLS

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## TABLE OF CONTENTS

|                                                                      | Page |
|----------------------------------------------------------------------|------|
| ABSTRACT .....                                                       | 1    |
| ADMINISTRATIVE INFORMATION .....                                     | 1    |
| INTRODUCTION .....                                                   | 1    |
| ANALYSIS OF EARLY GLASS JOINTS .....                                 | 4    |
| PARAMETRIC STUDY OF THE JOINT PROBLEM .....                          | 6    |
| FINAL JOINT DESIGNS .....                                            | 9    |
| DESCRIPTION OF MODELS .....                                          | 10   |
| TEST PROCEDURE .....                                                 | 13   |
| TEST RESULTS AND DISCUSSION .....                                    | 14   |
| SUMMARY .....                                                        | 19   |
| ACKNOWLEDGMENTS .....                                                | 21   |
| REFERENCES .....                                                     | 104  |
| APPENDIX - BACKGROUND ON GLASS AND CERAMIC SPHERICAL<br>SHELLS ..... | 71   |

## LIST OF FIGURES

|                                                                                                       | Page |
|-------------------------------------------------------------------------------------------------------|------|
| Figure 1 - Analysis of Constant Thickness Hemispherical<br>Shell .....                                | 22   |
| Figure 2 - Grinding Flaws at Beveled Edge .....                                                       | 23   |
| Figure 3 - Annealed Glass Hemisphere after Static Test to<br>17,000 psi .....                         | 24   |
| Figure 4 - Analysis of Reinforced Joint Design .....                                                  | 25   |
| Figure 5 - Surface Compressed Hemisphere with Reinforced Joint<br>after 10 Cycles to 10,000 psi ..... | 26   |
| Figure 6 - Joint Geometries for Parametric Study .....                                                | 27   |
| Figure 7 - Stress Contours .....                                                                      | 28   |
| Figure 8 - Final Joint Designs .....                                                                  | 37   |
| Figure 9 - Compressive Stress-Strain Curve for<br>662 Titanium .....                                  | 38   |
| Figure 10 - Analysis of Final Joint Designs .....                                                     | 39   |
| Figure 11 - Glass Hemispherical Shell .....                                                           | 54   |

|                                                                                                                       | Page |
|-----------------------------------------------------------------------------------------------------------------------|------|
| Figure 12 - Assembled Spheres .....                                                                                   | 55   |
| Figure 13 - Model in Test Facility .....                                                                              | 56   |
| Figure 14 - Inspection Set Up .....                                                                                   | 57   |
| Figure 15 - Fracture on Hemisphere 15 after 100 Cycles to<br>6500 psi .....                                           | 58   |
| Figure 16 - Inside Edge Chip on Hemisphere 13 after 898 Cycles<br>to 5000 psi .....                                   | 59   |
| Figure 17 - Outside Edge Spall on Hemisphere 13 after 1048 Cycles<br>to 5000 psi .....                                | 60   |
| Figure 18 - Flaw in Hemisphere 3 .....                                                                                | 61   |
| Figure 19 - Models after Test .....                                                                                   | 64   |
| Figure 20 - Summary of Test Results of 10-Inch-Diameter 0.28 Wall<br>Fusion Sealed Annealed Pyrex Glass Spheres ..... | 82   |
| Figure 21 - Examples of Fusion Sealed Seams .....                                                                     | 83   |
| Figure 22 - Nominal Model Dimensions for Fusion Sealed Spheres<br>with Penetration .....                              | 84   |
| Figure 23 - 44 Inch Diameter Fusion Sealed Annealed Glass<br>Sphere .....                                             | 85   |
| Figure 24 - Pressure Strain Plots for 44 Inch Glass<br>Sphere .....                                                   | 86   |
| Figure 25 - Damage to Model 44-1 after 3500 psi .....                                                                 | 87   |
| Figure 26 - Gage Locations and Strain Sensitivities for<br>44 Inch Sphere .....                                       | 88   |
| Figure 27 - Damage to Model C-2 after Cycling to<br>5000 psi .....                                                    | 90   |
| Figure 28 - Nominal Model Dimensions and Test Result of 5 Inch<br>Diameter Pyroceram Hemisphere .....                 | 91   |

#### LIST OF TABLES

|                                                                                                                            | Page |
|----------------------------------------------------------------------------------------------------------------------------|------|
| Table 1 - Summary of Geometric and Material Properties .....                                                               | 67   |
| Table 2 - Test Results of 0.28 in. Wall--10-Inch-Diameter Surface<br>Compressed Glass Hemispheres .....                    | 68   |
| Table 3 - Test Results of 10-Inch-Diameter 0.36 Wall PPG 1080 K <sup>+</sup><br>Surface Compressed Glass Hemispheres ..... | 69   |
| Table 4 - Test Results of 10-Inch-Diameter Variable Wall PPG 1578<br>Surface Compressed Glass Hemispheres .....            | 70   |

|                                                                                                                                | Page |
|--------------------------------------------------------------------------------------------------------------------------------|------|
| Table 5 - Effect of Loading Rate and Pressure Medium on Collapse Strength .....                                                | 92   |
| Table 6 - Collapse Strength of 10-Inch-Diameter 0.28 Wall Fusion Sealed Annealed Pyrex Glass Spheres with Modified Seams ..... | 93   |
| Table 7 - Cyclic Tests of 10-Inch-Diameter 0.28 Wall Fusion Sealed Annealed Pyrex Glass Spheres .....                          | 94   |
| Table 8 - Collapse Strength of 10-Inch-Diameter 0.36 Wall Fusion Sealed Annealed Pyrex Glass .....                             | 95   |
| Table 9 - Summary of Static Tests of 10-Inch-Diameter Fusion-Sealed Annealed Pyrex Glass Spheres with Penetrations .....       | 95   |
| Table 10 - State Cyclic Tests of 10-Inch-Diameter 0.18 Wall Monolithic Alumina Spheres .....                                   | 96   |
| Table 11 - Summary of Static Tests of Chemically Strengthened Herculite II (1080 Na <sup>+</sup> ) Glass Hemispheres .....     | 97   |
| Table 12 - Test Results of 10-Inch-Diameter 0.281 Wall Annealed Pyrex Glass Hemispherical Shells without Gaskets .....         | 98   |
| Table 13 - Test Results of 10-Inch-Diameter 0.28 Wall Annealed Pyrex Glass Hemispheres with Gaskets .....                      | 99   |
| Table 14 - Summary of Cyclic Tests of 10-Inch-Diameter 0.28 Wall Annealed Pyrex Glass Hemispheres .....                        | 100  |
| Table 15 - Summary of Test Results of 10-Inch-Diameter 0.36 Wall PPG 1080 Annealed Glass Hemispherical Shells .....            | 101  |
| Table 16 - Summary of Static Tests of Chemcor Hemispheres with Reinforced Bearing Surfaces .....                               | 102  |
| Table 17 - Summary of Cyclic Tests of Chemcor 0312 Hemispheres with Reinforced Bearing Surfaces .....                          | 103  |



## ABSTRACT

A report on glass pressure vessels for deep submergence is presented. Emphasis is on the structural response of spherical and hemispherical glass shells under external hydrostatic and cyclic pressure. Results of earlier programs are reviewed. A computerized analysis trading off the variables in the joint problem is presented. Final joint geometries are discussed and data on chemically strengthened glass hemispherical shells with equatorial joint rings under fatigue conditions are presented. The results indicate relatively efficient ( $W/D = 0.5$ ), small pressure vessels of chemically strengthened glass are practical for unmanned noncritical applications to 20,000 ft. Nine 10-inch diameter chemically strengthened glass hemispherical shells of PPG 1080 glass with overall weight to displacement ratios of 0.5 survived at least 3000 cycles to 20,000 ft. Each hemisphere was then subjected to a proof test to 30,000 ft. Although this data is encouraging, substantial effort is necessary before glass structures can be applied in critical conditions even on the present small scale.

## ADMINISTRATIVE INFORMATION

The work described in this report was sponsored by the Deep Ocean Technology (DOT) project and funded under Task Area S 4636, Task 12326.

## INTRODUCTION

Glass is a material which exists in large quantities on this earth. Its wide use is prompted largely by economic factors as industrial processing methods have been developed to make its use relatively cheap in such areas as the manufacture of bottle containers, sheet, plate, kitchenware, and fibrous glass products. In general, the present applications require that the glass carry very little to no load. This is only natural because of the brittleness of glass. In the past, whenever a transparent structural material was required designers have favored plastics such as polymethyl methacrylate. The structural plastics, however, are not without their limitations as strength eventually becomes a problem in modern technological applications. Aircraft windshields and pressure vessels for deep sea applications are such examples.

The use of massive glass for deep submergence pressure vessels has been under study by the Navy for several years. Exploratory tests and feasibility studies<sup>1,2</sup> demonstrated the potential superiority of glass over metallic materials. Subsequently, efforts were conducted by several laboratories for various manned and unmanned objectives. The Naval Ordnance Laboratory<sup>3</sup> (NOL) conducted experiments at sea to study the sympathetic implosion problem. They also conducted fatigue tests of annealed and surface strengthened glass hemispherical shells and reported successful results on chemically strengthened models.<sup>4</sup> Stachiw<sup>5</sup> conducted numerous tests on commercially manufactured annealed glass flasks for

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<sup>1</sup>Kiernan, T.J., "An Exploratory Study of the Feasibility of Glass and Ceramic Pressure Vessels for Naval Applications," NSRDC Report 2243 (Sep 1966).

<sup>2</sup>Coffman, W.B. et al., "Feasibility Study of Plastic-Clad Glass Capsules for Deep Diving Submersibles," NOL TR 65-76 (Jun 1965).

<sup>3</sup>Heathcote, T.B., "The Resistance of Hollow Glass Models to Underwater Explosions at Great Depths III Spheres with Overlays," NOL TR 66-78 (May 1966).

<sup>4</sup>Perry, H.A., "Surface Compression Strengthened Glasses: Some Properties," NOL TR 71-21 (Mar 1971).

<sup>5</sup>Gray, K.O. and J.D. Stachiw, "Light Housings for Deep Submergence Applications--Part III. Glass Pipes with Conical Flanged Ends," NCEL Technical Report R618 (Mar 1969).

adaptation to light housings for deep submergence. Foreman<sup>6</sup> and Murphy<sup>7</sup> in work on the Deep View and Hikino vehicles studied the joint problem on small and large scale annealed glass specimens. NSRDC conducted studies on the impact<sup>8</sup> behavior of brittle hulls, a theoretical study of an imploding spherical bubble,<sup>9</sup> and also the bearing strength of brittle materials.<sup>10</sup>

In 1967 a concerted effort to develop massive glass for deep submergence was established in the U.S. Navy's Deep Ocean Technology Project. One of the long range objectives of the program was the development of a relatively small (7-10 ft diameter), light weight (W/D of 0.5) manned vehicle for operation to 20,000 ft. Glass was one of the candidate materials for this vehicle. Based on work accomplished prior to 1967, the scope of the DOT massive glass effort was established. In essence the guidelines were:

1. The effort would be concentrated on the spherical shell and the hull material would be of a surface strengthened glass.
2. The pressure hull would have an openable girth joint for passage of personnel and equipment.

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<sup>6</sup>Foreman, W. and R. DeHart, "Submersible Deep View Pioneers Glass/Metal Bonding," Undersea Technology, pp. 24-27 (Dec 1967).

<sup>7</sup>Murphy, D.W., "Development and Testing of a 56-In.-Dia. Jointed Glass Pressure Hull," ASME Paper No. 69-WA/UnT-2 presented at Winter Annual Winter, L.A. Calif (Nov 16-20, 1969).

<sup>8</sup>Zillicaus, S. and H. Hashmall, "Impact Strength and Response of Protected Brittle Models of Deep Submergence Structures," David Taylor Model Basin Report 2314 (Dec 1966).

<sup>9</sup>Lilliston, R.R., "Calculations on the Collapse of a Spherical Gas-Filled Cavity in a Compressible Liquid," David Taylor Model Basin Report 2223 (Aug 1966).

<sup>10</sup>Moreno, D.H. and M.L. Salive, "The Effects of Size and Environment on the Uniaxial Compressive Breaking Strength of Glass, Alumina, and Pyroceram," NSRDC Report 3315 (May 1970).

The structural aspects of the DOT program were assigned to the Naval Ship Research and Development Center (NSRDC) and the material aspects to NOL. After 3 years of effort, a critical review of the massive glass program indicated that the realization of glass in a man rated situation was still a number of years away. Thus, a decision to terminate this phase of the program was made. This report summarizes the analytical and experimental data generated at NSRDC.

#### ANALYSIS OF EARLY GLASS JOINTS

Prior to the DOT program a number of experiments had been conducted on glass joints. Much of this work was very exploratory in nature and was conducted in many cases mainly to observe mechanical response through simple structures such as a spherical shell formed by butting together two glass hemispherical shells or placing a hemispherical shell on a metal block and loading hydrostatically. A review of some of this work is presented in the appendix. As a general rule the early results indicated that failure in glass hemispherical shells were stress rather than buckle induced. However, an accurate knowledge of the stresses at the joint were not known. The rapid advances made in the field of finite element<sup>11</sup> has made solutions to problems such as joints in glass hemispheres quite routine. In an attempt to explain some of the difficulties experienced in developing reliable mechanical butt joints, two geometries, extensively tested experimentally, were stress analyzed. The finite element computer program utilized was developed by Gifford<sup>12</sup> of the Center. It utilizes triangular ring elements and is applicable to any elastic-plastic axisymmetric structure. It will handle nonlinear effects of the contact problem.

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<sup>11</sup>Gifford, L.N. and R.F. Jones, "Structural Analysis of Deep Submergence Pressure Hulls," SNAME Paper No. 12 presented at Spring Meeting, Honolulu, Hawaii (May 25-28 1971).

<sup>12</sup>Gifford, L.N., "Finite Element Analysis for Arbitrary Axisymmetric Structures," NSRDC Report 2641 (Mar 1968).

The first geometry analyzed was the glass spherical shell formed by butting together two uniform wall hemispherical shells. The equator represents an axis of symmetry and therefore only one half of the sphere need be analyzed. In the actual hemisphere the edges of the bearing face are beveled or rounded. For this analysis a rounded edge was assumed. A structural idealization of the joint is shown in Figure 1. The mesh was generated by a computer program written by Rockwell and Pincus<sup>13</sup> of the Center. The results of the analysis are also presented graphically in Figure 1. It may be noted that in a spherical shell under hydrostatic pressure the principal directions of stress are meridional, circumferential and radial. Generally, the meridional and circumferential stresses are high in compression and are not believed to be a factor in failure of glass joints. The principal stress with the lowest magnitude is the radial which is shown in Figure 1. Away from local disturbances of the joint, the stress in the radial direction at the outer surface is equal to the hydrostatic pressure and at the inner surface is equal to zero. Note that tensile stresses are present in an area very close to the inner edge of the bearing surface. Thus, flaws in the circumferential direction would be expected to play a role in the fracture process. It is known that flaws of this type exist. Photographs from a typical glass hemispherical shell of Pyrex glass are shown in Figure 2. In this case the edge of the bearing face is beveled at 45 deg. An example of a hydrostatic test of this type of hemispherical shell and the resulting damage is shown in Figure 3. Note the spalling at the inner edge of the hemisphere.

The second geometry analyzed was the reinforced joint design utilized on hemispherical shells of Chemcor 0312 glass. The tests of these models occurred prior to initiation of the DOT project and are summarized in the appendix. Although the results of these tests were quite encouraging, fractures were observed in static tests and catastrophic failure resulted in two fatigue tests after about 100 cycles to 22,500 ft. The average bearing stress at 22,500 ft is about 50,000 psi. The idealized

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<sup>13</sup>Rockwell, R.D. and D.S. Pincus, "Computer Aided Input/Output for Use with Finite Element Method of Structural Analysis," NSRDC Report 3402 (Aug 1970).

structure used in the analysis is shown in Figure 4a and the results of the analysis are shown in Figures 4b and 4c. Note the tensile stress in the radial direction. This stress is relatively low and would not be expected to cause fracture in Chemcor 0312 glass for the tensile stress (3,000 psi) that was applied during most of the tests. Fractures nevertheless did occur and an example is shown in Figure 5. It is suspected that flaws also played a significant role in these tests.

#### PARAMETRIC STUDY OF THE JOINT PROBLEM

One of the guidelines established at the initiation of the program was that the glass pressure hull have an openable girth joint. The early results on glass hemispherical shells provided little insight on the optimum joint geometry. Therefore, in an attempt to optimize joint design in glass hemispherical shells a parametric study of the joint problem using the finite element method was conducted. The variables investigated were ring rigidity, glass bearing face geometry and interface layer properties. A summary of the material and geometric parameters is shown in Table 1. The following assumptions were made for this study.

1. The overall weight displacement ratio of the pressure hull would be about 0.5. For a 10 in. diameter shell the corresponding thickness was 0.30 in.
2. The pressure hull would be formed essentially by butting together two hemispherical halves with an equatorial joint.
3. The joint assembly would include a metallic rim into which the glass hemisphere would be potted.
4. The elastic effect of an interface layer between the glass and metallic rim would be considered.
5. The geometry of the edge of the glass hemisphere would be varied.

Sketches showing the nominal model dimensions for the three geometries are shown in Figure 6. The majority of computer runs were with a titanium with a ring 0.58 in. wide. This thickness was obtained by equating the deflection of a 10 inch diameter glass sphere with a wall thickness of 0.3 in. to the deflection of the titanium ring. The results of the computer output are presented in the form of contour maps in Figure 7. Only

the principal stress in the direction through the thickness is shown since the stresses in the other two directions are high in compression. The stresses are given in psi/psi. The results of the output are summarized below.

#### EFFECT OF POISSON'S RATIO OF THE INTERFACE LAYER

In these runs the following parameters were held constant

|                                         |                      |
|-----------------------------------------|----------------------|
| Thickness of interface layer, $h_i$     | 0.01 in.             |
| Young's modulus of the interface, $E_i$ | $5 \times 10^6$ psi  |
| Width of ring $\omega$                  | 0.58 in.             |
| E of titanium ring                      | $15 \times 10^6$ psi |

The value of Poisson's ratio of the interface layer was varied from 0.1, 0.3, and 0.45. For a flat bearing face, as Poisson's ratio of the interface was increased, the radial compressive stress decreased slightly. For rounded-type joints, increasing Poisson's ratio appeared to slightly increase radial compressive stress.

#### EFFECT OF YOUNG'S MODULUS OF THE INTERFACE LAYER

This series of test cases was identical to the above except that Poisson's ratio of the interface layer was held constant at 0.3. Young's modulus of the interface layer was then changed from  $0.5 \times 10^6$ ,  $5 \times 10^6$ , and  $50 \times 10^6$  psi. For the flat bearing face, increasing Young's modulus from  $0.5$  to  $50 \times 10^6$  psi did not appear to have a discernible effect for the mesh size used. In the case of the rounded joints, a markedly undesirable effect was caused by increasing Young's modulus of the interface layer. At the low value of  $0.5 \times 10^6$  psi, the compressive stresses in the radial direction were relatively high for both the semi-rounded and full-rounded configurations. At the high value of  $50 \times 10^6$ , the stress approached a value of 0 for the semi-rounded configuration and relatively high tensile stresses were observed for the full-rounded configuration.

#### EFFECT OF RING RIGIDITY

Two configurations were examined for comparison with the membrane titanium ring (0.58-in. width). In one case the ring width was changed

from 0.58 to 0.40 in. and the material was assumed to be titanium with a Young's modulus of  $15 \times 10^6$  psi. In the second case, a ring width of 0.40 in. was assumed, and the ring material was steel with a Young's modulus of  $30 \times 10^6$  psi. Decreasing the thickness of a titanium ring from 0.58 to 0.40 in. appeared to have a slightly undesirable effect. Compressive stresses in the radial direction were decreased for all three geometries (flat, semi-rounded, and full-rounded). However, a steel ring of 0.40-in. width appeared to create a more desirable stress state in the glass than did either the membrane titanium ring or a 0.40-in. titanium ring. Higher radial compressive stresses were apparent for all three geometric configurations. At the operating depth of 20,000 ft, the equivalent HVM stresses are 140,000 and 85,000 psi for the steel and titanium rings, respectively. Assuming a factor of safety of 2 on yielding of the ring, a steel with a proportional limit of 280,000 psi and titanium with 170,000 psi would be required.

#### EFFECT OF THICKNESS OF THE INTERFACE LAYER

One series of test cases was run to examine the effect of interface layer thickness. Respective thicknesses of 0.03 and 0.04 in. were assumed for the flat bearing face and the rounded joints, results were compared to those for the standard thickness of 0.01 in. used for all other runs. Increasing the interface layer thickness caused a slightly undesirable effect (lower radial stress) for the flat bearing face, very little effect for the semi-rounded case, and a slightly desirable effect for the full-rounded configuration.

In general it appeared that the flat bearing face was the least sensitive to changes in material properties of the interface layer. The rounded geometry was the most sensitive. If an interface layer with a high Poisson's ratio and low Young's modulus could be kept between the glass and the metal then the rounded type joint would be expected to perform satisfactorily. From a practical point of view this was considered to be very unlikely. The limited data suggested that extrusion of soft material was a serious problem. Thus, the rounded geometry was eliminated from the possible joint geometries. The optimum properties for the flat geometry was a high value of Young's modulus and a low value of Poisson's ratio. Again,



it appeared that such a material could cause practical difficulties because of microscopic imperfections in the glass part. For example it is very unlikely that a butt joint of a glass hemisphere on a block of a very rigid material such as alumina or tungsten carbide would perform in a desirable manner because of the local contact stresses. Fortunately, changing  $E$  and  $\nu$  of the interface layer does not have a marked effect on the stresses in the glass. Since it was felt that compliance was important a decision to utilize glass reinforced plastic was made.

#### FINAL JOINT DESIGNS

In the final design of the glass models a number of dimensional changes were made. The wall thicknesses of 10 inch diameter models were 0.28 and 0.36. The titanium ring was made of an alloy (662) that had a Young's modulus of  $17.5 \times 10^6$  psi rather than  $15 \times 10^6$  psi assumed in the parametric study. Finally in the course of the program it was decided that a joint ring which would permit in service inspection was desired.

Two membrane joint designs were selected for the 10 in. diameter 0.28 wall type glass hemispherical shell. These are shown in Figures 8a and 8b. The first designated Mod 1 had an "L" shaped cross section, while the Mod 2 ring had a "U" shaped cross section. The advantage of the Mod 1 ring was that it provided greater visibility for inspections. Both rings were of 662 titanium and were designed for membraned deflections at the equator. Because of the slightly different material and geometric properties of the final designs these joints were also stress analyzed by finite element. In the analysis it was assumed that slipping would take place at the curved surfaces of the shell and that no slipping would take place at the glass gasket boundary. The plastic analysis was utilized and the assumed stress-strain curve for the titanium ring is shown in Figure 9. The results of the finite element analysis is presented graphically in Figure 10. Note from the displaced structures membrane conditions were achieved (no bending). Also, there is no indication of tensile stresses in the glass. First yielding (the first triangular ring element whose Henky von Mises stress exceeds the proportional limit) occurs at a pressure of 9540 psi for the Mod 1 ring while first yielding occurs at a pressure of 8910 psi for the Mod 2 ring.

For a 10 inch diameter 0.06 wall glass hemispherical shell a ring with a "U" shaped cross section similar to the Mod 2 ring for the 0.28 wall hemisphere was chosen. A sketch of the geometry is shown in Figure 8c. A finite element analysis was performed on this joint. However, graphical output capability was not available on the computer program at the time and therefore, the stresses are not shown. The ring was designed to provide membrane conditions at the equator and no tensile stresses were indicated on the computer output.

The fourth design was a reinforced concept shown in Figure 8d. This was an attempt to lower the bearing stress at the joint without increasing the overall weight displacement ratio of the structure. The results of this analysis are shown in Figure 10. No tensile stresses are indicated. Note that first yielding in the titanium ring for this geometry does not occur till a pressure of 13,400 psi.

#### DESCRIPTION OF MODELS

All of the models tested were of chemically treated, surface compressed glass. Twenty four hemispheres were of PPG Code 1578 glass, fifteen were of PPG 1080, and two were of Corning Chemcor 0313 glass. Most of the models were constant-thickness hemispherical shells with an outside radius of 5 in. The PPG 1578 and Chemcor 0313 models were 0.28-in. thick, and the PPG 1080 models were 0.36 in. thick. The corresponding weight-to-displacement ratios for these thicknesses are 0.36 and 0.46. In addition 6 hemispheres of PPG 1578 which had reinforced joints were tested. The W/D ratio for this model was about 0.4.

The PPG 1578 constant thickness and variable wall glass hemispheres were fabricated by pressing hemispherical shell blanks from 0.375-in. and 0.75 plate material. The blanks were then rough ground at the curved surfaces and bearing face with 120-grit wheel. The flat bearing face and edges were then successively ground with loose abrasive as follows:

| Loose Abrasive | Material Removed, in. |
|----------------|-----------------------|
| 120            | 0.0024                |
| W2             | 0.0016                |
| W5             | 0.0014                |
| W8             | 0.0011                |
| Polish         | 0.0003                |

The edges were put on with an orbital sander. After grinding on the flat bearing face was completed using a loose abrasive of a particular size, the rounded edge was finished with the same abrasive. The procedure was followed through the steps shown. The models were then acid treated in a 10 percent HF acid solution to remove 0.001 in. of glass, and the hemispheres were chemically strengthened in a sodium salt bath. Surface flatness was checked by placing the bearing surface on a flat table and passing shim stock between them. This inspection procedure indicated that the surface was flat to within 0.001 in. However, when a flat rod was placed across the bearing surface and a light source positioned directly behind, it could be observed that contact was being made only at the inner corner of the bearing surface. It is estimated that the inner edge was less than a half mil higher than the outer edge. The out of flatness of the bearing face is attributed to the effect of the ion exchange treatment.

PPG 1080 glass hemispherical shells with two different strengthening treatments were tested. Six hemispheres were treated in a sodium salt bath (hereafter referred to as 1080  $\text{Na}^+$  glass) which has an abraded modulus of rupture of about 40 ksi and 15 hemispheres were treated in a potassium salt bath (hereafter referred to as 1080  $\text{K}^+$  glass) which has an abraded modulus of rupture of about 80 ksi. All of the hemispheres were 10 in. diameter in wall. The 1080  $\text{Na}^+$  models were fabricated by grinding the entire surface with 120 grit fixed abrasive. The bearing face was then prepared by grinding with successively finer loose abrasives, starting with 120 grit and finishing with W8 garnet. No attempts were made to refine grind the edges of the bearing face. The bearing surface was then polished and the entire hemisphere etched in a solution of 2 percent solution of hydrofluoric acid for 10 minutes. Following this the models were chemically strengthened.

The PPG 1080  $K^+$  glass hemispheres were fabricated in a manner similar to the PPG 1578 models. However, after rough grinding of the shells, one additional acid treatment step was utilized where 0.002 in. of glass was removed. The same steps were utilized in fine grinding the flat bearing face and corner radius as for the 1578 shells. Seven of the nine 1080  $K^+$  models were acid treated and chemically strengthened after completing the grinding steps. Two hemispheres were polished after grinding, then acid treated and chemically strengthened. The latter procedure was utilized to achieve transparency. This also reduced the wall thickness by about 0.02 on the 2 polished hemispheres. No flatness measurements were made on the shells although it is suspected that the same degree of flatness was obtained as in the case of the 1578 hemispheres.

The fabrication of the Chemcor 0313 models was quite different. The hemispheres were formed by pressing, and no work was performed on the curved surfaces except for acid treatment. The initial rough grinding step at the bearing face was done with a 90-grit loose abrasive. The hemispheres were then acid etched in a HF acid solution. The flat bearing face was then refinished with W-1 loose abrasive, and the edges were ground manually with a 320-grit stone. Following this, a second acid treatment in HF solution was used. The models were then chemically strengthened in a sodium salt bath. Flatness inspection indicated gaps of 0.001 in. for as much as 3 in. around the circumference.

Two of the spherical assemblies HGS 1 and HGS 2 which had PPG 1080  $Na^+$  hemispheres were potted into the titanium rings which had been filled with epoxy. The remaining models tested were assembled with glass reinforced plastic as the gasket material. The procedure for the models with glass reinforced plastic was as follows.

The glass hemispheres were assembled by first cleaning the glass and titanium rings with alcohol. A release was then applied to the flat surface. Epoxy (EPON 828 and Vers 125) was then applied to the flat bearing face and unidirectional 12 and fiberglass ribbons were manually layed up on the bearing face so that the fibers were oriented in the radial direction. After completion of the layup around the circumference, epoxy was applied to the glass fibers from the top. The inside of the titanium ring was coated with epoxy and the edge of the glass hemisphere placed in

it. The assembled hemisphere was then placed in the concave down position on a flat plate. A hole was drilled into the plate so that a vacuum could be drawn on the inside of the hemisphere. The procedure minimized the thickness\* of the GRP gasket and ensured that all excess epoxy was extruded prior to curing (under a vacuum load, a bearing stress of approximately 100 psi is applied). After curing, the excess GRP was trimmed off. A photograph of a completed 1578 hemisphere is shown in Figure 11, and assembled spheres of 1578 and 1080 glass in Figure 12.

#### TEST PROCEDURE

The primary objective of the program was to observe the performance of surface compressed glass hemispheres under cyclic loads. The cyclic tests of PPG 1080 Na<sup>+</sup> models were tested at 10,000 psi. In the later tests of the PPG 1578 and 1080 glass models, cyclic testing was started at moderately low levels of pressure to observe fatigue behavior at various levels of applied bearing loads. The cyclic test procedure is shown in Tables 2 and 3.

The titanium bearing surface of each hemisphere was coated with silicone grease. The hemispheres were put together, covered with urethane rubber jackets about 0.125-in. thick and then held together with aerosol bands. The urethane rubber jackets were used so that the glass would not contact the tank wall during the tests. Tests were conducted in the NSRDC 11.5-in.-diameter, and 15-in.-diameter high-pressure test facilities. Figure 13 shows a model in the test facility. Except for HGS-1 which was tested in oil, all other tests were conducted with fresh water as the pressure medium. Cycling rate varied from 60 to 85 cycles per minute. The lower rate of 60 cycles per minute was associated with higher maximum pressures. The pressure application rate for all tests was relatively

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\* In the early model assemblies gaskets were measured and thicknesses of approximately 0.005 in. were obtained. In later tests gaskets were made by overlapping the fiber ribbons to obtain a more dense packing. This also increased the thickness of gaskets to as much as 0.020 in. The reason for this change is discussed later in the report.

constant. The pressure profile was roughly 15 sec. to load, 15 sec. hold at maximum pressure, 15 sec. to relieve pressure, and 15 sec. at minimum pressure (50 psi). Models were inspected at a predetermined number of cycles. The inspection procedure (developed at NOL) consisted of placing the hemisphere in a fluid (cedar oil) with an index of refraction equal to that of the glass so that the glass bearing face could be viewed from the outside. A setup for inspection is shown in Figure 14.

## TEST RESULTS AND DISCUSSION

Test results are summarized in Tables 2 and 3.

### PPG 1578 GLASS

Cyclic testing of PPG Code 1578 constant thickness glass hemispherical shells was initiated at a pressure of 6500 psi. The average bearing stress at the joint for this pressure is 59,200 psi. The first model tested (designated HGS-10) survived the predetermined objective of 3000 cycles. However, a large crack about 0.5-in. long was observed on Hemisphere 15 of Model HGS-11 after 100 cycles; see Figure 15. The pretest inspection of this model had not revealed any gross flaws in this area although short scratches (less than 0.025 in.) were noted at the inner edge of the bearing face. Unfortunately no photographs were taken of these flaws. However, examination of the photograph in the fractured area appears to indicate that the crack did not extend to the inner corner. The fracture on this hemisphere resembles those more commonly observed on annealed glass hemispheres although this type of splitting has been observed on surface-compressed hemispheres (for example, in Figure 4).

Subsequent to the fracture observed in HGS-11, the cyclic test pressure was reduced to 5000 psi. The average bearing stress at the joint for this pressure is 45,900 psi. Even at this pressure, fatigue damage was observed in the test of Model HGS-12. After 898 cycles to 5000 psi, a small chip on the inner edge was observed on Hemisphere 13; see Figure 16. The pretest inspection of this model had not revealed gross flaws in this area. After additional 150 cycles to 5000 psi were applied to the model, further damage was observed on Hemisphere 13; light spalling of the inner

edge at the 40-deg orientation, light spalling of the outer edge at the 165-deg orientation, and spalling at the outer edge at the 110-deg orientation. Damage in the first two areas could not be identified with pre-existing anomalies, but damage in the third area was identified as originating from a deep grinding flaw on the bearing face (see Figure 17).

After damage had been observed on HGS-12 at 5000 psi, the cyclic test pressure was further reduced to 2500 psi for the remaining four model tests. All four assemblies survived 3000 cycles to 2500 psi and subsequently 3000 cycles to 3750 psi. Although each sphere survived 3000 cycles to 5000 psi, spalling was observed in two areas of Hemisphere 3 of Assembly HGS-16. The light spalling on the outer edge of the bearing face at the 235-deg orientation could not be identified with a preexisting flaw. The heavy damage on the inner edge of the bearing face at the 45-deg orientation is thought to have been caused by an untreated zone on the bearing joint. The pretest inspection of the joint revealed a check in the rounded corner which was so oriented that a piece of glass about 0.125-in. long was about to spall; see Figure 18a. After the visual inspection, a plastic replica was made of the edge and examination indicated that the piece of glass had actually spalled out; see Figure 18b. After 3000 cycles to 5000 psi, rather extensive damage was observed in this area; see Figure 18c. The previous inspection at 1800 cycles had not revealed any fatigue damage. No further tests were attempted on HGS-16 after 3000 cycles to 5000 psi. However, the remaining three assemblies were cycled at 6500 psi. Models HGS-14 and HGS-17 survived 2000 cycles and HGS-15 1500 cycles at this pressure. When the cyclic pressure was raised to 7700 psi (average stress of 70,600 psi), both HGS-14 and HGS-17 failed after application of only 30 cycles. Figure 19 shows photographs of the models after test. No further tests were attempted on HGS-15 after 1500 cycles to 6500 psi, although no damage was apparent in either hemisphere.

Inspections conducted during the earlier tests showed that the GRP gasket (0.005 in. thick) was severely damaged in some of the models. Repeated loads had caused the glass to cut through the fiberglass layer at the inner edge. This was observed at a pressure level of 6500 psi or a membrane stress of 59,200 psi. The cutting in this area is attributable

mainly to high-contact stresses caused by the slightly raised inner edge of the bearing face. Once the deterioration was observed, the model was disassembled and reset with a new gasket. In later tests, an attempt was made to improve the durability of the gaskets by overlapping the fiber ribbons to obtain a more densely packed gasket. This also caused an increase of 0.010 to 0.015 in. in gasket thickness. It appears that some success was achieved since there was no apparent cutting through of the gaskets even after as many as 11,000 cycles of pressure to membrane stress levels between 23,000 and 59,000 psi.

Two types of joint rings were investigated in the tests. The Mod 1 ring had only the inner wall whereas the Mod 2 ring had inner and outer walls. Although the data are limited, one interesting observation can be made regarding the damage that occurred. In all of the tests conducted, the most frequent type of damage observed was at the inner edge of the bearing face. In some instances, it was noted that spalling occurred at the outer edge and in each of these cases (Hemispheres 3, 13, and 18) the models were assembled with Mod 1 type ring. It would appear that the outer wall of the Mod 2 type ring provides better support at the outer radius and may help to prevent the occurrence of spalling. Although the epoxy at the outer radius of a Mod 1 type ring is expected to cause a reaction, it is possible that the less confined condition permits yielding and extruding to occur. If this does take place at the outer edge, the only reaction at the corner that can be expected is that from hydrostatic pressure. Since no spalling was observed at the outer edge of a hemisphere assembled with a Mod 2 type ring, greater confidence can be placed on this geometry.

Six PPG 1578 glass hemispherical shells with reinforced joints were tested. The results are shown in Table 4. Although the first assembly HGS 20 performed extremely well, surviving as many as 15,000 cycles to depths ranging from 14,600 to 30,000 ft, the last 2 assemblies failed catastrophically in the very early stages of the cyclic progression. HGS 21 survived 2000 cycles to 14,600 ft and failed after 300 cycles to 17,200 ft. HGS 22 failed after 1532 cycles to 14,600 ft. For this geometry the average bearing stress at 14,600 ft is 38,000 psi. Based on these results and those obtained on constant thickness PPG 1578 glass hemispherical shells, it appears that bearing loads in excess of about 30,000 ksi should be avoided for this glass, method of treatment and assembly procedure.



### CORNING 0313 GLASS

Only one spherical assembly of Corning Chemcor 0313 glass was tested. The model failed catastrophically after 218 cycles to 5000 psi (stress of 46,000 psi). The results of this one test appear to be consistent with results obtained by NOL. They have observed cracks at the inner edge after 675 cycles to 3000 psi. In two other tests, catastrophic failure resulted within 5 cycles when a pressure of 9000 psi was applied. In view of these results, no further attempts were made to continue these tests.

### PPG 1080 GLASS

The 3 spherical assemblies of PPG 1080 Na<sup>+</sup> were all tested to a pressure of 10,000 psi in fatigue.

Model HGS 1 survived 106 cycles to 10,000 psi. Inspection of the glass at this level revealed no apparent damage to the model and therefore it was placed back in the test facility. While pressure adjustments were being made in the cyclic system, the model failed at a pressure of 8300 psi.

Model HGS 2 survived 715 cycles to 10,000 psi. The model was inspected after 1, 10, 300, and 700 cycles and gave no indications of damage. After inspection at 700 cycles, the model was put back in the test tank. It failed on the 715th cycle, while pressure was being applied at 9000 psi.

Model HGS 3 survived a total of 2380 cycles to 10,000 psi. The last inspection of the model was after 1100 cycles at which time no damage was apparent except for some pits on the inner and outer surfaces of one hemisphere. The model failed on the 2380th cycle, while pressure was being applied at 9000 psi.

The failure of Models HGS 1, 2, and 3 is believed to have occurred at the joint. In each case the fractured glass in the titanium ring was in the form of very fine white powder that had a considerably finer grain than all other pieces of fractured glass. A photograph is shown in Figure 19. The average bearing stress at 10,000 psi for this geometry is 72,000 psi. Since the residual surface compression on PPG 1080 Na<sup>+</sup> models

is similar to 1578 glass it is not surprising that failure occurred on HGS 1, 2, and 3. None of the PPG 1578 hemispheres survived more than 380 cycles at a stress of 70,000 psi.

Nine hemispherical shells of PPG 1080  $K^+$  models were tested. The results are shown in Table 3. Each of the hemispheres survived a minimum of 3000 cycles to a depth of 20,000 feet. Seven of the 9 hemispheres were subjected to as many as 12,500 cycles to depths ranging from 24,600 to 27,500 feet. All 9 hemispheres were then proof tested to a depth of 30,000 feet. The results of these tests are some of the most encouraging obtained to date. In view of the repeatability of the tests and the fact that 7 hemispheres survived at least 500 cycles to 27,500 feet (bearing stress of 87,000 psi) it is estimated that reliable performance from PPG 1080  $K^+$  10 in. diameter models can be obtained at a stress of 64,000 psi.

The significant difference in performance of PPG 1578  $Na^+$  and PPG 1080  $K^+$  models is attributed to the effects of the ion exchange treatment. The average modulus of rupture for unabraded 1578  $Na^+$  glass based on concentric ring tests of 21 samples of 3/8 in. plate was 70,800 psi. These plate specimens were ion exchanged with the hemispherical shell models. The average modulus of rupture for unabraded 1080  $K^+$  glass based on concentric ring tests of 15 samples of 0.115 in. plate was 90,300 psi. Probably as important as the difference in strengths is the fact that 1578  $Na^+$  glass is more susceptible to strength degradation from mechanical abrasion than is 1080  $K^+$  glass. Although only 2 abraded (sand blasted) specimens of 1578  $Na^+$  glass were tested there is strong indication that the abraded strength may be more than 30 percent less than the unabraded strength. NOL, in independent tests, reports an average modulus of rupture of 37,000 psi for the abraded condition. By comparison, the 1080  $K^+$  glass shows very little effect from mechanical abrasion. The 14 abraded 1080  $K^+$  specimens had an average modulus of rupture of 84,000 psi or only about 7 percent less than the unabraded strength. Under bearing loads as in the case of hemispherical shells, it would be suspected that mechanical abrasion plays a role in the fracture process.

The reproducible results obtained on PPG 1080 K<sup>+</sup> glass hemispherical shells indicates that they are practical for unmanned *noncritical* conditions to 20,000 ft for the size investigated (10 inches). Additional effort is required to study the effects of exposure to marine environment, design details to ensure water tight integrity, and the effects of thermal shock and dynamic loads. Although the results obtained on PPG 1080 models are encouraging, a considerable effort is necessary before glass can be considered practical for critical application even on the present scale. The basic requirement in critical applications as detailed in Reference 14 is that the glass structure not present a hazard that may affect the material adequacy of the submersible. In essence the glass structure must be as reliable as the submersible's pressure hull. To begin with surface compressed glasses, especially those that are tempered in potassium bath have very shallow compression layers, on the order of 5 mils. The glass surface contains numerous microflaws which are believed to play an important role in the fatigue fracture process. At the present time strength controlling features in glass at this level cannot be identified and thus an acceptable method of distinguishing a good specimen from a bad one does not exist. Proof testing methods which have been applied to metallic structures may not be sufficient for critical glass structures, unless it can be shown that significant damage was not incurred during the overstressing. Finally, before a glass structure can be considered practical for critical use, in service inspection techniques are necessary to assure structural adequacy.

#### SUMMARY

1. The finite element method of stress analysis is useful in understanding the behavior of glass structures although it is not a panacea for the joint problem. This is so because flaws which are not considered in the analysis play a role in the fatigue fracture

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<sup>14</sup>"Material Configuration Procedures and Criteria Manual for Manned Noncombatant Submersibles," NAVSHIPS 0900-028-2010 (Sep 1968).

process. It nevertheless provides a description of the gross stresses. Two joints tested in the past that had resulted in "premature" fractures were discovered to have areas of tensile stress. The analysis applied in a parametric study also demonstrated the sensitivity of glass to changes in material properties of the metal ring and gasket layer. Round glass bearing surfaces were found to be highly sensitive to changes in properties of the gasket layer whereas, flat bearing surfaces were not.

2. Significant difference in fatigue performance between PPG 1578 and PPG 1080 chemically strengthened glass hemispherical shells was noted. Catastrophic failure was observed at a bearing stress of 38,000 psi on PPG 1578 glass, whereas, no failure has been observed on the 1080 hemispheres at bearing stresses as high as 64,000 psi. The difference is attributed to the ion exchange treatments. The 1080 glass treated in potassium inherently produces a higher residual surface compression stress and is less susceptible to strength degradation from mechanical abrasion than is the 1578 glass treated in sodium.
3. Tests of 24 10-inch-diameter glass hemispherical shells of PPG 1578 Na<sup>+</sup> of constant thickness and variable wall with titanium joint rings were disappointing. First fracture on the constant thickness shells was observed at a bearing stress of 46,000 psi and on the variable wall shells at a stress of 38,000 psi. Although great care was taken in the design and fabrication of the glass "premature" fracture nevertheless occurred. It is therefore concluded that the present technology does not permit use of this glass to bearing stress in excess of 30,000 psi for the size tested.
4. Tests of 9 10-inch-diameter 0.36 wall PPG 1080 K<sup>+</sup> glass hemispherical shells with titanium joint rings were quite encouraging. Each hemisphere survived at least 3000 cycles to 20,000 ft and a subsequent proof test to 30,000 ft. At 20,000 ft the bearing stress is 64,000 psi. Because of the reproducible results, 10-inch-diameter 0.36 wall PPG 1080 K<sup>+</sup> glass hemispherical shells are

considered practical for unmanned noncritical conditions to 20,000 ft. Some effort is necessary to study effect of exposure to marine environment, design details to ensure watertight integrity and effects of thermal shock and dynamic loads.

5. Although some encouraging data was obtained in this program a considerable effort is necessary before surface strengthened glasses can be considered practical for critical applications, even for the size tested.

#### ACKNOWLEDGMENTS

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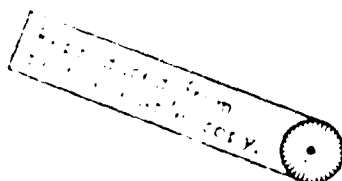
22



INTERSECTION OF  
OUTER CURVED  
SURFACE  
AND BEVEL

INTERSECTION OF  
BEVEL SURFACE  
AND FLAT  
BEARING FACE

Figure 2 - Grinding Flaws at Beveled Edge



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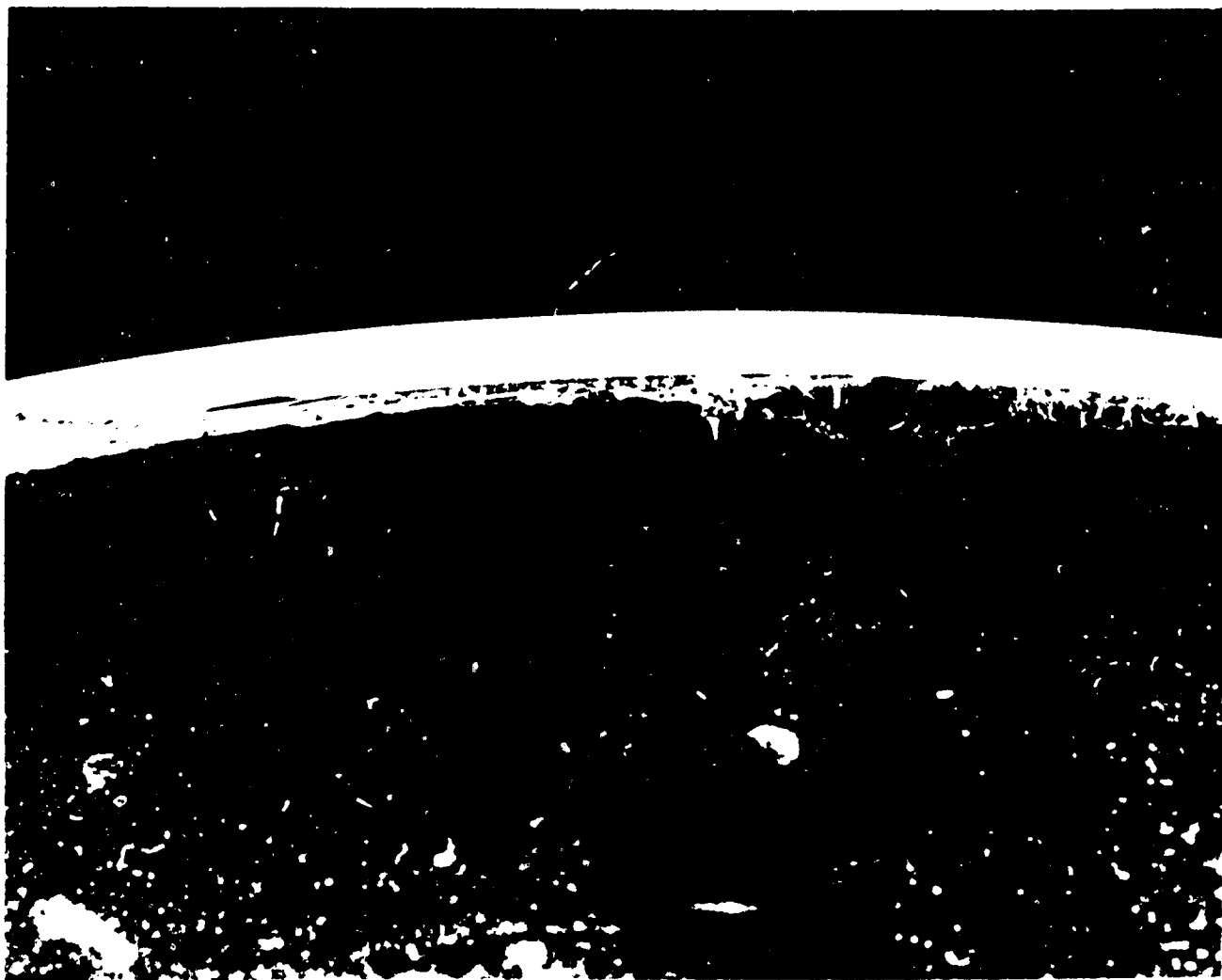


Figure 3 - Annealed Glass Hemisphere after Static Test  
to 17,000 psi

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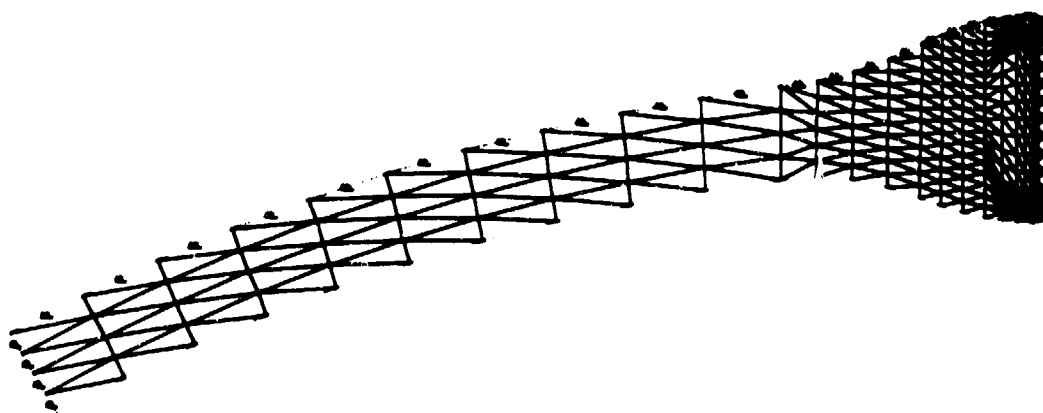


Figure 4a - Structure Idealization

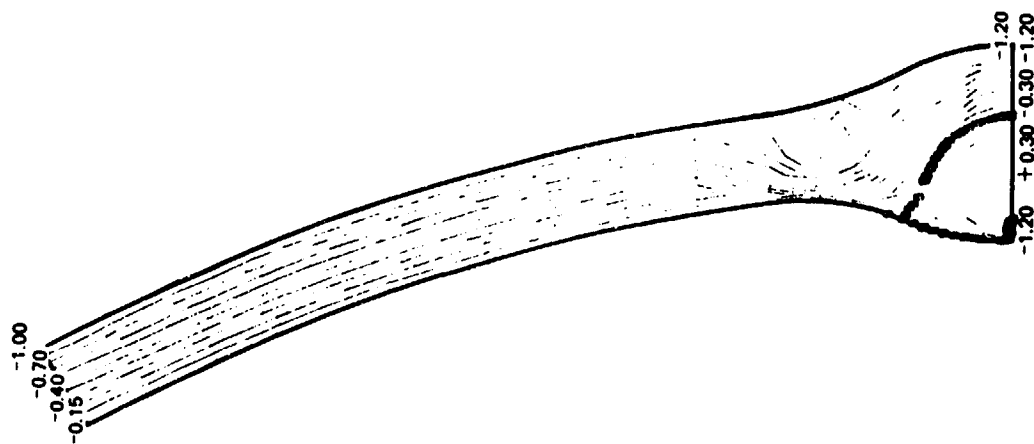


Figure 4b - Radial Stress

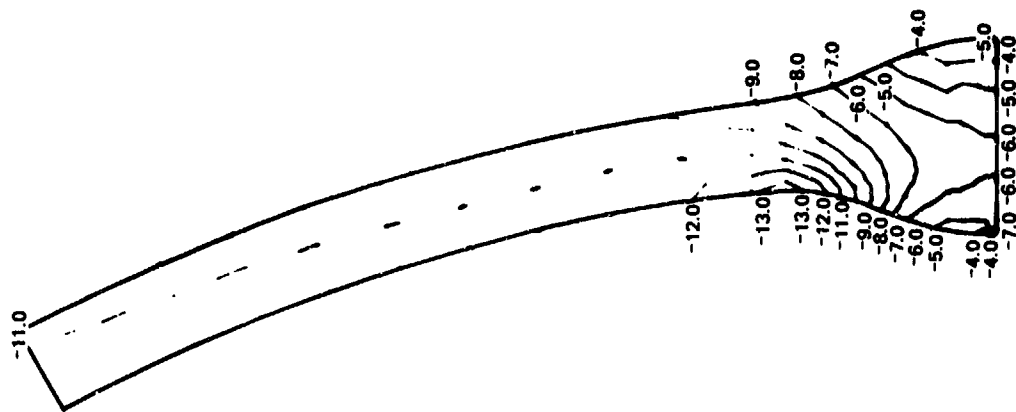


Figure 4c - Meridional Stress

Figure 4 - Analysis of Reinforced Joint Design



Figure 5 - Surface Compressed Hemisphere with Reinforced Joint after  
10 Cycles to 10,000 psi

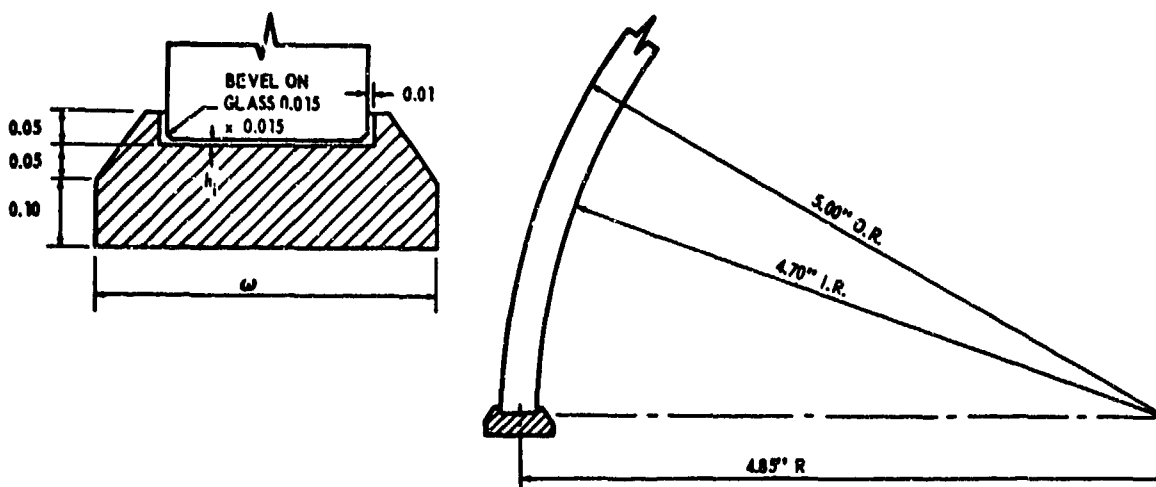


Figure 6a - Flat Juncture (G1)

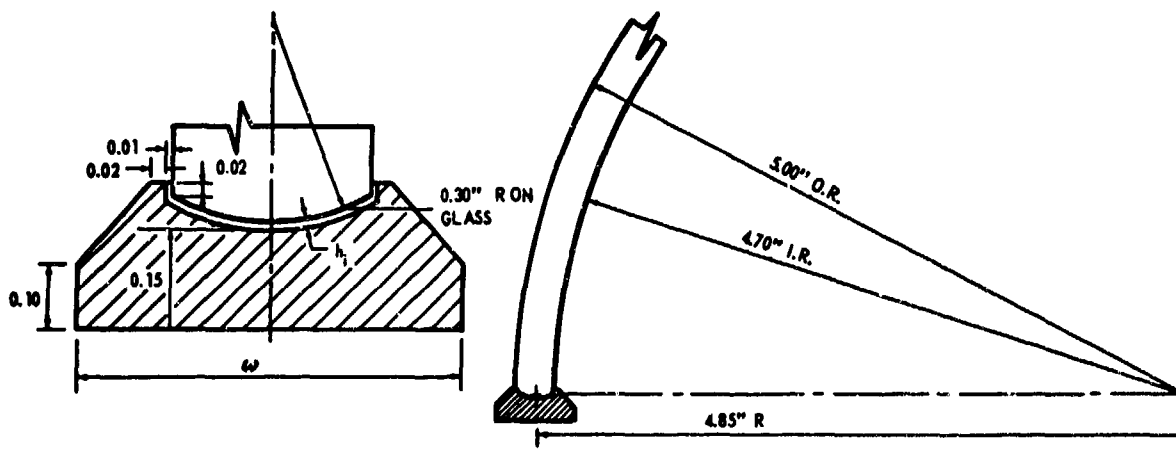


Figure 6b -  $R = h$  Toroid (G2)

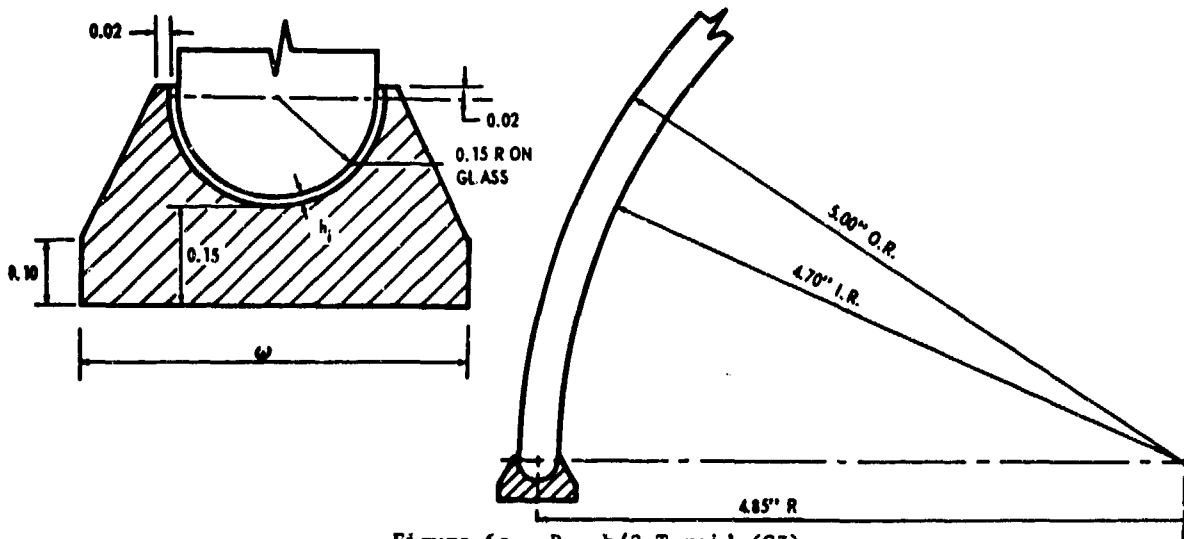


Figure 6c -  $R = h/2$  Toroid (G3)

Figure 6 - Joint Geometries for Parametric Study

Figure 7 - Stress Contours

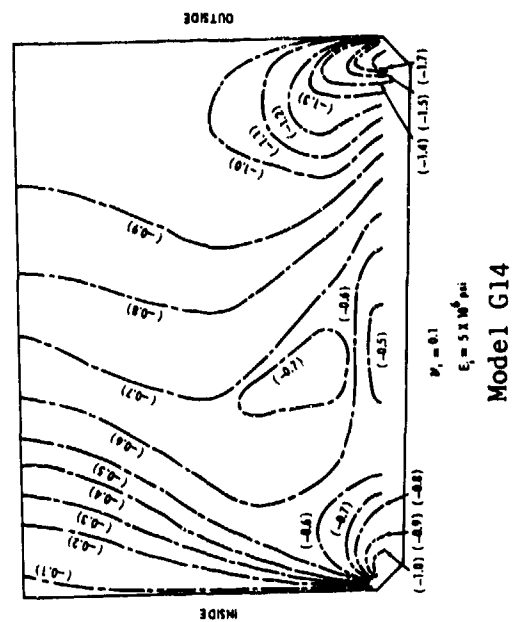
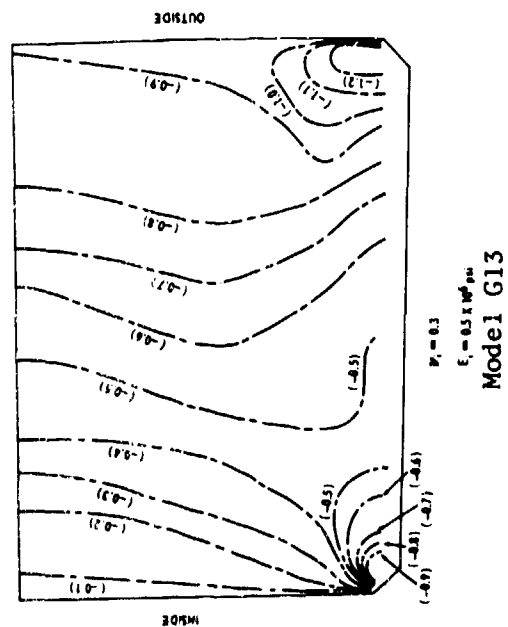
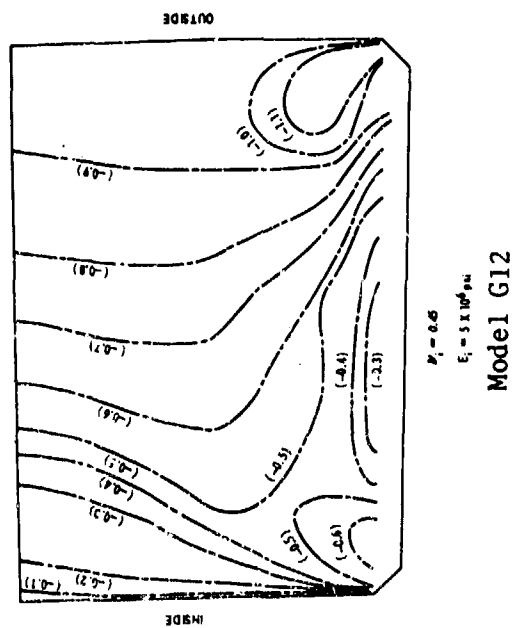
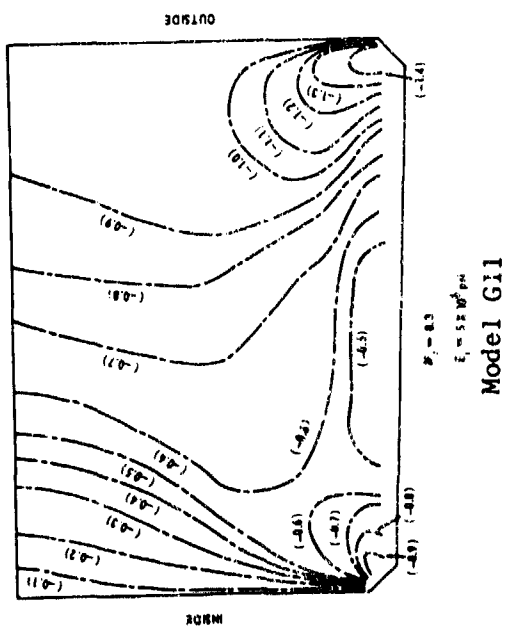
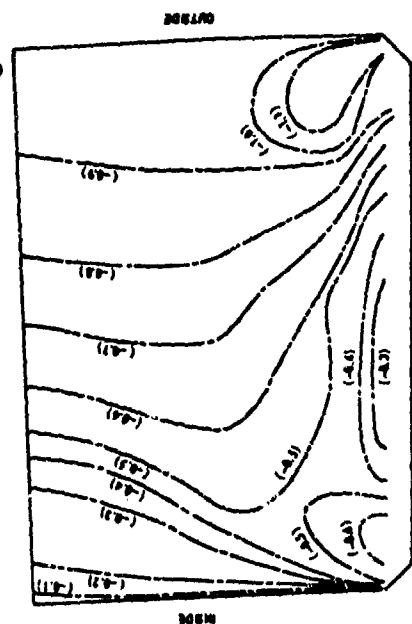
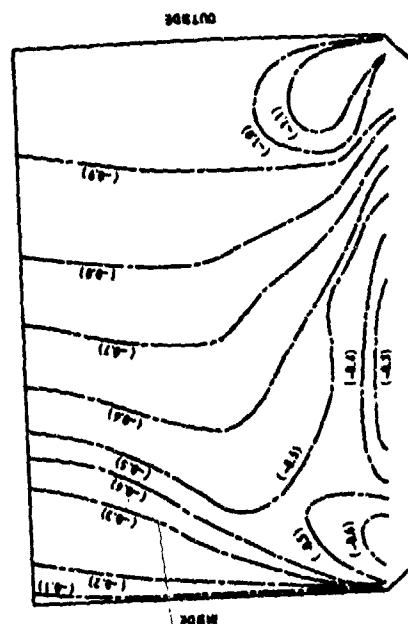


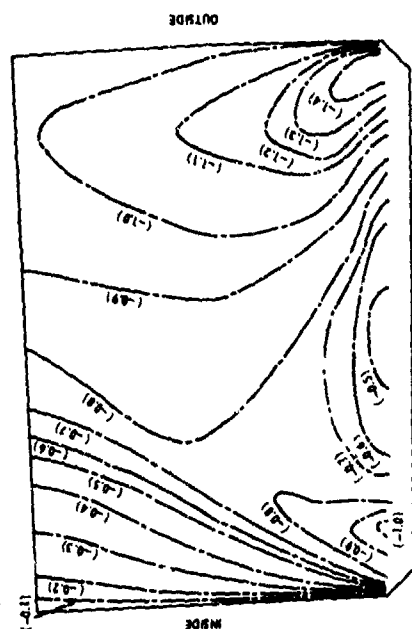
Figure 7 (continued)



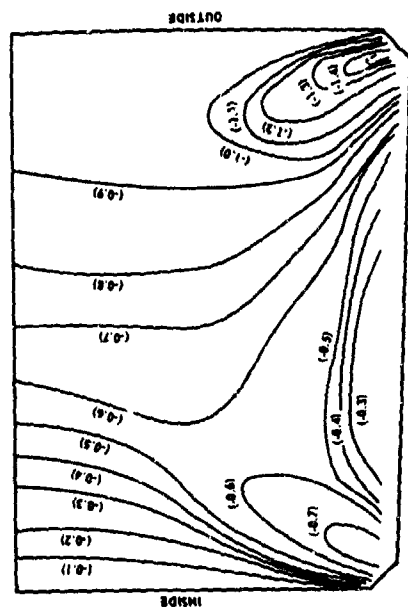
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 $\xi_1 = 0.1 \times 10^{-4}$   
 Model G15



$\eta_1 = 0.6$   
 $\xi_1 = 0.1 \times 10^{-4}$   
 Model G17

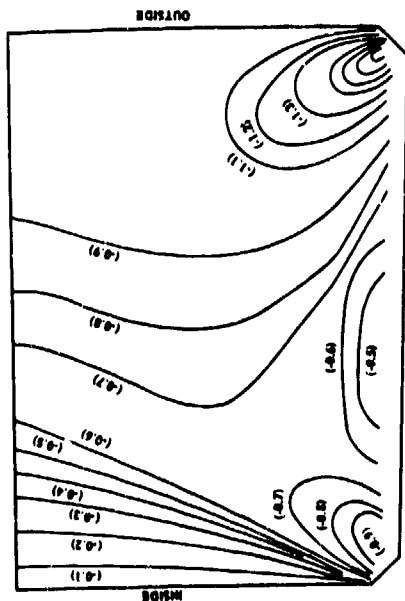


$\eta_1 = 0.1$   
 $\xi_1 = 0.1 \times 10^{-4}$   
 Model G16



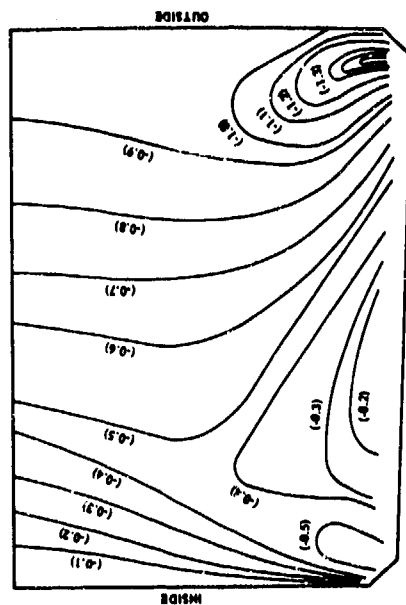
$\eta_1 = 5 \times 10^4$   
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 $\eta_2 = 0.009$   
 Model G18

Figure 7 (continued)



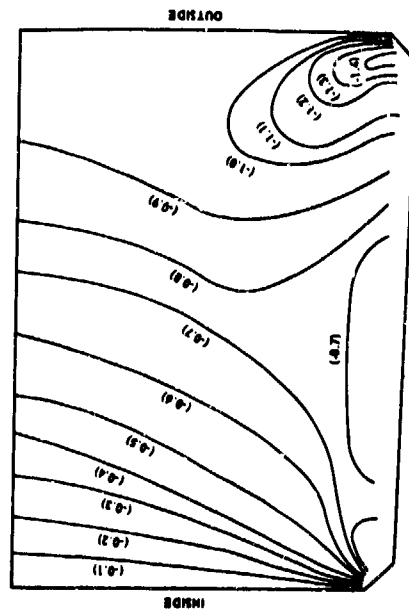
$E_1 = 0.5 \cdot 10^6$   
 $\nu_1 = 0.25$   
 $\nu_2 = 0.30$

Model G18a



$E_1 = 5 \cdot 10^6$   
 $\nu_1 = 0.25$   
 $\nu_2 = 0.30$   
 $\nu_3 = 0.40$   
 $E_2 = 15 \cdot 10^6$

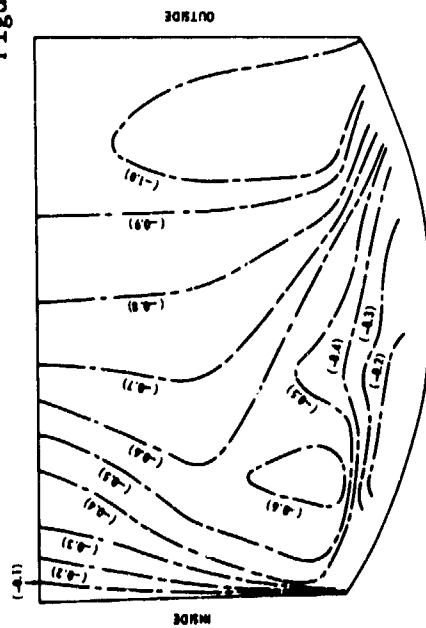
Model G19



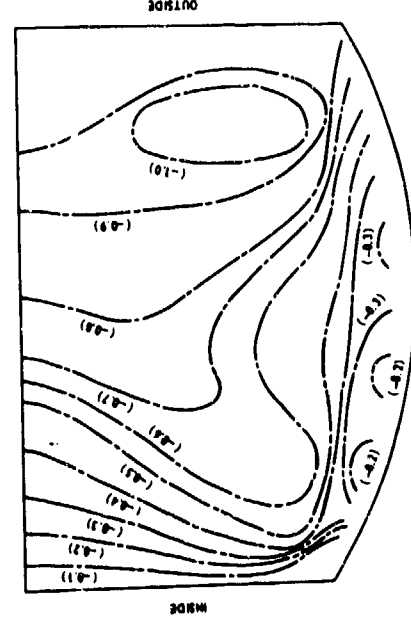
$E_1 = 5 \cdot 10^6$   
 $\nu_1 = 0.25$   
 $\nu_2 = 0.30$   
 $\nu_3 = 0.40$   
 $E_2 = 15 \cdot 10^6$

Model 19a

Figure 7 (continued)



$P_1 = 0.1$   
 $E_1 = 5 \times 10^6 \text{ psi}$   
 Model G21



$P_1 = 0.05$   
 $E_1 = 5 \times 10^6 \text{ psi}$   
 Model G23

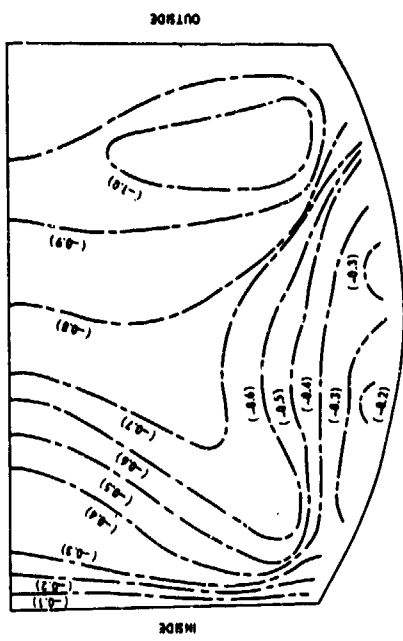
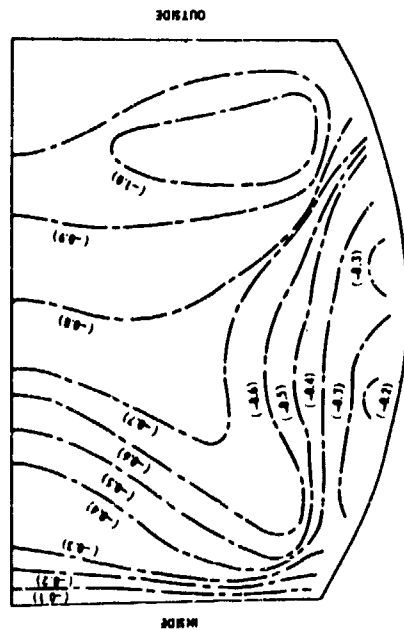
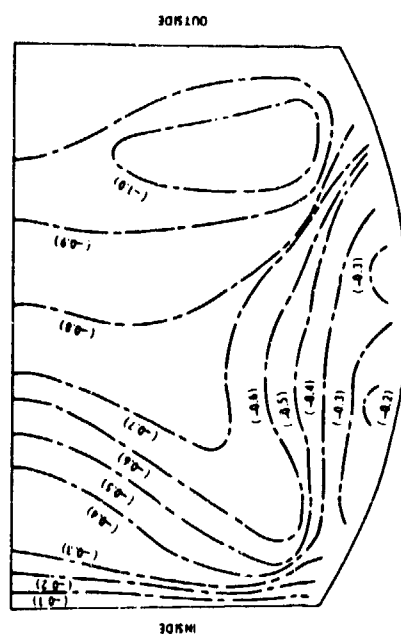


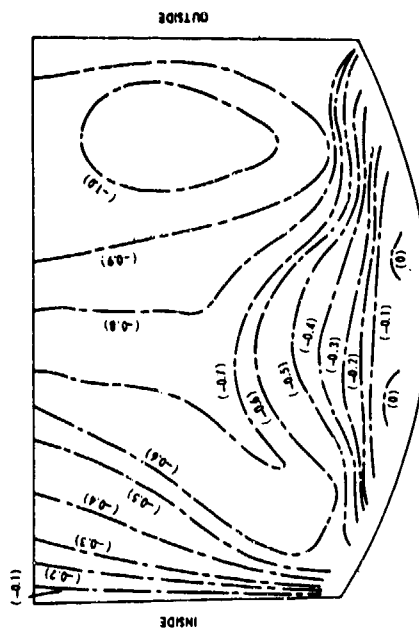
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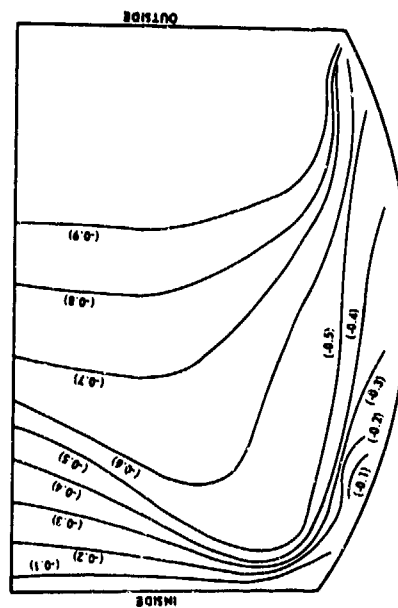
$\mu = 0.3$   
 $E_1 = 5.11 \times 10^6 \text{ psi}$   
Model G25



$\mu = 0.3$   
 $E_1 = 5.11 \times 10^6 \text{ psi}$   
Model G27



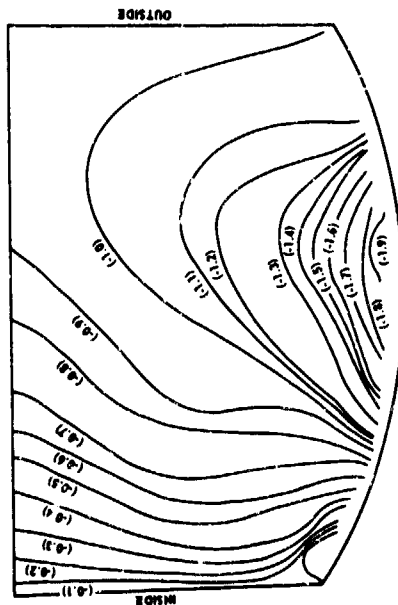
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 $E_1 = 5.0 \times 10^6 \text{ psi}$   
Model G26



$E_1 = 5 \times 10^6$   
 $\mu = 0.3$   
 $\nu_1 = 0.04$   
Model G28

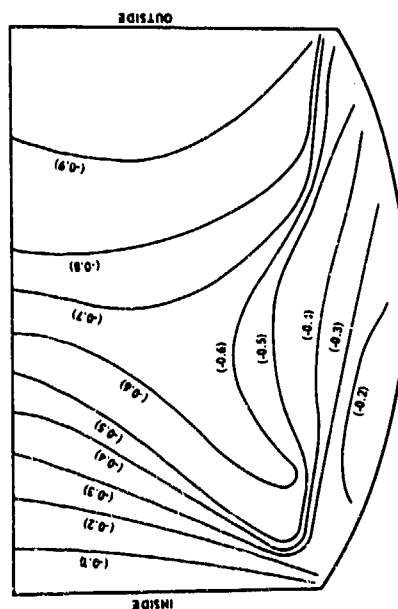


Figure 7 (continued)



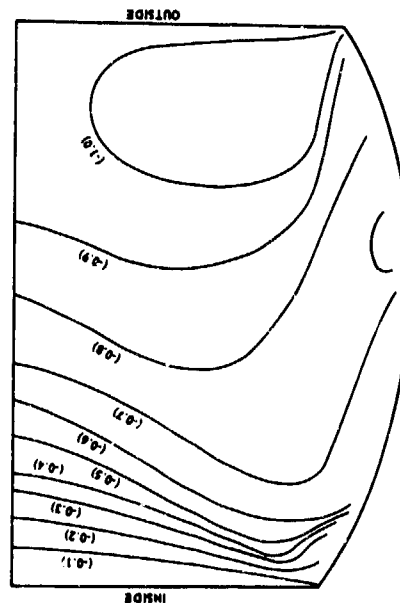
$E_1 = 0.5 \times 10^6$   
 $\mu_1 = 0.45$   
 $\mu_2 = 0.546$

Model G28a



$E_1 = 5 \times 10^6$   
 $\mu_1 = 0.010$   
 $\mu_2 = 0.30$   
 $\nu = 0.40$   
 $E_2 = 15 \times 10^6$

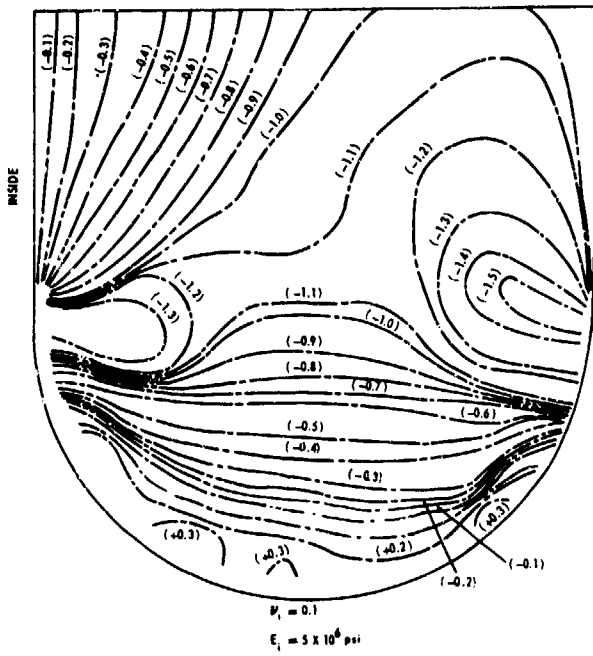
Model G29



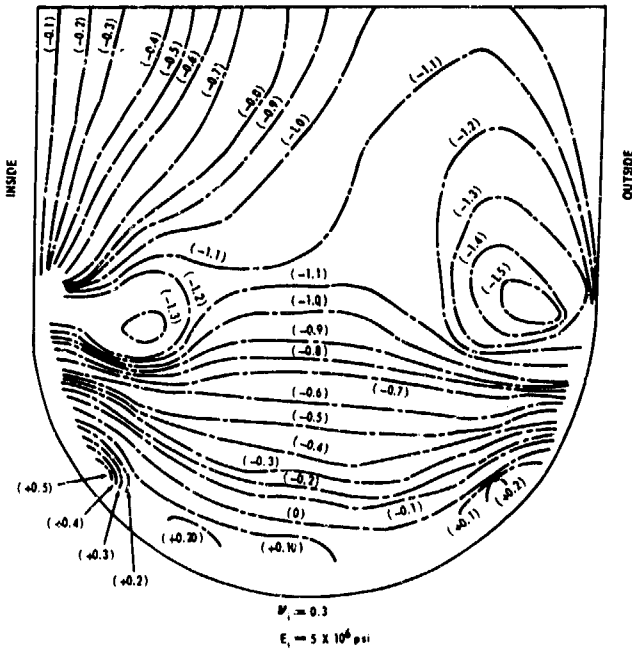
$E_1 = 5 \times 10^6$   
 $\mu_1 = 0.010$   
 $\mu_2 = 0.30$   
 $\nu = 0.40$   
 $E_2 = 30 \times 10^6$

Model G29a

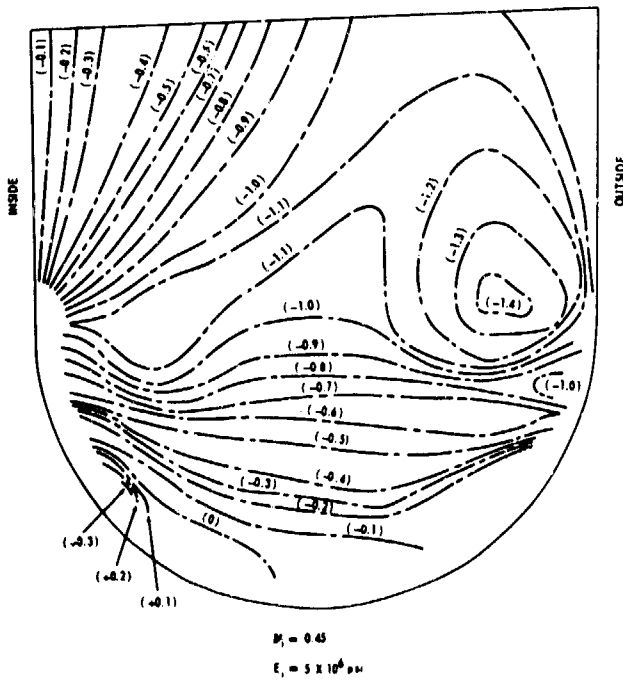
Figure 7 (continued)



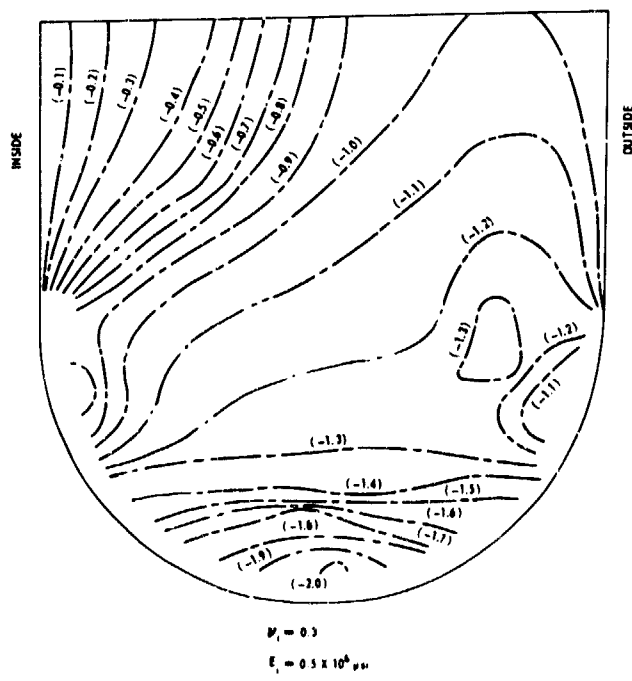
Model G31



Model G32

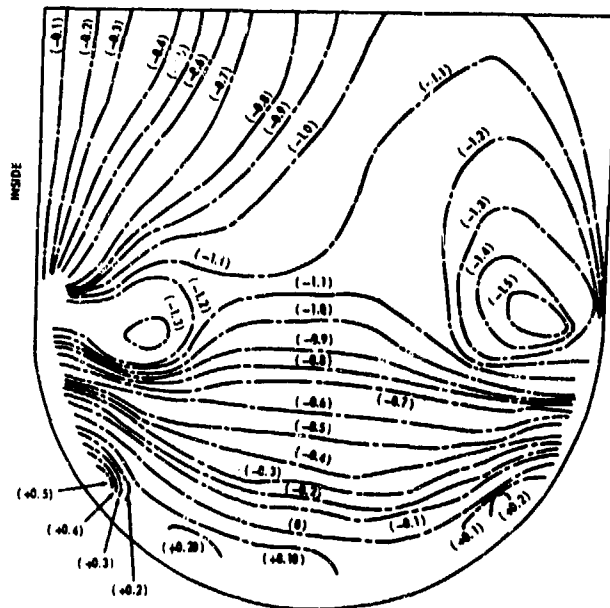


Model G33

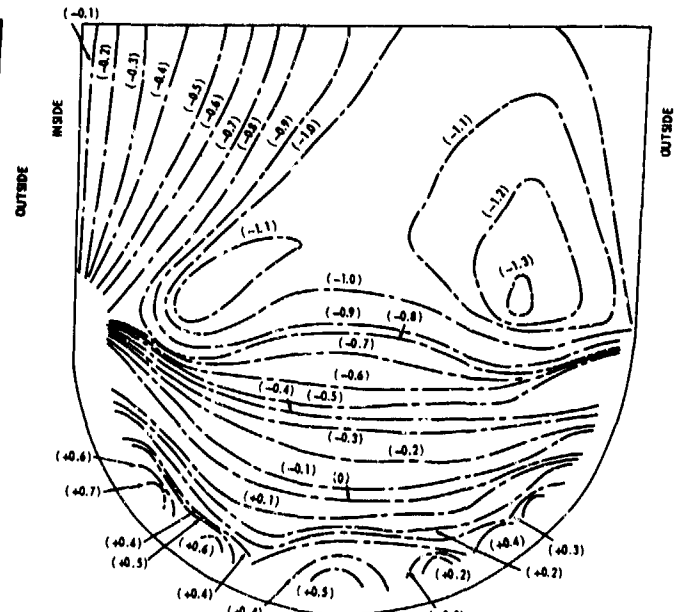


Model G34

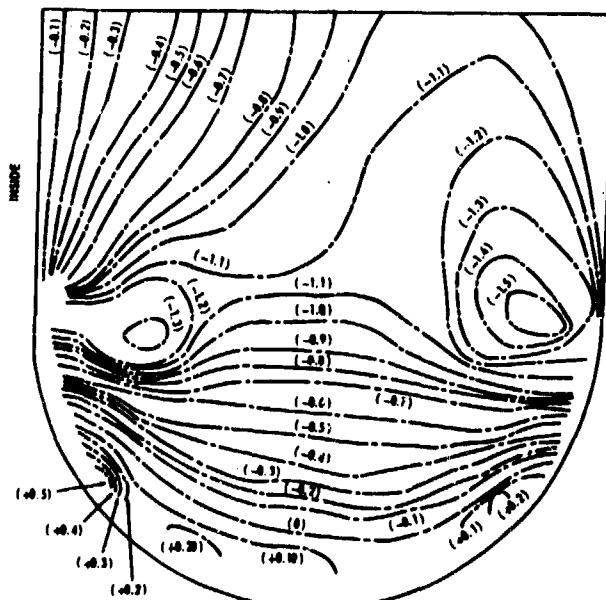
Figure 7 (continued)



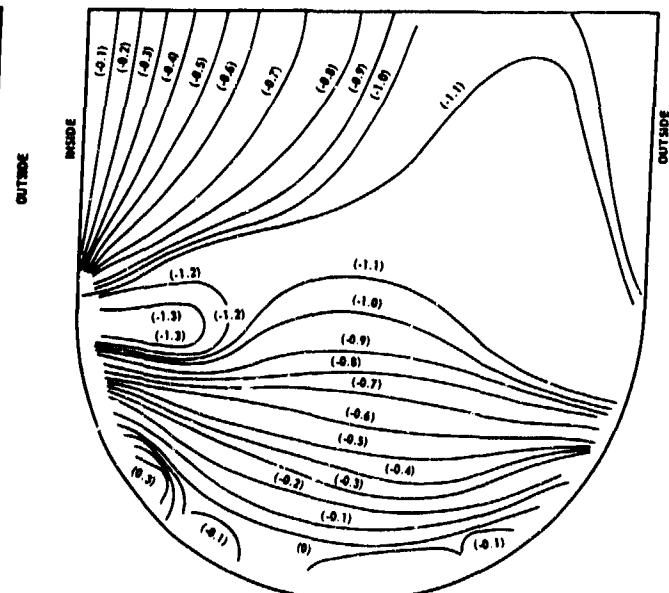
$P_1 = 0.3$   
 $E_1 = 5 \times 10^6 \text{ psi}$   
 Model G35



$P_1 = 0.3$   
 $E_1 = 50.0 \times 10^6 \text{ psi}$   
 Model G36

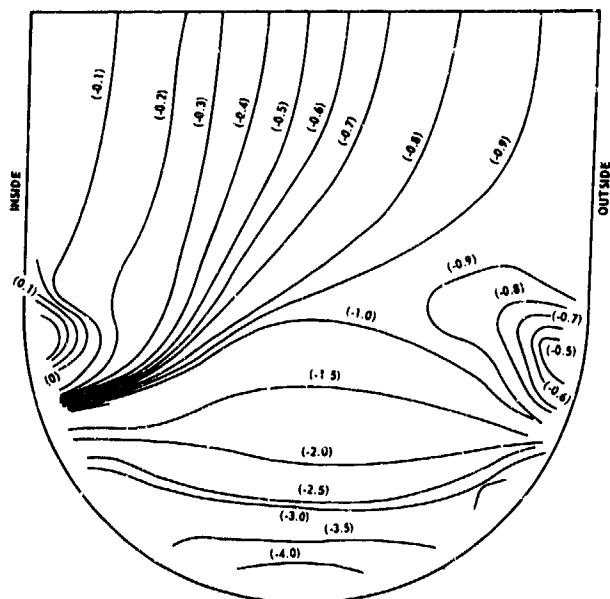


$P_1 = 0.3$   
 $E_1 = 5 \times 10^6 \text{ psi}$   
 Model G37

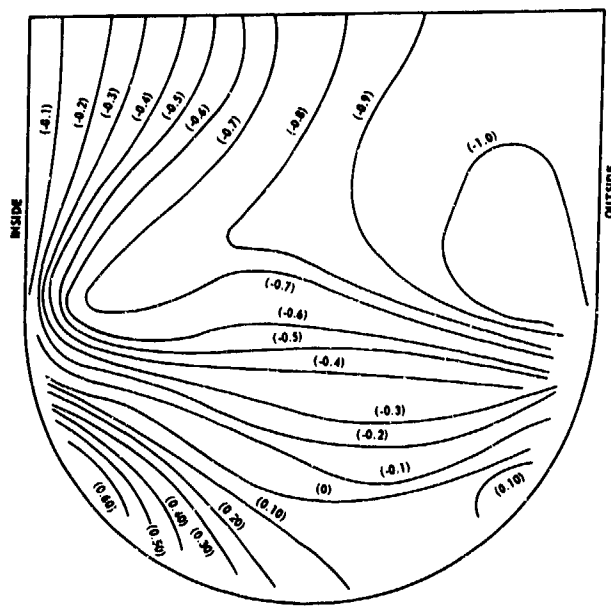


$E_1 = 5 \times 10^6$   
 $P_1 = 0.3$   
 $h_1 = 0.040$   
 Model G38

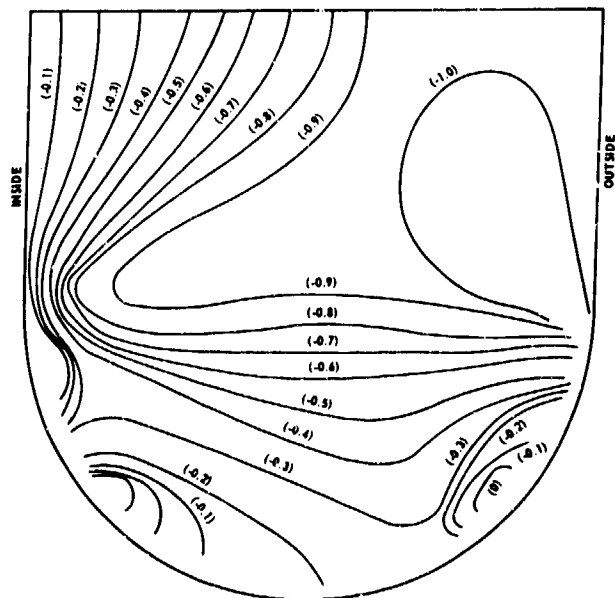
Figure 7 (continued)



$E_1 = 0.5 \times 10^6$   
 $\mu_1 = 0.45$   
 $h_1 = 0.040$   
 Model G38a



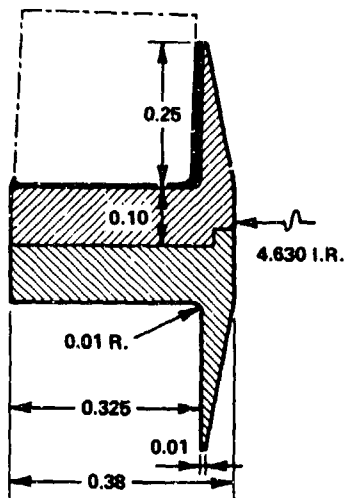
$E_1 = 5 \times 10^6$   
 $h_1 = 0.010$   
 $\mu_1 = 0.30$   
 $W = 0.40$   
 $E_R = 15 \times 10^6$   
 Model G39



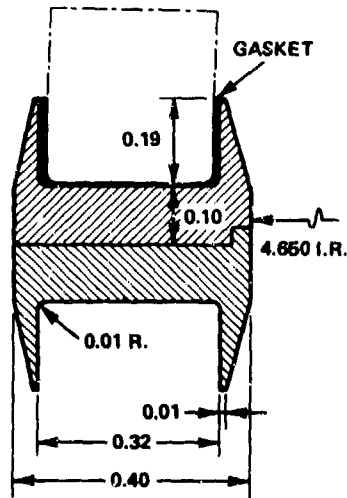
$E_1 = 5 \times 10^6$   
 $h_1 = 0.010$   
 $\mu_1 = 0.30$   
 $W = 0.40$   
 $E_R = 30 \times 10^6$   
 Model G39a

# 0.28 WALL MODELS

# 0.36 WALL MODELS



MOD 1  
Figure 8a



MOD 2  
Figure 8b

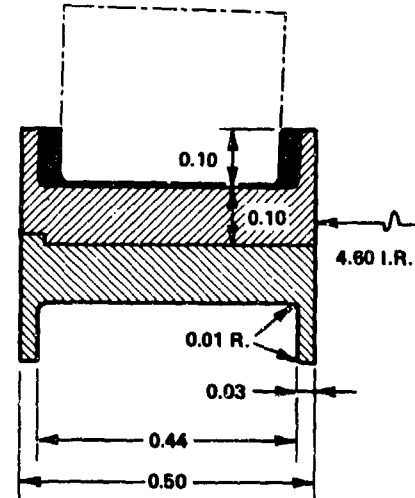


Figure 8c

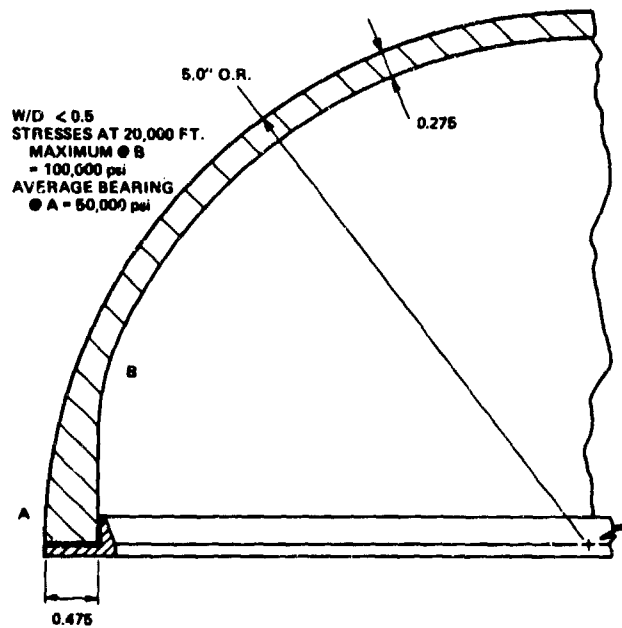


Figure 8d

Figure 8 - Final Joint Designs

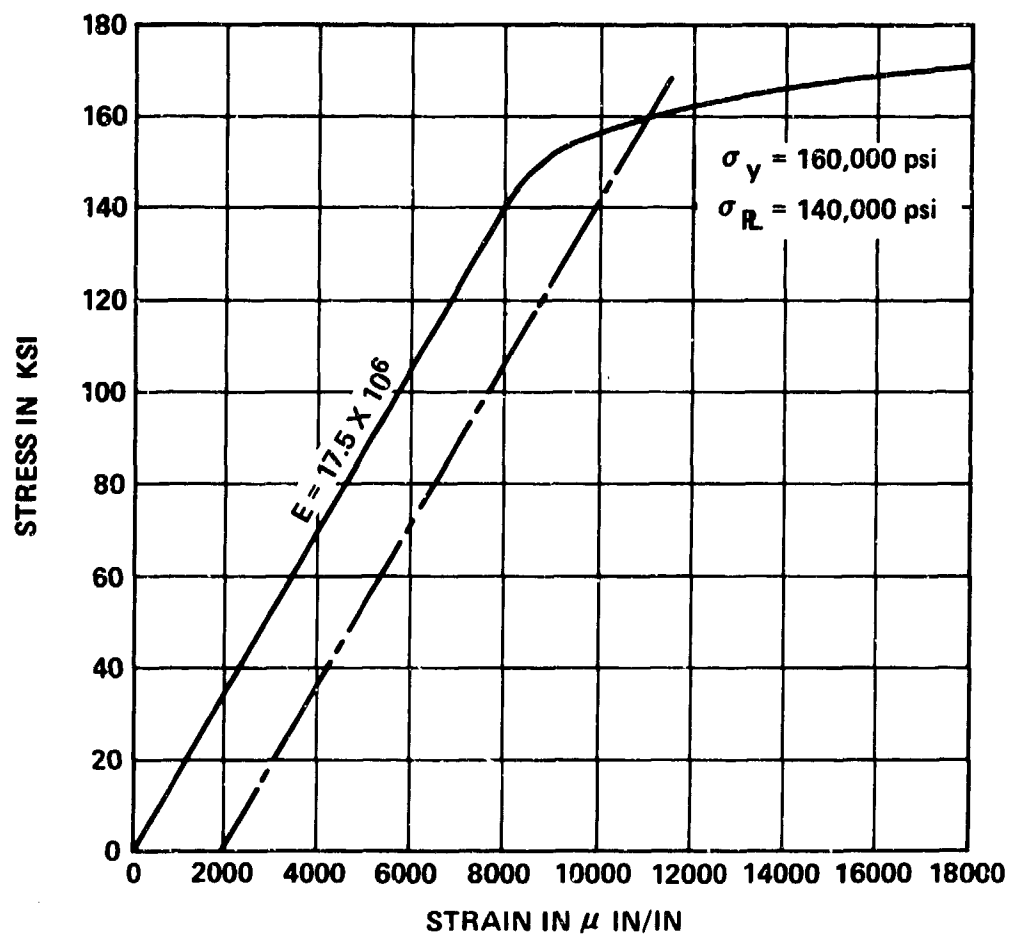


Figure 9 - Compressive Stress-Strain Curve for 662 Titanium

Figure 10 - Analysis of Final Joint Designs

MOD 1 MEMBRANE FOR 0.28 WALL GLASS HEMISPHERE

MATERIAL PROPERTIES:

|           |                                                                                       |
|-----------|---------------------------------------------------------------------------------------|
| TITANIUM  | $E = 17.5 \times 10^6 \text{ psi}$<br>$\nu = 0.3$<br>$\sigma_R = 140,000 \text{ psi}$ |
| GLASS     | $E = 10.5 \times 10^6 \text{ psi}$<br>$\nu = 0.225$                                   |
| INTERFACE | $E = 0.4 \times 10^6 \text{ psi}$<br>$\nu = 0.4$                                      |

LOADS:

|                               |            |
|-------------------------------|------------|
| INCREMENT 1                   | - 1 psi    |
| FIRST YIELDING IN<br>TITANIUM | - 9540 psi |

ZP26

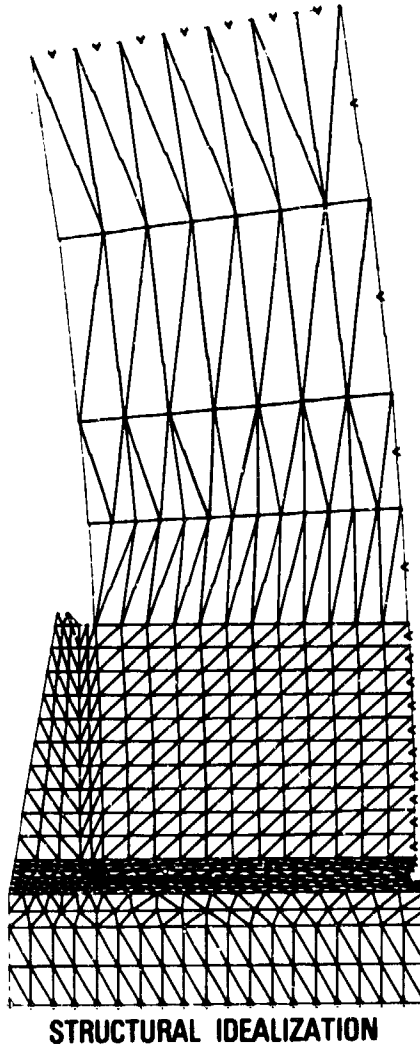
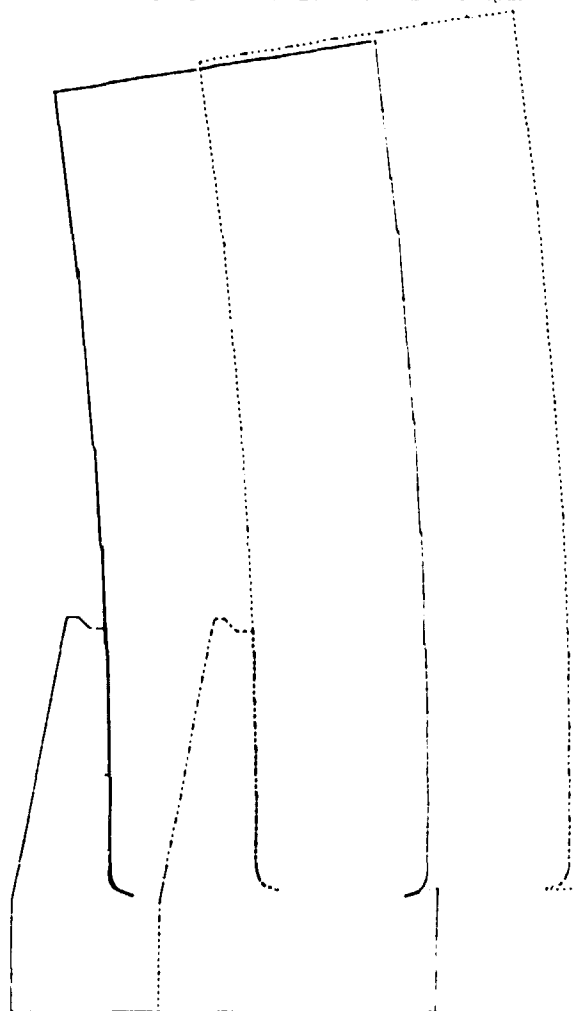


Figure 10a - Mod 1 Structural Idealization

**MOD 1 MEMBRANE RING FOR 0.28 WALL GLASS HEMISPHERE**



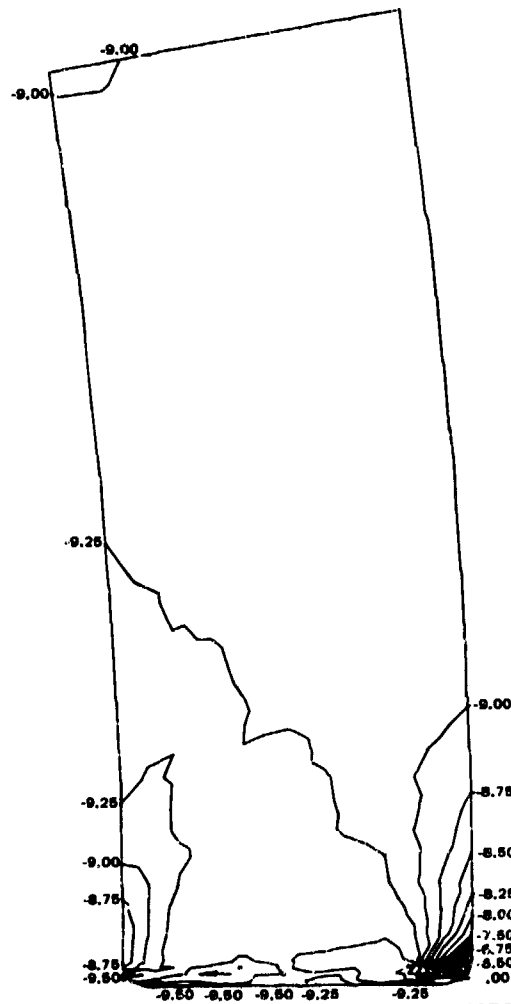
**ZP26 DISPLACED STRUCTURE**

**INCREMENT NUMBER 1**

**Figure 10b - Mod 1 Displaced Structure**



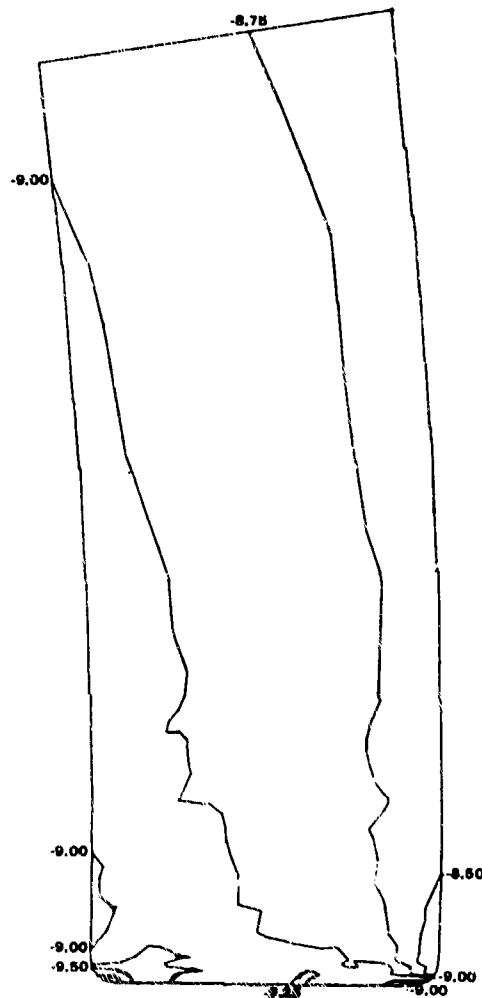
**MOD 1 MEMBRANE RING FOR 0.28 WALL GLASS HEMISPHERE**  
 CONTOUR INTERVAL IS 0.25



**ZP26 CONTOUR PLOT • AXIAL STRESS • INCREMENT NUMBER 1**

Figure 10c - Mod 1 Axial Stress

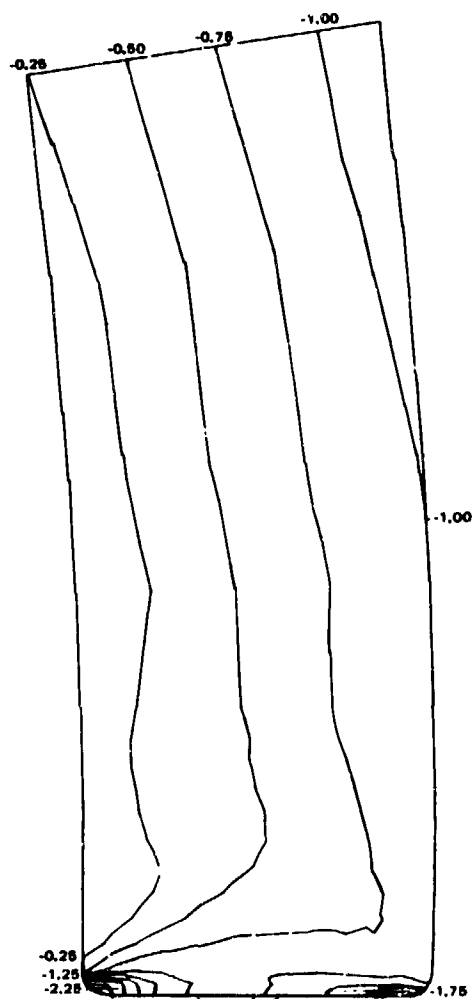
**MOD 1 MEMBRANE RING FOR 0.28 WALL GLASS HEMISPHERE**  
CONTOUR INTERVAL IS 9.36



**ZP26 CONTOUR PLOT • CIRCUMFERENTIAL STRESS • INCREMENT NUMBER 1**

Figure 10d - Mod 1 Circumferential Stress

**MOD 1 MEMBRANE RING FOR 0.28 WALL GLASS HEMISPHERE**  
 CONTOUR INTERVAL IS 0.25



**ZP26 CONTOUR PLOT • RADIAL STRESS • INCREMENT NUMBER 1**

Figure 10e - Mod 1 Radial Stress

# MOD 2 MEMBRANE RING FOR 0.28 WALL HEMISPHERE

## MATERIAL PROPERTIES:

|           |                                                                                       |
|-----------|---------------------------------------------------------------------------------------|
| TITANIUM  | $E = 17.5 \times 10^6 \text{ psi}$<br>$\nu = 0.3$<br>$\sigma_R = 140,000 \text{ psi}$ |
| GLASS     | $E = 10.5 \times 10^6$<br>$\nu = 0.225$                                               |
| INTERFACE | $E = 0.4 \times 10^6$<br>$\nu = 0.4$                                                  |

## LOADS:

|                               |            |
|-------------------------------|------------|
| INCREMENT 1                   | - 1 psi    |
| FIRST YIELDING IN<br>TITANIUM | - 8910 psi |

ZP28

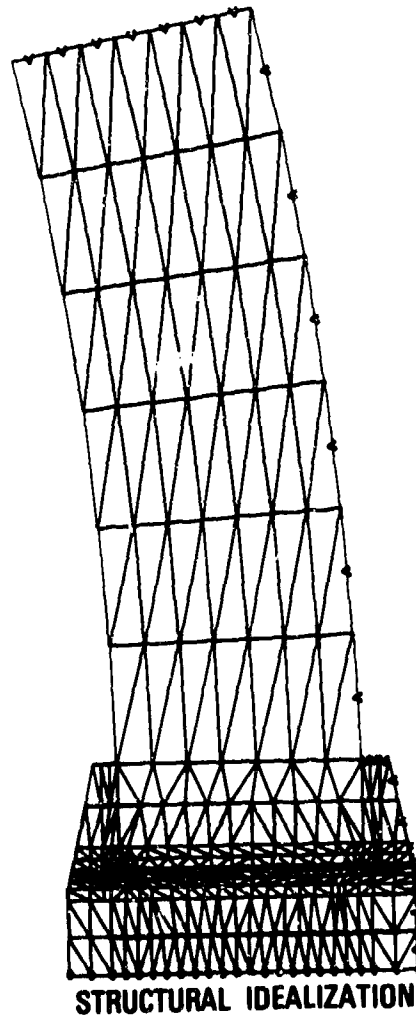
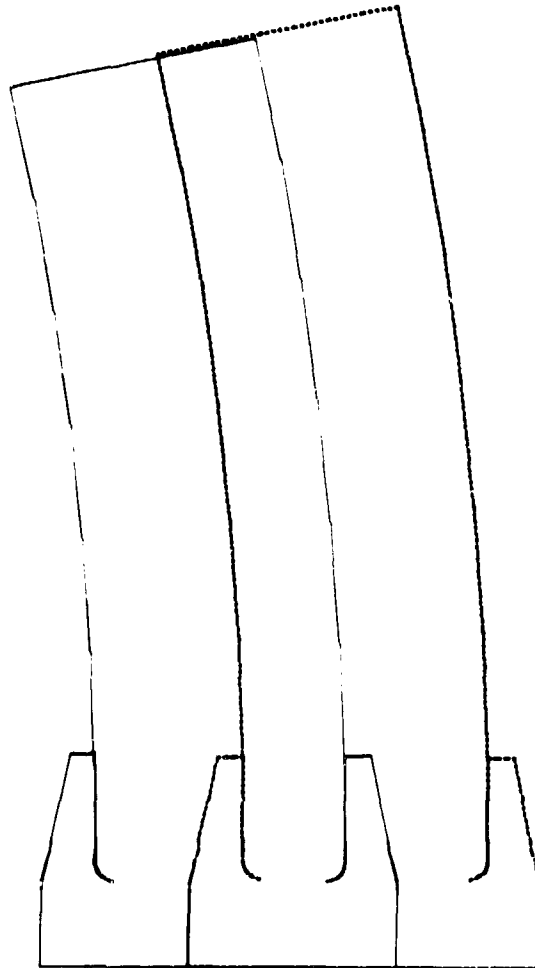


Figure 10f - Mod 2 Structural Idealization

**MOD 2 MEMBRANE RING FOR 0.28 WALL HEMISPHERE**



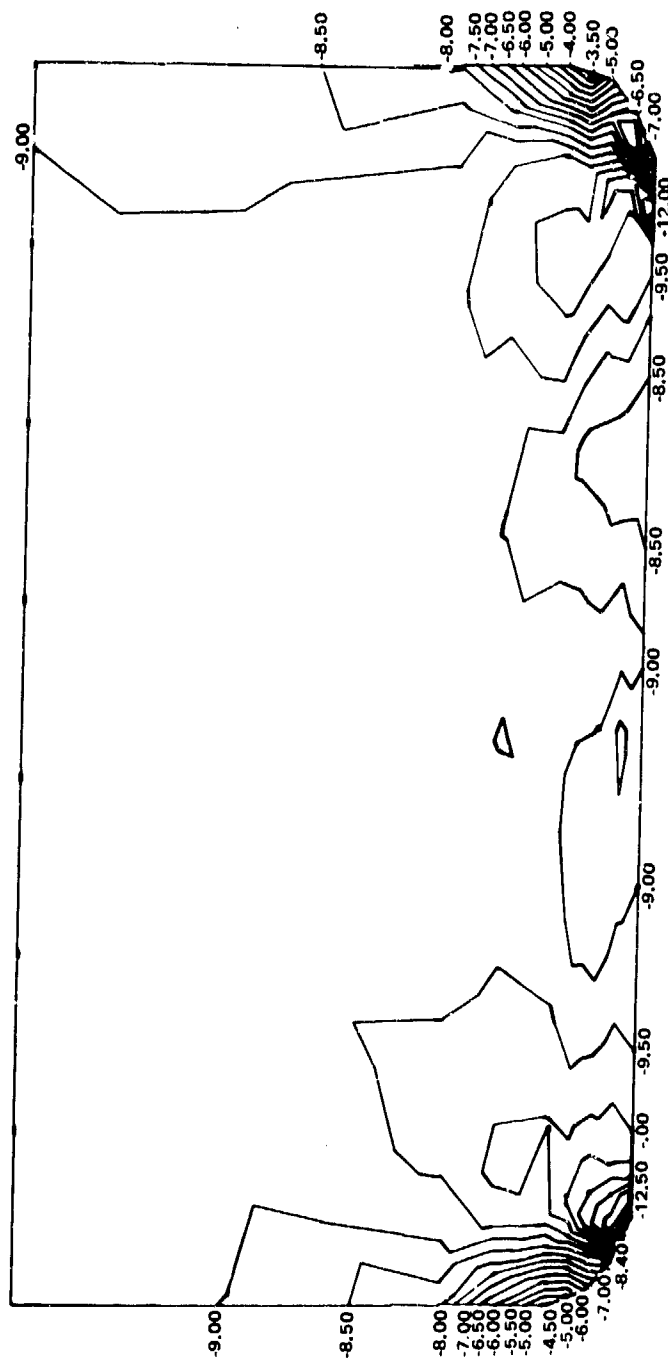
**ZP26 DISPLACED STRUCTURE**

**INCREMENT NUMBER 1**

**Figure 10g - Mod 2 Displaced Structure**

# MOD 2 MEMBRANE RING FOR 0.28 WALL HEMISPHERE

CONTOUR INTERVAL IS 0.50

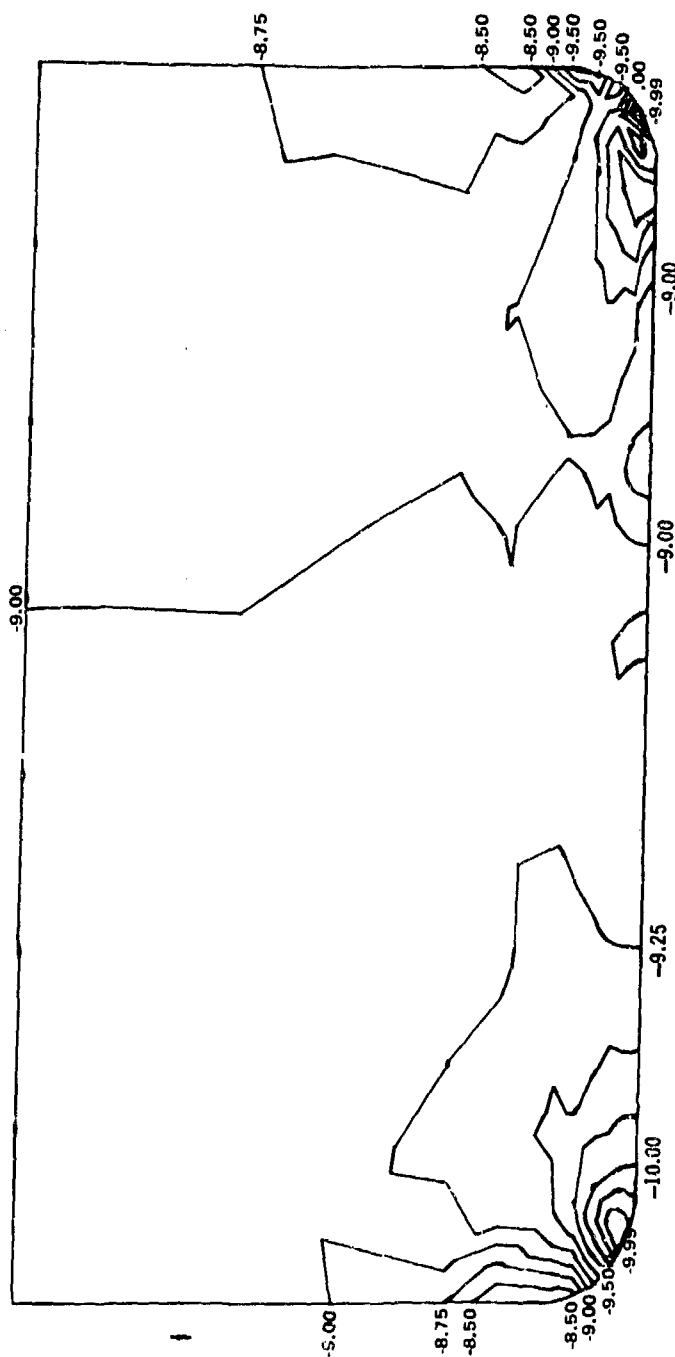


ZP26 CONTOUR PLOT \* AXIAL STRESS \* INCREMENT NUMBER 1

Figure 10h - Mod 2 Axial Stress

# MOD 2 MEMBRANE RING FOR 0.28 WALL HEMISPHERE

CONTOUR INTERVAL IS 0.25

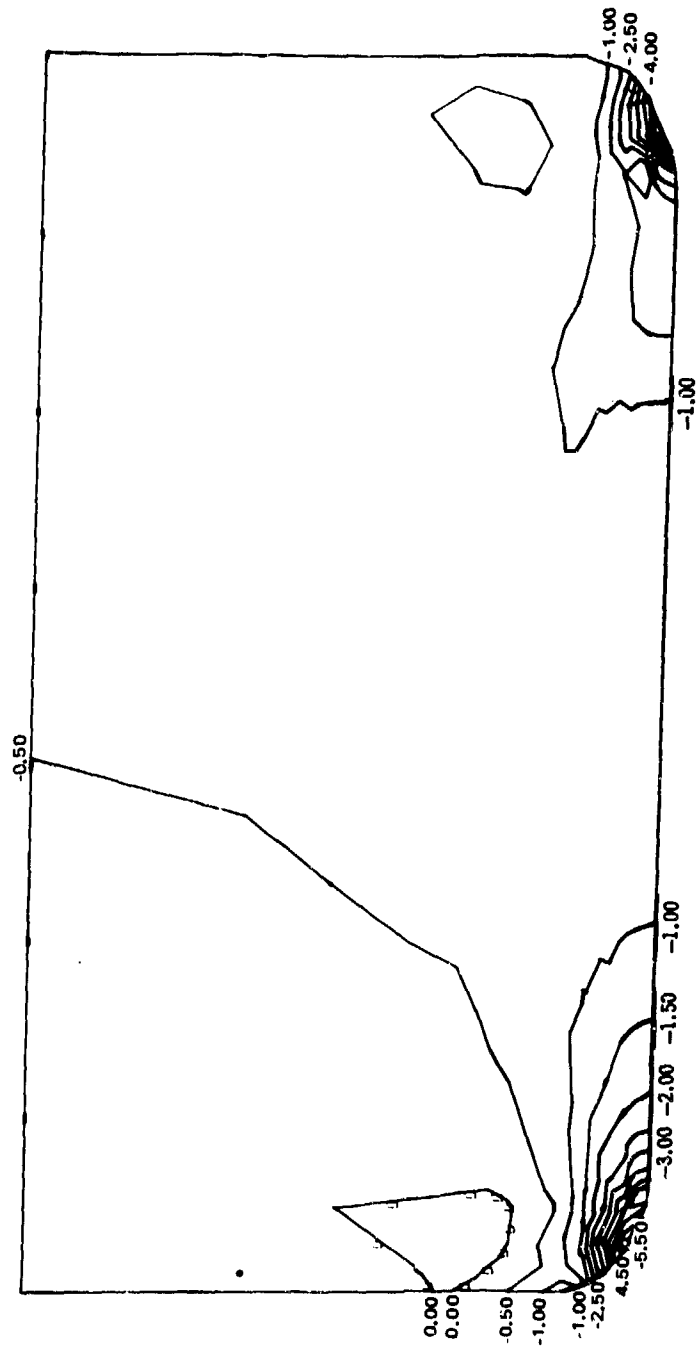


ZP26 CONTOUR PLOT \* CIRCUMFERENTIAL STRESS \* INCREMENT NUMBER 1

Figure 10j - Mode 2 Circumferential Stress

# MOD 2 MEMBRANE RING FOR 0.28 WALL HEMISPHERE

CONTOUR INTERVAL IS 0.50



ZP26 CONTOUR PLOT

\* RADIAL STRESS

\* INCREMENT NUMBER 1

Figure 10k - Mod 2 Radial Stress



## INTERNALLY REINFORCED GLASS JOINT---0.46W/D

### MATERIAL PROPERTIES:

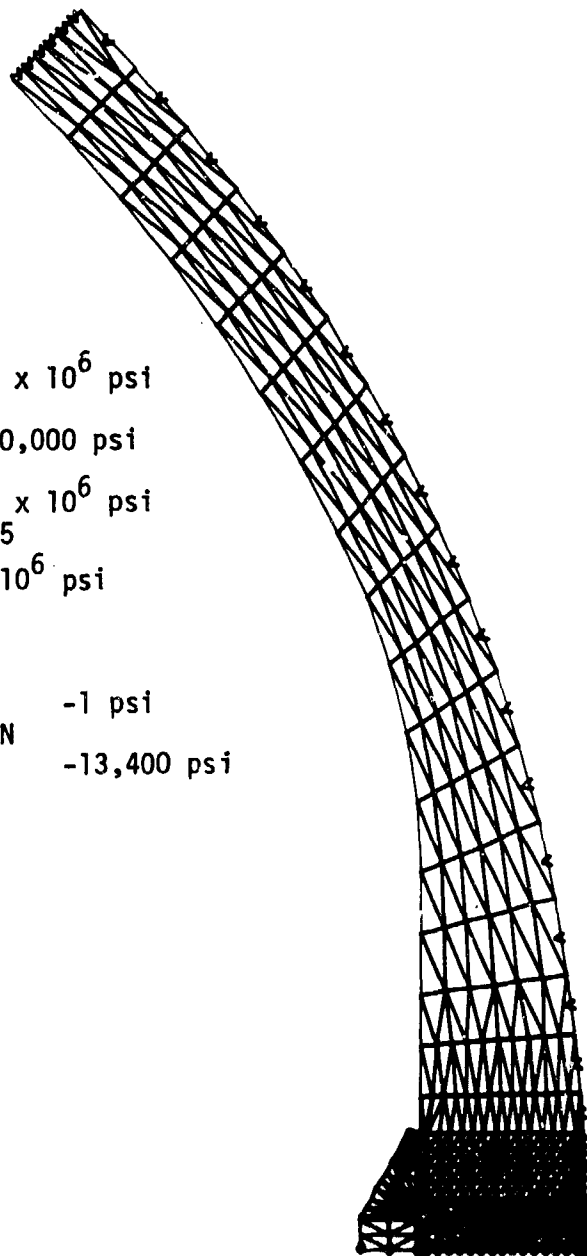
TITANIUM  $E = 17.5 \times 10^6$  psi  
 $\nu = 0.3$   
 $\sigma_{pl} = 140,000$  psi

GLASS  $E = 10.5 \times 10^6$  psi  
 $\nu = 0.225$

INTERFACE  $E = 5 \times 10^6$  psi  
 $\nu = 0.4$

### LOADS:

INCREMENT 1 -1 psi  
FIRST YIELDING IN  
TITANIUM -13,400 psi

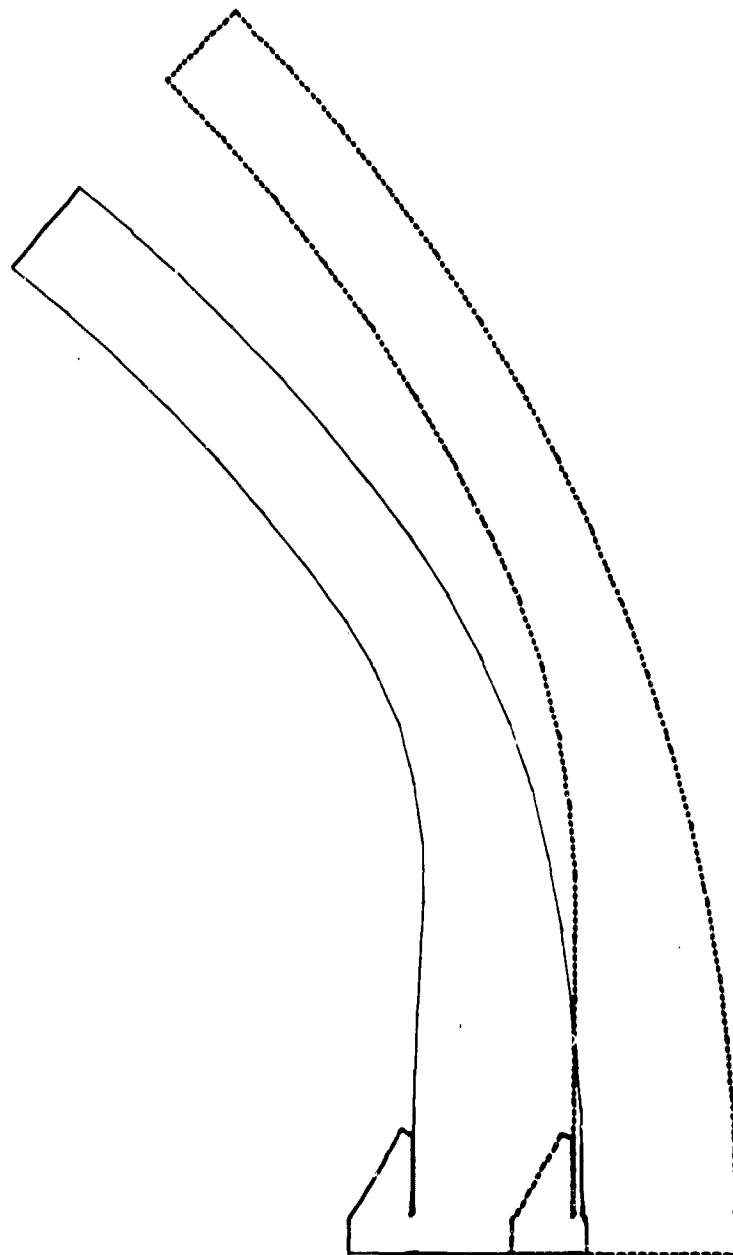


ZP26

### STRUCTURAL IDEALIZATION

Figure 101 - Internally Reinforced Joint Structural Idealization

INTERNALLY REINFORCED GLASS JOINT---0.46W/D



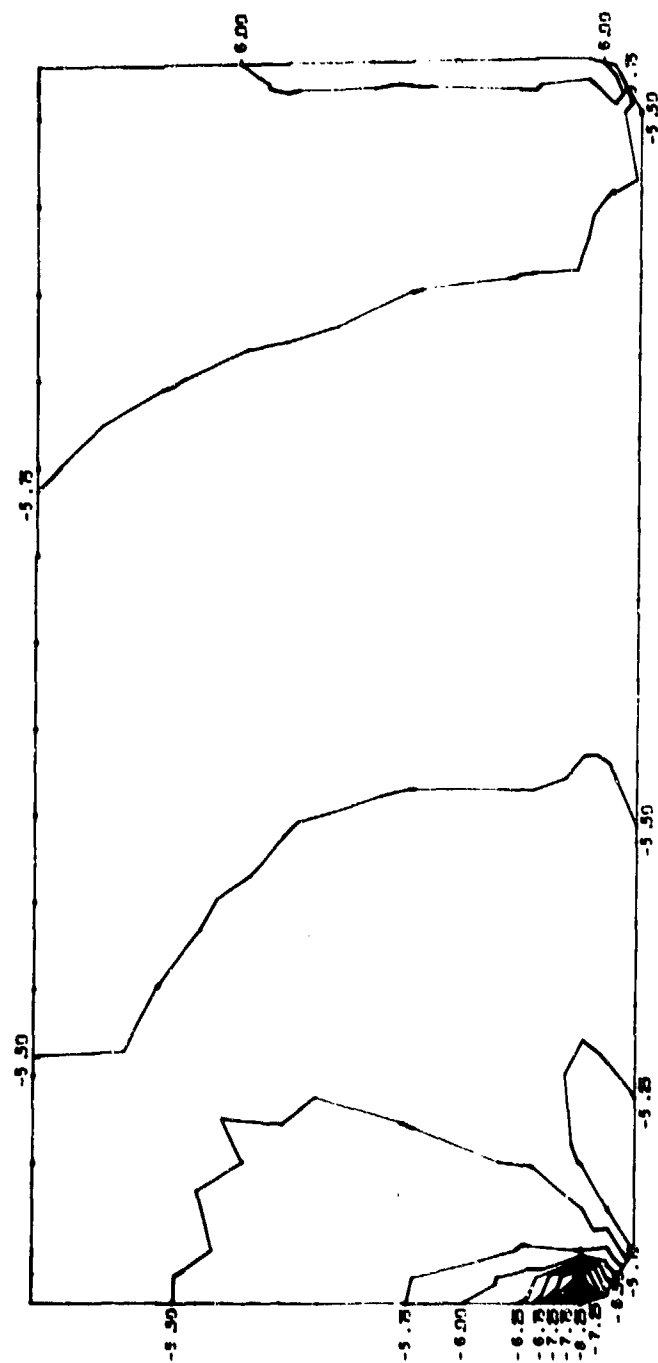
ZP26  
DISPLACED STRUCTURE

INCREMENT NUMBER 1

Figure 10m - Internally Reinforced Joint Displaced Structure

# INTERNALLY REINFORCED GLASS JOINT---0.46W/D

CONTOUR INTERVAL 150.25

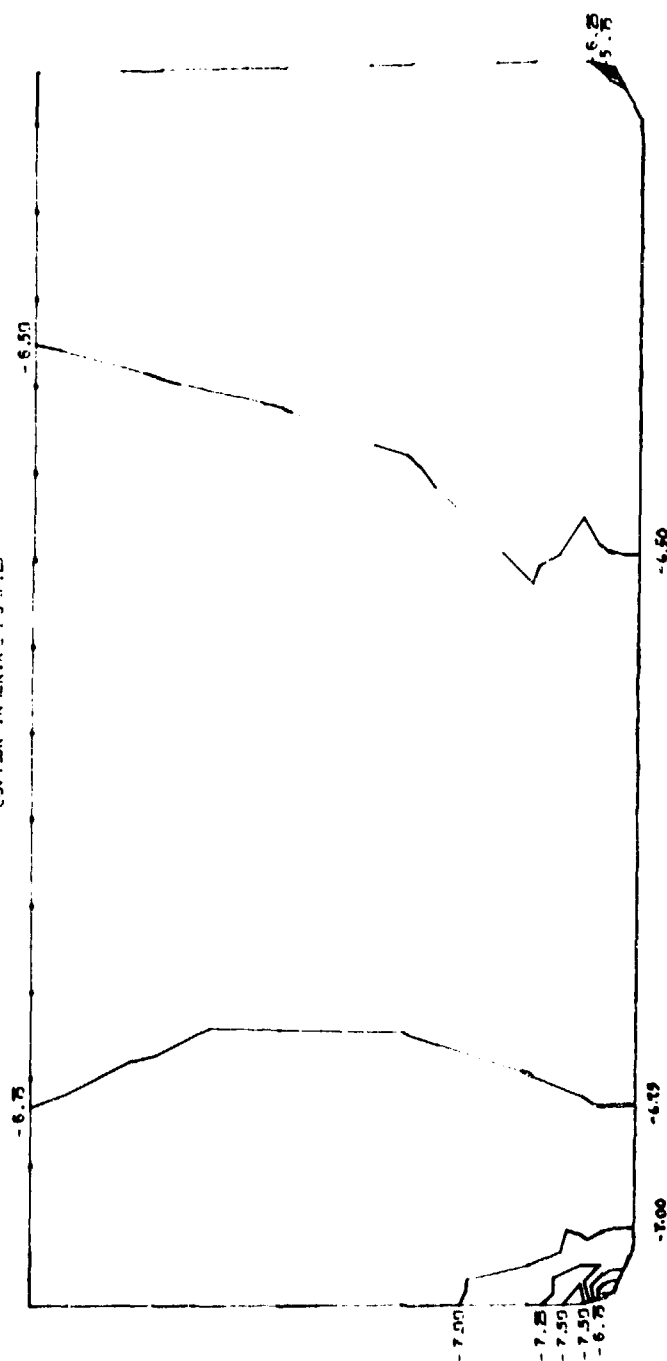


ZP26  
CONTOUR PLOT \* AXIAL STRESS \* INCREMENT NUMBER 1

Figure 10n - Internally Reinforced Joint Axial Stress

# INTERNALLY REINFORCED GLASS JOINT---0.46W/D

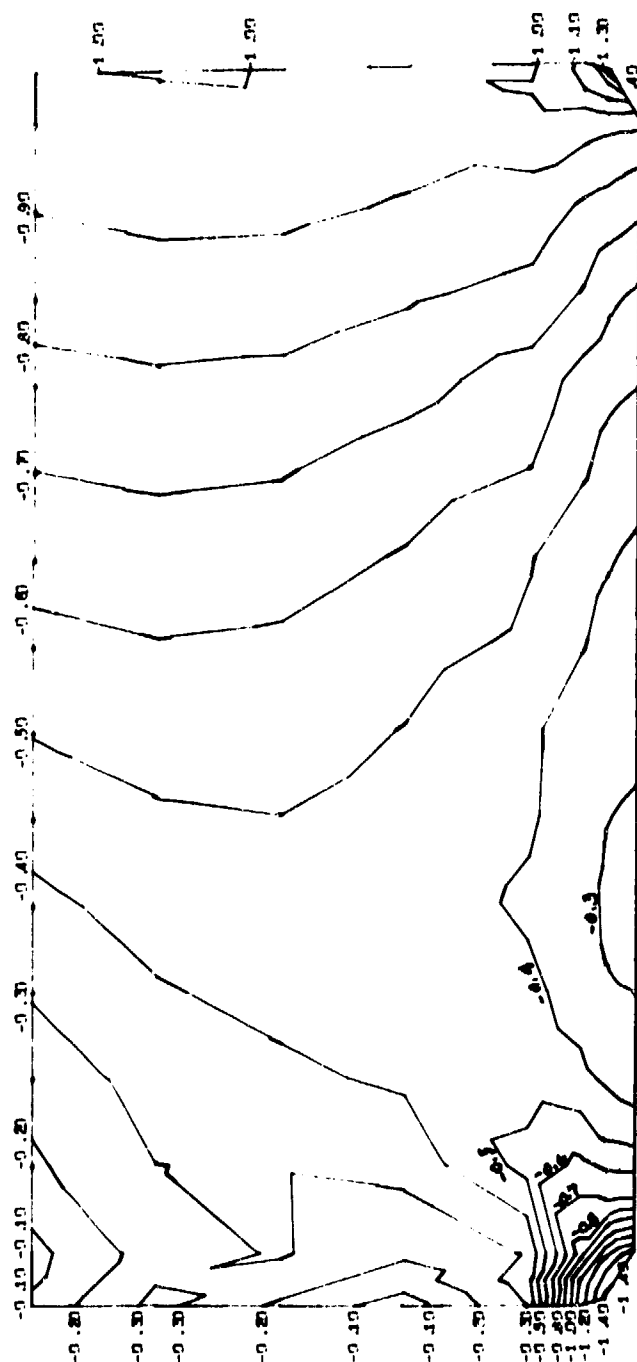
CONTOUR INTERVAL 150.25



## ZP26 CONTOUR PLOT \* CIRCUMFERENTIAL STRESS \* INCREMENT NUMBER 1

Figure 10p - Internally Reinforced Joint Circumferential Stress

CONTINUED ON REVERSE



ZP26  
CONTOUR PLOT

|  | * RADIAL STRESS | * INCREMENT NUMBER 1 |
|--|-----------------|----------------------|
|--|-----------------|----------------------|

**Figure 10q - Internally Reinforced Joint Radial Stress**

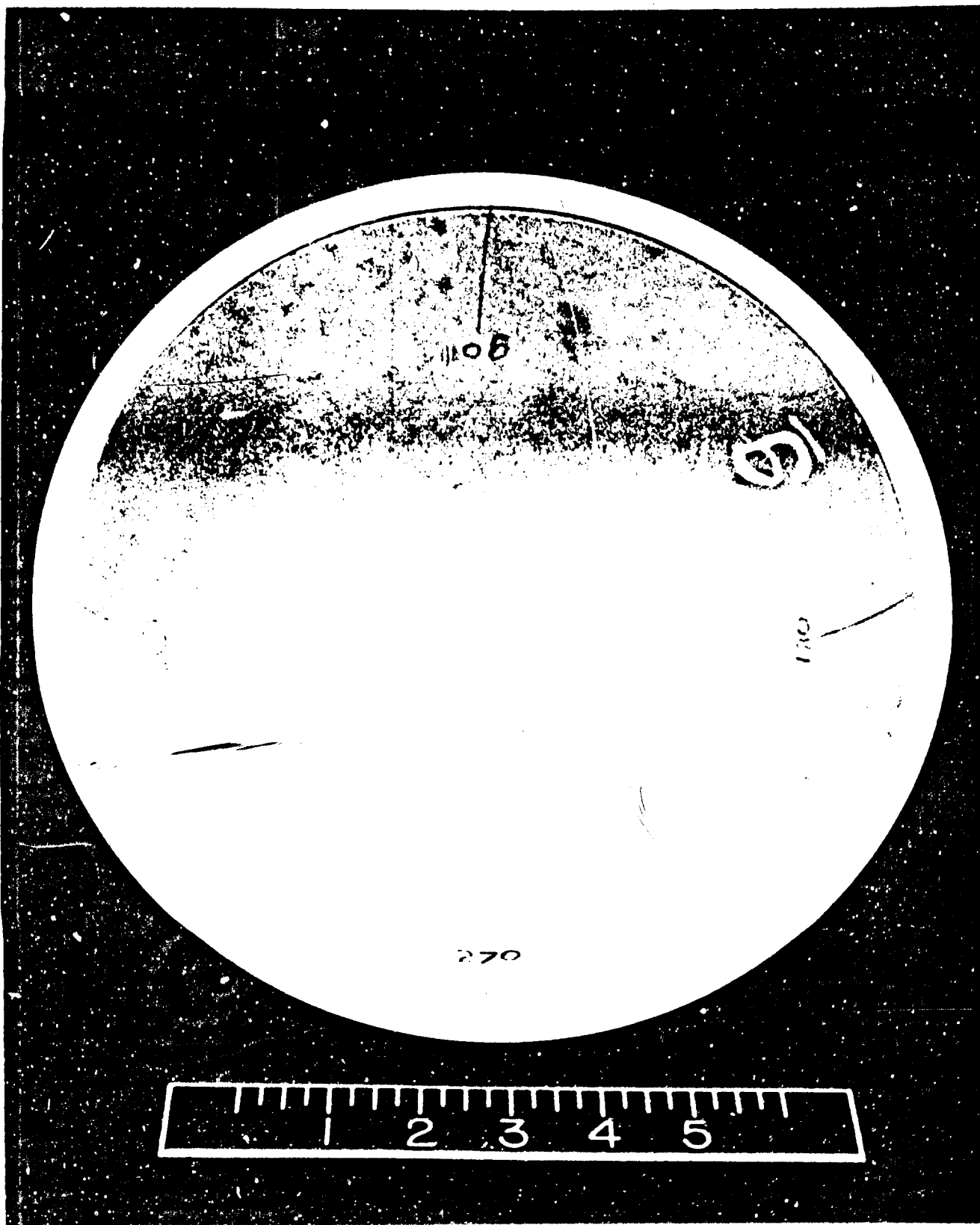
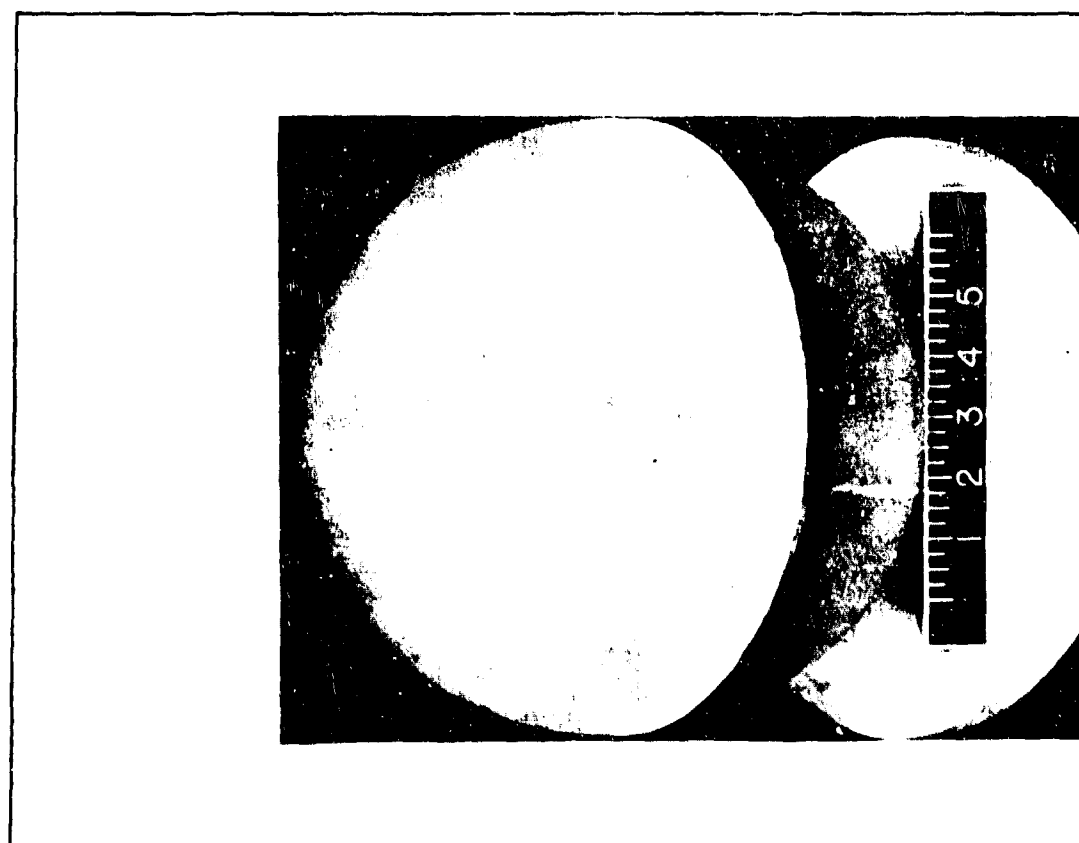


Figure 11 - Glass Hemispherical Shell

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Best Available Copy



PPG 1578



PPG 1080

Figure 12 - Assembled Spheres



Figure 13 - Model in Test Facility

Reproduced from  
best available copy.





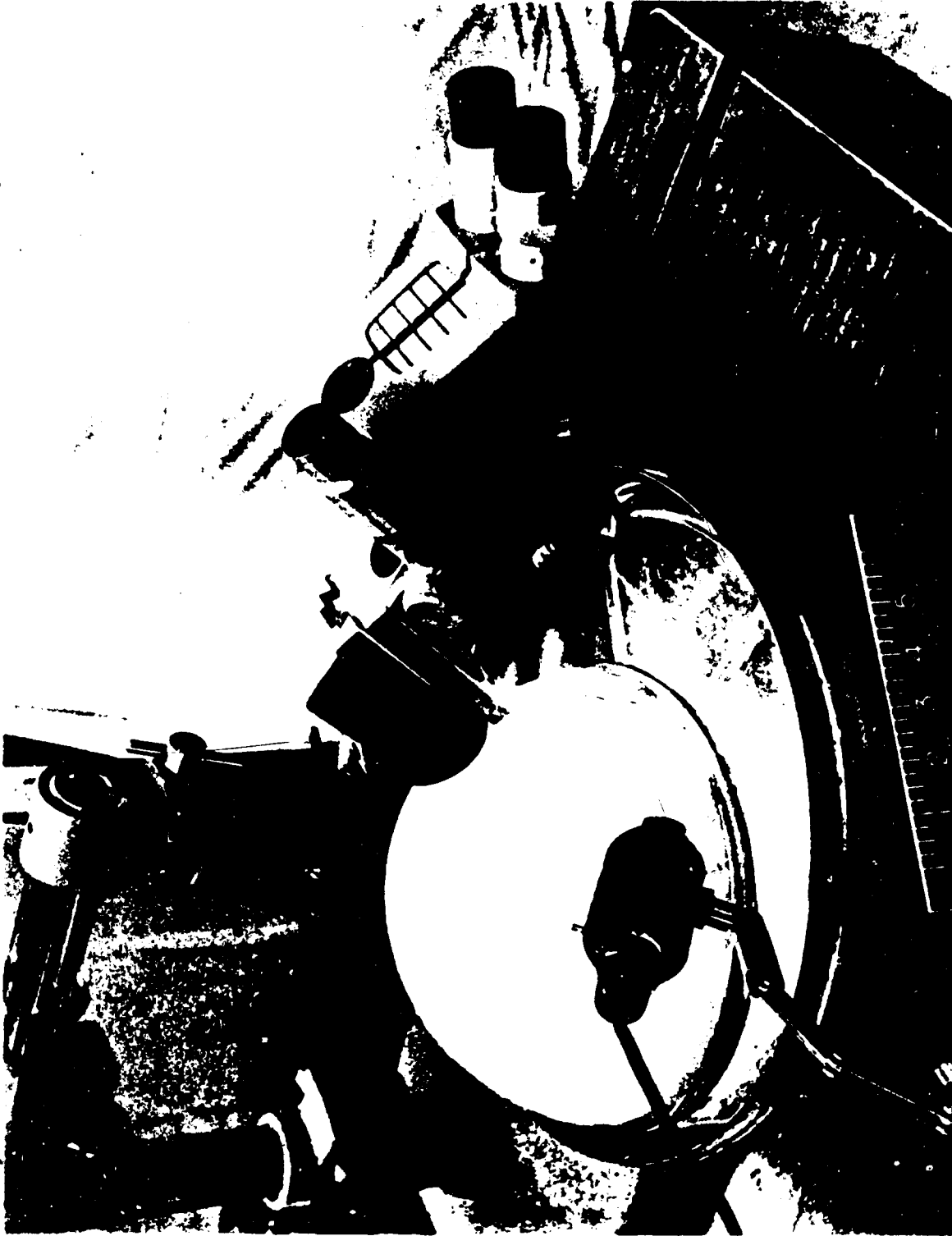


Figure 14 - Inspection Set Up



Figure 15 - Fracture on Hemisphere 15 after 100 Cycles to 6500 psi



Figure 16 - Inside Edge Chip on Hemisphere 13 after 898 Cycles to 5000 psi

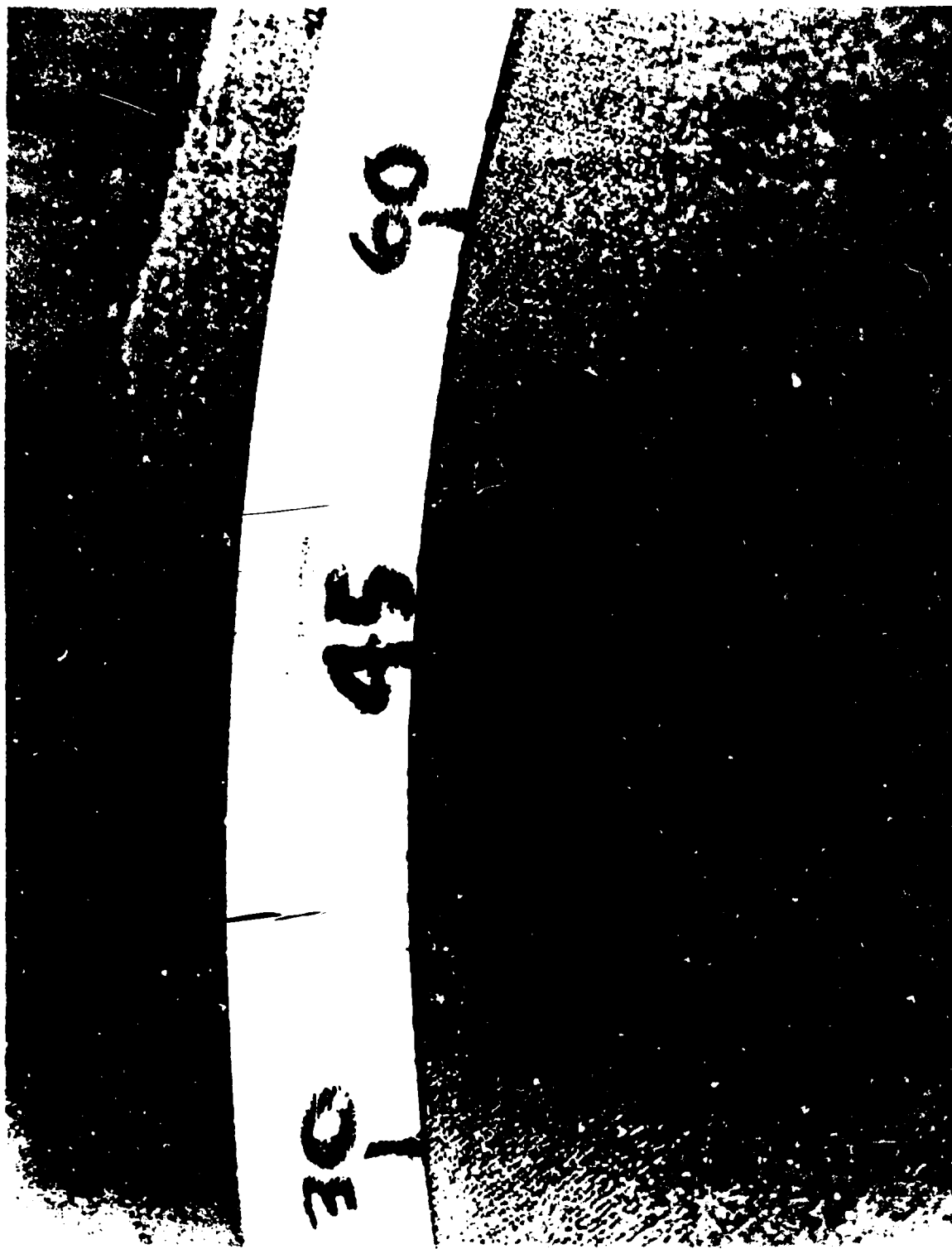


Figure 17 - Outside Edge Spall on Hemisphere 13 after 1048 Cycles to 5000 psi

Figure 18 - Flaw in Hemisphere 3



Figure 18a - Check at Inner Edge of Model Before Making Replica



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Figure 18b - Inner Edge Spall on Replica

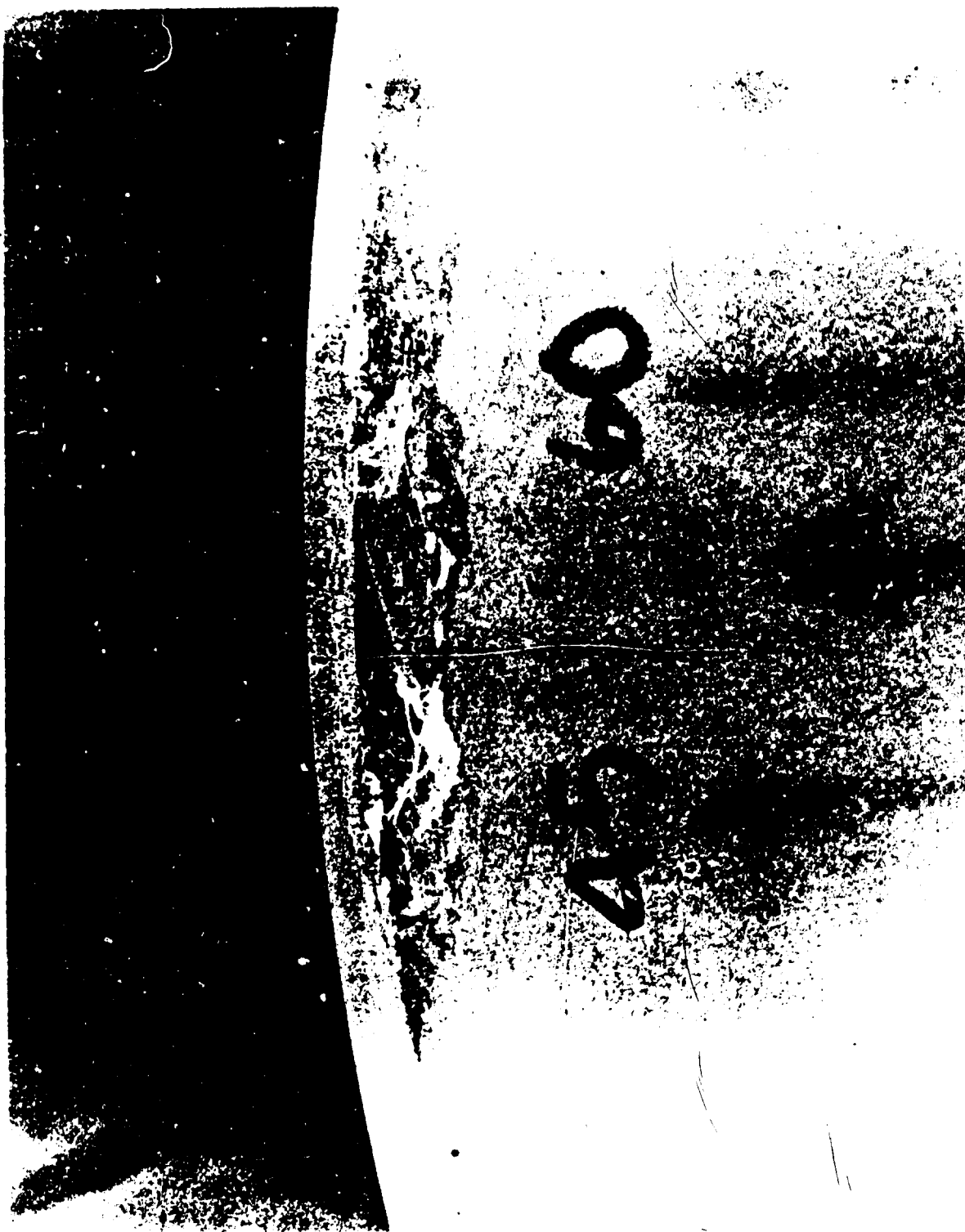


Figure 18c - Model After 5,000 Cycles to 5,000 psi

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Figure 19 - Models after Test



Model 19a - HGS-14





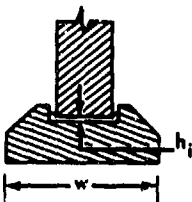
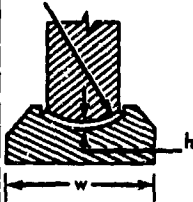
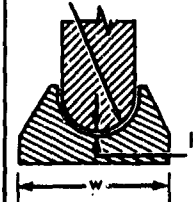
Figure 19b - HGS-17

Reproduced From  
Best Available Copy



Figure 19c - HGS-3

TABLE 1 - SUMMARY OF GEOMETRIC AND MATERIAL PROPERTIES

| TEST<br>CASE<br>NUMBER |    |                          |                          | CONSTANTS*                                               |
|------------------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--------------------------|--------------------------|----------------------------------------------------------|
|                        | G1                                                                                                                                                                                                                                                     | G2                       | G3                       |                                                          |
| 1                      | $\nu_i = 0.1$                                                                                                                                                                                                                                          | $\nu_i = 0.1$            | $\nu_i = 0.1$            | $E_i = 5 \times 10^6$<br>$h_i = 0.010$<br>$w = 0.58$     |
| 2                      | $\nu_i = 0.3$                                                                                                                                                                                                                                          | $\nu_i = 0.3$            | $\nu_i = 0.3$            |                                                          |
| 3                      | $\nu_i = 0.45$                                                                                                                                                                                                                                         | $\nu_i = 0.45$           | $\nu_i = 0.45$           |                                                          |
| 4                      | $E_i = 0.5 \times 10^6$                                                                                                                                                                                                                                | $E_i = 0.5 \times 10^6$  | $E_i = 0.5 \times 10^6$  | $\nu_i = 0.30$<br>$h_i = 0.010$<br>$w = 0.58$            |
| 5                      | $E_i = 5.0 \times 10^6$                                                                                                                                                                                                                                | $E_i = 5.0 \times 10^6$  | $E_i = 5.0 \times 10^6$  |                                                          |
| 6                      | $E_i = 50.0 \times 10^6$                                                                                                                                                                                                                               | $E_i = 50.0 \times 10^6$ | $E_i = 50.0 \times 10^6$ |                                                          |
| 7                      | $h_i = 0.010$                                                                                                                                                                                                                                          | $h_i = 0.010$            | $h_i = 0.010$            | $E_i = 5 \times 10^6$<br>$\nu_i = 0.30$<br>$w = 0.58$    |
| 8                      | $h_i = 0.030$                                                                                                                                                                                                                                          | $h_i = 0.040$            | $h_i = 0.040$            |                                                          |
| 8a                     | $h_i = 0.030$                                                                                                                                                                                                                                          | $h_i = 0.040$            | $h_i = 0.040$            | $E_i = 0.5 \times 10^6$<br>$\nu_i = 0.45$<br>$w = 0.58$  |
| 9                      | $w = 0.40$                                                                                                                                                                                                                                             | $w = 0.40$               | $w = 0.40$               | $E_i = 5 \times 10^6$<br>$h_i = 0.010$<br>$\nu_i = 0.30$ |
| 9a                     | $w = 0.40$                                                                                                                                                                                                                                             | $w = 0.40$               | $w = 0.40$               |                                                          |

STEEL  
RING  
 $E_R = 30 \times 10^6$

\*UNLESS OTHERWISE INDICATED  
RING IS OF TITANIUM WITH  
 $E_R = 15 \times 10^6$  AND  $\nu_R = 0.3$

TABLE 2 - TEST RESULTS OF 0.28 IN. WALL--10-INCH-DIAMETER  
SURFACE COMPRESSED GLASS HEMISPHERES

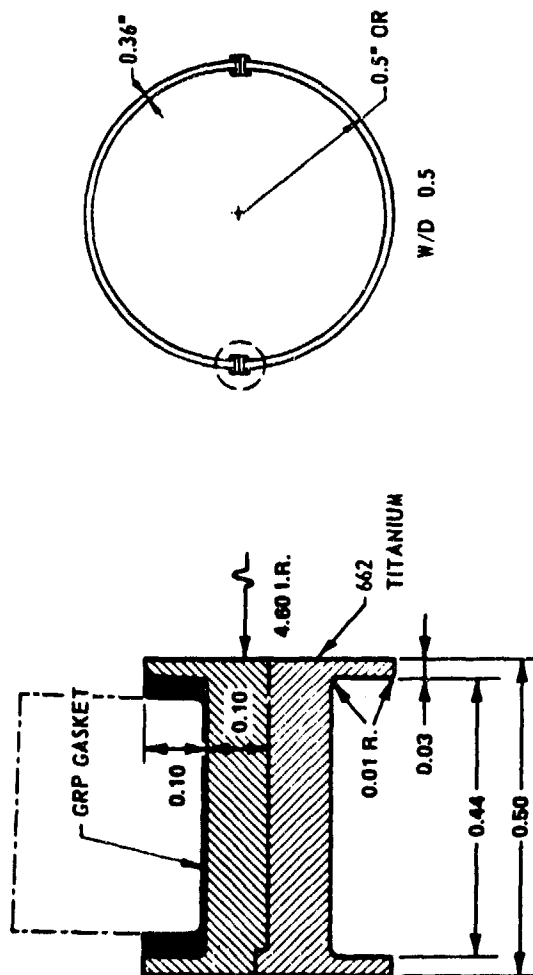
| PPG CODE 1578 GLASS <sup>1</sup> |                                                   |                                           |                                     |                                     |                                     |                                     |
|----------------------------------|---------------------------------------------------|-------------------------------------------|-------------------------------------|-------------------------------------|-------------------------------------|-------------------------------------|
| HEMI<br>NO                       | ASSEMBLY<br>NUMBER AND<br>JOINT TYPE <sup>3</sup> | NUMBER OF CYCLES <sup>2</sup> SURVIVED AT |                                     |                                     |                                     |                                     |
|                                  |                                                   | 2500 psi<br>$\sigma_{AVG} = 23,000$       | 3750 psi<br>$\sigma_{AVG} = 34,500$ | 5000 psi<br>$\sigma_{AVG} = 45,900$ | 6500 psi<br>$\sigma_{AVG} = 59,600$ | 7700 psi<br>$\sigma_{AVG} = 70,600$ |
| 4                                | HGS-10                                            |                                           |                                     |                                     | 3100                                | 380<br>Collapsed                    |
| 7                                | MOD-2                                             |                                           |                                     |                                     | 3100                                | 380<br>Collapsed                    |
| 9                                | HGS-11                                            |                                           |                                     |                                     | 100<br>No Damage                    |                                     |
| 15                               | MOD-2                                             |                                           |                                     |                                     | 100<br>Crack                        |                                     |
| 9                                | HGS-11a                                           |                                           |                                     | 3000                                | 1494<br>Collapsed                   |                                     |
| 2                                | MOD-2                                             |                                           |                                     | 3000                                | 1494<br>Collapsed                   |                                     |
| 13                               | HGS-12                                            |                                           |                                     | 898<br>Inside Edge Chip             |                                     |                                     |
| 14                               | MOD-1                                             |                                           |                                     | 898<br>No Damage                    |                                     |                                     |
| 11                               | HGS-12a                                           |                                           |                                     | 3000                                | 1342<br>Collapsed                   |                                     |
| 14                               | MOD-1                                             |                                           |                                     | 3000                                | 1342<br>Collapsed                   |                                     |
| 18                               | HGS-13                                            |                                           |                                     | 3000                                | 692<br>Crack                        |                                     |
| 19                               | MOD-1                                             |                                           |                                     | 3000                                | 692<br>Crack                        |                                     |
| 1                                | HGS-14                                            | 3000                                      | 3000                                | 3100                                | 2000                                | 30<br>Collapsed                     |
| 12                               | MOD-2                                             | 3000                                      | 3000                                | 3100                                | 2000                                | 30<br>Collapsed                     |
| 16                               | HGS-15                                            | 3000                                      | 3000                                | 3000                                | 1500                                |                                     |
| 17                               | MOD-2                                             | 3000                                      | 3000                                | 3000                                | 1500                                |                                     |
| 3                                | HGS-16                                            | 3000                                      | 3000                                | 3000<br>Crack                       |                                     |                                     |
| 5                                | MOD-1                                             | 3000                                      | 3000                                | 3000<br>No Damage                   |                                     |                                     |
| 6                                | HGS-17                                            | 3000                                      | 3100                                | 3000                                | 2000                                | 30<br>Collapsed                     |
| 8                                | MOD-2                                             | 3000                                      | 3100                                | 3000                                | 2000                                | 30<br>Collapsed                     |
| CORNING CHEMCOR 0313 GLASS       |                                                   |                                           |                                     |                                     |                                     |                                     |
| 6                                | CH-1                                              |                                           |                                     | 218<br>No Damage                    |                                     |                                     |
| 24                               | MOD-1                                             |                                           |                                     | 218<br>Collapsed                    |                                     |                                     |

1. Chemically strengthened in sodium salt bath. Surfaces of glass have residual compression stress of approximately 60,000 psi for 1578 models and 35,000 psi for 0313 models.

2. All tests were conducted in fresh water at a rate of approximately 1 cycle per minute.

3. See Figure 4 for joint geometry.

TABLE 3 - TEST RESULTS OF 10-INCH-DIAMETER 0.36 WALL PPG 1080 K<sup>+</sup>  
SURFACE COMPRESSED GLASS HEMISPHERES



| Model No. | Hemi No. | Number of Cycles Survived at             |                                          |                                          |                                          |                                          |                                          |                                          |
|-----------|----------|------------------------------------------|------------------------------------------|------------------------------------------|------------------------------------------|------------------------------------------|------------------------------------------|------------------------------------------|
|           |          | 14,600 Ft<br>$\sigma_{Avg}$ = 46,900 psi | 17,500 Ft<br>$\sigma_{Avg}$ = 55,400 psi | 20,000 Ft<br>$\sigma_{Avg}$ = 64,200 psi | 22,500 Ft<br>$\sigma_{Avg}$ = 72,100 psi | 25,000 Ft<br>$\sigma_{Avg}$ = 74,900 psi | 27,500 Ft<br>$\sigma_{Avg}$ = 87,700 psi | 30,000 Ft<br>$\sigma_{Avg}$ = 96,500 psi |
| HGS 4     | 52*      | 2000                                     | 3000                                     | 3000                                     | 3000                                     | 1000                                     | 500                                      | 1                                        |
|           | 99       | 2000                                     | 3000                                     | 3000                                     | 3000                                     | 1000                                     | 500                                      | 1                                        |
| HGS 5     | 28       | 2000                                     | 3000                                     | 3000                                     | 3000                                     | 3000                                     | 2000                                     | 4<br>Collapsed<br>4                      |
|           | 33       | 2000                                     | 3000                                     | 3000                                     | 3000                                     | 3000                                     | 2000                                     |                                          |
| HGS 6     | 64       | 2000                                     | 3000                                     | 3000                                     | 3000                                     | 1000                                     | 500                                      | 1                                        |
|           | 104      | 2000                                     | 3000                                     | 3000                                     | 3000                                     | 1000                                     | 500                                      | 1                                        |
| HGS 7     | 52*      | 2000                                     | 3000                                     | 3000                                     | 3700                                     | 1000                                     | 500                                      | 1                                        |
|           | 55       | 2000                                     | 3000                                     | 3000                                     | 3700                                     | 1000                                     | 500                                      | 1                                        |
| HGS 8**   | 1        | 2000                                     | 3000                                     | 3000                                     |                                          |                                          |                                          | 1                                        |
|           | 3        | 2000                                     | 3000                                     | 3000                                     |                                          |                                          |                                          | 1                                        |

\* Used twice.

\*\* Hemispheres were ground and polished over entire surface. Thickness was about 0.02 in. less than unpolished models.

\* Used twice.

\*\* Hemispheres were ground and polished over entire surface. Thickness was about 0.02 in. less than unpolished models.

TABLE 4 - TEST RESULTS OF 10-INCH-DIAMETER VARIABLE WALL PPG 1578  
SURFACE COMPRESSED GLASS HEMISPHERES

| Assembly | Hemi No. | Number of Cycles Survived at        |                                     |                                     |                                       |                                       |                                       |                                       |
|----------|----------|-------------------------------------|-------------------------------------|-------------------------------------|---------------------------------------|---------------------------------------|---------------------------------------|---------------------------------------|
|          |          | 6500 psi<br>$\sigma_{Avg} = 38,000$ | 7700 psi<br>$\sigma_{Avg} = 43,000$ | 8900 psi<br>$\sigma_{Avg} = 50,000$ | 10,000 psi<br>$\sigma_{Avg} = 56,000$ | 11,100 psi<br>$\sigma_{Avg} = 62,000$ | 12,200 psi<br>$\sigma_{Avg} = 68,000$ | 13,400 psi<br>$\sigma_{Avg} = 75,000$ |
| HGS-20   | 7        | 2000                                | 3000                                | 3000                                | 3000                                  | 2000                                  | 1000                                  | 1000                                  |
|          | 9        | 2000                                | 3000                                | 3000                                | 3000                                  | 2000                                  | 1000                                  | 1000                                  |
| HGS-21   | 1        | 2000                                |                                     | 300<br>Collapsed                    |                                       |                                       |                                       |                                       |
|          | 3        | 3000                                |                                     | 300<br>Collapsed                    |                                       |                                       |                                       |                                       |
| HGS-22   | 2        | 1532<br>Collapsed                   |                                     |                                     |                                       |                                       |                                       |                                       |
|          | 4        | 1532<br>Collapsed                   |                                     |                                     |                                       |                                       |                                       |                                       |

## APPENDIX

### BACKGROUND ON GLASS AND CERAMIC SPHERICAL SHELLS

Numerous tests had been conducted prior to initiation of the DOT massive glass effort. A number of these studies will be discussed with emphasis on those conducted at the Center.

#### SPHERICAL SHELLS FOR BUOYANCY SPHERES

Although the pressure hull of a deep submergence vehicle may be positively buoyant, the complete vehicle is usually not because of instruments, machinery and outer structure weight. The approach taken to provide positive buoyancy is to surround the structure with syntactic foam, a composite of glass microballoons in a plastic matrix. Until recently the best foam available for 20,000 feet had a density on the order of 42 pounds per cubic feet. As a possible alternative, glass and alumina spherical shells were investigated at the Center in the Search Vehicle program of DSSP. At the time these studies were to be undertaken two of the more promising production techniques for buoyancy spheres were Corning Glass Work's fusion sealing of annealed Pyrex glass hemispheres and Coors Procelain Company's casting method for monolithic alumina spheres.

The glass spherical shells investigated were 10 inch diameter by 0.28 wall Corning Code 7740 annealed Pyrex glass. This glass has a Young's modulus of approximately  $9.1 \times 10^6$  psi, Poisson's ratio of 0.2, and a density of 139 lb/ft.<sup>3</sup> The W/D ratio of the glass spheres were 0.36. The spheres are formed by butting together two hemispherical shells, heating the area of the glass joint, and passing an electric arc across the butt joint to make a fusion weld. Through the period between 1964 and 1968, nearly 100 model tests were conducted to observe static and cyclic performance of fusion welded spheres. Kiernan<sup>1</sup> conducted collapse tests of 18 models. The results are shown in Figure 20. Subsequently tests<sup>15</sup> were

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<sup>15</sup>Nishida, K., "Static and Cyclic Fatigue Tests of Fusion Sealed Pyrex Glass Spheres," David Taylor Model Basin Report 2246 (Sep 1966).

conducted to study effects of loading rate, pressure medium, and sealing technique on short term static strength. These results are shown in Tables 5 and 6 and also in Figure 20. In addition to static tests, 10 models were tested under cyclic conditions. The results are shown in Table 7. The interesting points of the data are:

1. There was no apparent effect of loading rate on collapse strength when tests were conducted in simulated sea water at three rates of compressive stress. Nine spheres were each tested at rates of 140,000, 3500, and 200 psi/min. The average collapse strengths were 31,700, 31,600, and 32,500 feet.

2. No appreciable difference in collapse strength was obtained when simulated sea water and oil were used as pressure medium. The average collapse strength for 9 models in sea water was 31,600 feet and for 9 models in oil was 34,000 feet.

3. The static strength of fusion sealed annealed glass spheres is dependent on sealing technique. Three sets of glass spheres gave average collapse depths of 32,000 feet, 38,000 feet, and 47,000 feet. The early models tested were characterized by large internal beads at the fusion sealed seam. This was subsequently improved with some modification in the manufacturing procedure. Figure 21 shows the difference in the weld seams before and after the change.

4. The 10 spheres tested cyclically survived 5000 cycles 22,500 feet. One sphere may have suffered fatigue damage after 3000 cycles at the fusion welded seam. Each sphere had been proof tested to 30,000 feet prior to cycling. Five spheres including the damaged one were collapsed after cycling. In each case the collapse pressure was considerably higher than the initial proof pressure.

In addition to the data of 0.28 wall models, 6 collapse tests were conducted on 10-in.-diameter 0.36 wall fusion sealed spheres. The results are summarized in Table 8. The empirical elastic buckling pressure for this geometry is about 40,000 psi. The 6 models failed at pressures significantly below this and thus, it is concluded that all failed by stress induced conditions. All of these models were sealed with the early technique. No data was generated with the modified sealing process.



Two 44 inch diameter fusion sealed annealed Pyrex glass spheres were tested<sup>16</sup> as a part of the evaluation of fusion sealed seams. These two tests were preceded by a series of static tests on 10 inch diameter versions. Nominal model dimensions for the 10 and 44 inch models are shown in Figure 22. A summary of the results of the five 10 inch models is shown in Table 9. Note that the experimental collapse pressures were within 10 percent of the calculated values based on near perfect geometry. The excellent results obtained in these tests are attributed to the quality of the fusion sealed seam. The thinner shell wall (0.23 against 0.28 for unpenetrated uniform wall models) and the fact that air pressure was applied inside the model through the penetration made it possible to obtain a better fusion sealed seam. Physically this resulted in a zone much more uniform than those observed for the 0.28 wall spheres.

The fusion sealed seams of the 10 inch models were not representative of the 44 inch models. The two 44 inch models had sharp notches at the inner surface of the fusion sealed seam. In the case of Model 44-1 this caused a reduction in wall thickness of nearly 50 percent at the base of the notch.

The two 44 in. glass spheres were hydrostatically tested in the Center's 4 ft 15,000 psi high pressure test facility. A photograph of a model being lowered in the test facility is shown in Figure 23. The tests were conducted in fresh water. In the case of Model 44-1 a hydrostatic pressure of 3500 psi was applied at which point sharp cracking sounds were audible from distances fairly remote to the test facility. The strain gages in the area of the fusion sealed seam also indicated a sharp change in strain. Typical examples of this behavior are shown in Figure 24. The test was terminated at this point and pressure was slowly reduced. Inspection of the model after test revealed heavy spalling in the inner and outer surfaces of the fusion sealed seam. Typical photographs of the damaged areas are shown in Figure 25. Strain sensitivities, defined as the slopes of the pressure strain diagram are shown in Figure 26. The maximum stress calculated from strain gage data was 70,000 psi.

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<sup>16</sup>Nishida, K., "Structural Studies of Massive Glass: Sep 1968-May 1969," NSRDC Report 3180 (Aug 1969).

Model 44-2 exhibited similar behavior. However, sharp cracking sounds were not audible in this case. The test was terminated when a sharp change in strain was detected at a pressure of 4500 psi. The spalling on 44-2 was mainly on the inner surface.

The results obtained on the two 44 inch models are similar to that obtained by the Woods Hole Oceanographic Institute in a test of a 44 inch model for Bell Telephone Laboratories. These tests suggest that a considerable effort is required before large fusion sealed glass spherical shells can be considered practical for deep submergence buoyancy spheres.

Alumina spherical shells were also tested extensively for possible application as buoyancy spheres. Most of the tested were 10 inch diameter 0.18 in. wall of AD 99C and fabricated by Coors Porcelain Company. AD 99C has a Young's modulus of  $52 \times 10^6$  psi, a Poisson's ratio of 0.22, and a density of 238 lb/ft.<sup>3</sup> The spheres tested had a W/D ratio of 40 percent. The spherical shells are formed while in the "green" state by a casting technique. The shells are then fired for curing. The tests carried out on alumina spheres were similar to those conducted on Pyrex glass. The results are discussed in detail in Reference 17, and are also tabulated in Table 10. The interesting points of the tests were.

1. The static strength of alumina spherical shells was quite encouraging. Stress levels in excess of 500,000 psi were achieved in many of the tests.

2. Loading rate does not appear to have a very significant effect on compressive strength based on tests conducted at rates between 350 and 400,000 psi/min. The average compressive stress of the 8 models tested at 350 psi/min was 460,000 psi, 3 models at 9000 psi/min was 510,000 psi, and 8 models at 400,000 psi/min was 500,000 psi.

3. Two 40 percent W/D alumina spheres survived proof tests of 30,000 ft and 5000 cycles of pressure to 22,500 feet. The two models were then collapsed at depths equal to about 60,500 feet. Thus, it appears that cycling did not affect the collapse strength of the models.

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<sup>17</sup>Reardon, E.F., "Exploratory Tests of Aluminum Spheres Under External Pressure," NSRDC Report 3013 (Apr 1969).

Attempts to manufacture larger alumina spheres by the casting method was not very successful as the shell had a tendency to sag of its own weight while the material was in the "green" state. This created undesirable flatspots at the apex. A fusing technique to form larger spheres was also attempted. However, poor tests were obtained on 10 inch models of this type primarily because of a notch effect at the inner surface of the joint. This defect was very similar to those observed on the 44 inch diameter fusion sealed Pyrex glass spheres. Electron beam and laser welding were also explored on 3 inch diameter by 0.1 wall hemispheres.<sup>18</sup> This work indicated additional effort was required to eliminate thermal stress cracking and incomplete penetration welds. The data indicate that further development is required before large alumina spheres can be considered practical for deep submergence buoyancy spheres.

#### MECHANICAL COMPRESSION JOINTS

A pressure vessel designed to house instruments or man will require at least one mechanical joint. This problem has been under study for a number of years and has proven to be one of the more difficult ones encountered. Very exploratory work conducted by Krenzke and Charles<sup>19</sup> on the static strength of 2 inch diameter annealed Pyrex glass hemispheres were quite encouraging. The collapse strength of the hemispheres could be predicted by elastic theory up to stresses as high as 300,000 psi. Kiernan<sup>1</sup> subsequently conducted experiments on larger 18 inch diameter hemispheres of annealed and surface strengthened glass and alumina. Various types of gaskets were also explored. A summary of the interesting points are:

1. Generally, chemically strengthened glass (Herculite II) performed better than thermally tempered and annealed glasses as expected.
2. In the limited number of tests conducted, gasket material with various combinations of teflon, lead, alumina and titanium foil gave no better results than glass-to-glass tests.

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<sup>18</sup>Benecke, M.W., "Electron Beam and Laser Welding of Aluminum Oxide Hemispheres," Prepared by Boeing Company for U.S. Navy under Contract N00660-69-C-0370 (May 1967).

<sup>19</sup>Krenzke, M.A. and R.M. Charles, "The Elastic Buckling Strength of Spherical Glass Shells," David Taylor Model Basin Report 1759 (Sep 1963).

3. Of the nearly 50 collapse tests conducted, less than 10 percent could be associated with elastic shell buckling. All other failures were attributed to stress conditions at the joint.
4. Collapse tests of 8 alumina spherical shells with W/D ratios of about 25 percent indicated that the joint problem in alumina ceramic may not be as severe as in glass. Four of the spheres were cast monolithically and four were formed by butting together a pair of hemispheres. No reduction in strength could be attributed to the presence of the joint.

Additional static and cyclic tests of Herculite II glass hemispherical shells not reported in Reference 20 have been conducted. The results are shown in Table 11. Five collapse tests of models butted together glass-to-glass were performed. The bearing stresses at collapse ranged from 127,000 to 219,000 psi. Fatigue tests were attempted on models also assembled glass-to-glass. None of the 3 models cycled survived more than 30 cycles of pressure which ranged from 10,000 to 13,333 psi. Similar results have been reported by Perry of NOL for this glass.

In view of the scatter of the data and the limited number of tests conducted under identical conditions an extensive effort to study the joint problem under more rigidly controlled conditions was attempted. All of the hemispherical shells tested were 10 inch diameter 0.28 inch wall of annealed Pyrex glass. Two sets of tests were conducted. One to observe the effects of surface flatness and the other the effect of "soft" gasket materials. The results of these tests are summarized in Tables 12 and 13. It is interesting to note the following trends indicated by the tests.

1. As might be expected, surface flatness appears to have an effect on collapse strength. The average collapse strength of 16 spherical assemblies formed by butting together two hemispherical shells which were finished at the bearing edge with 1200 mesh diamond dust abrasive was nearly 30 percent higher than the average collapse strength of 17 spherical assemblies

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<sup>20</sup> National Materials Advisory Board, "Massive Glass as a Naval Structural Material," NMAB-262, April 1970.

whose hemispheres were finished at the bearing edge with 150 grit diamond embedded carbon wheel. Interestingly, the lowest collapse strength of the finely finished models (11,125 psi) was higher than the highest collapse strength of the roughly finished models (10,650 psi).

2. The data indicates that "soft" gasket materials can have a beneficial effect on short term static collapse strength. However, in a number of individual cases of gasket tests the models did no better than glass-to-glass tests. The average of 6 models with gaskets of glass fiber cloth impregnated with epoxy were 20 percent higher than glass-to-glass models of the same surface finish. The average collapse strength of 6 models with glass fiber cloth impregnated with synthetic sulfide rubber was nearly 50 percent better than glass-to-glass models of the same surface finish.

The better performance of gasketed models is attributed to the more even distribution of stress it creates. The compliant gasket material has a tendency to reduce the significance of contact stresses which are most likely the cause of premature failures in glass-to-glass models. None of the glass-to-glass models failed at a pressure that could be associated with the elastic buckling strength, which for this geometry is approximately 20,000 psi. In a number of cases of models with gaskets, the short term collapse strength could be associated with elastic buckling. It is also of interest to note that the collapse pressures of 3 models with glass reinforced rubber were actually not catastrophic. These tests were terminated when a slight drop in the pressure gage was noted. Inspection of these models indicated that the edges of the bearing surface had spalled off on both the inner and outer wall. Figure 3 is a photograph of a model terminated at a pressure of 17,000 psi.

Fatigue tests have been conducted on annealed Pyrex glass hemispherical shells utilizing glass reinforced plastic gaskets. Although the static tests suggested that rubber was probably the better matrix material for short term static strength, inspection of these gaskets after a single application of pressure indicated that extrusion and deterioration were serious problems. Thus, two types of epoxy were used for the matrix:

(1) Hysol, a quick setting epoxy, and (2) high strength resin EPON 828. The cyclic tests of glass reinforced plastic (Hysol) have been disappointing. None of the three spherical assemblies survived more than 6 cycles of pressure to maximum depth of 22,500 ft.

The results of models with glass reinforced plastic (EPON 828) also were disappointing. The test results are summarized in Table 14. The five models designated C1 through C5 were cycled to depths of 11,250, 13,500, 18,000, and 22,500, respectively. A proof test of 30,000 feet was applied to Model 65 only. Inspection of Models C1 through C4 after 50 cycles of pressure indicated slight spalling at the inner edge of the bearing surface. Glass chips about  $1/4$  by  $1/32$  in. were observed. When Model C3 (15,750 ft cyclic depth) was reinserted in the test facility, it failed after a total of 197 cycles. Model C4 (18,000 ft cyclic depth) failed after a total of 150 cycles and C5 after 706 cycles. Models C1 and C2 survived 1000 cycles and were reinspected; further cyclic damage was observed in both cases. Model C1 exhibited spalling on the inner surface of the bearing edge. The spalled area was approximately  $1\ 1/2$  by  $3/8$  in. Model C2 spalled at the outer surface at the bearing edge. A photograph of this damage is shown in Figure 27. The models were reinserted in the tank for further cycling. Model C2 failed after a total of 2015 cycles. Model C1 survived 3000 cycles although further cyclic damage was quite obvious. Relatively large spalled areas were observed on the inner surface as well as the outer surface at the joint. A photograph of the damage after 3000 cycles is shown in Figure 27. No further testing was attempted on the model.

In addition to tests of annealed Pyrex glass, compression studies were conducted on PPG Industries' 1080 glass. The models are 10 in. diameter by 0.36 in. All models were tested in the annealed condition. Most had bearing surfaces prepared with No. 120 grit wheel. These models were tested in simulated sea water at various loading rates and held at constant pressure in some cases. A summary of the test results is presented in Table 15. All models, except two hemispheres tested on hardened steel surface, were formed by butting two hemispheres together glass-to-glass. It can be observed that the range of stresses obtained on these tests were 99,000 to 158,000 psi, excluding tests of glass hemispheres on

hardened steel. It is interesting to note that the two lowest test results were those conducted with steel as the bearing surface. It should be recognized that different loading rates, limited cycling, and sustained loading were involved for the glass-to-glass tests. This should be considered when comparing individual tests within the group. For example, it can be observed that most of the lower stresses at collapse were obtained on models that were cycled and held at pressure for a period of time. This is to be expected.

One static test of a 5 inch diameter by 0.11 inch wall glass ceramic hemispherical shell was conducted at the Center. The material was Corning's Pyroceram 9606 which has a Young's modulus of  $17.3 \times 10^6$  psi, Poisson's ratio of 0.245, and a density of 163 lb/ft.<sup>3</sup> The weight-to-displacement ratio for the hemisphere was 32 percent. A sketch of the model is shown in Figure 28. The hemisphere was tested by placing it on a hardened steel block in the NSRDC 30,000 psi 12 in. spherical pressure chamber. Simulated sea water was used as the pressure medium and an external pressure loading rate of 400 psi/min was used. The model was pressurized to the rated operating capacity of the chamber, 30,000 psi, at which point the loading was terminated. Upon releasing pressure, the model failed catastrophically at a pressure of 15,000 psi. At the maximum static pressure of 30,000 psi the membrane stress in the shell was 352,000 psi. The calculated elastic buckling strength of the hemisphere based on the empirical formula was 27,000 psi. Thus, the model exceeded the calculated empirical pressure by nearly 10 percent. The failure of the model upon releasing the pressure is probably associated with local yielding at the bearing surface of the hardened steel block. Permanent set takes place on the load application phase which inhibits the Pyroceram shell to relax to its original shape upon unloading.

Tests of glass ceramic structures have also been conducted by the Lockheed Missiles and Spacecraft Company (LSMC) and the General Electric Company (GE). The LSMC model was a bi-spherical structure with the juncture portion of titanium and the end closures of Pyroceram. The GE model was a geodesic structure with the lattice of titanium and the inserts of Pyroceram. A summary of the tests is presented in Reference 20.

A slightly different approach to solving the joint problem was investigated utilizing chemically strengthened Chemcor 0312 glass. The area of the bearing joint is reinforced so that the thickness at the bearing face is nearly twice the thickness of the uniform portion of the wall. The increased thickness at the bearing face reduces the bearing stresses and thus could reduce the contact problem. Several models have been statically tested to observe response. Two different loading rates were utilized to determine the effect of strength. These models were handlapped prior to testing. Measurements taken before and after lapping indicated that approximately 0.002 to 0.003 in. of the glass surface was removed as a result of lapping. In addition to static tests, a few cyclic tests have been conducted. All tests of chemically strengthened glass hemispheres have been conducted in simulated sea water.

The results of static tests of chemically strengthened glass hemispheres are presented in Table 16. The models were formed by butting two hemispheres together glass-to-glass. It is somewhat surprising to see that the average stress at collapse for the models tested at a slow loading rate (20 psi/min) was higher than the average for the fast rate tests (15,000 psi/min). Apparently an undesirable effect, possibly from friction, is created at the bearing surfaces of the model during a fast rate test.

The elastic buckling pressure for the uniform wall (0.23) portion of the shell is in the order of 14,000 psi. Although the collapse pressures could be associated with elastic buckling in some cases, the majority of models more likely failed by stress controlled conditions.

All static tests of Chemcor glass models were prior to tests conducted on annealed glass models with gaskets described previously. Since improvement in short term static strength was apparent in tests of annealed glasses, several cyclic tests of Chemcor 0312 glass hemispheres with reinforced bearing surfaces and glass reinforced plastic gaskets were conducted. A summary of these tests is included in Table 17. The results have been encouraging considering the rather severe conditions of the tests. A maximum cyclic pressure of 10,000 psi and a cyclic rate of approximately one cycle per minute were utilized in these tests. Thus, the loading rate was greater than that utilized for static tests of



glass-to-glass models tested at the fast loading rate. Five of the seven models cycled survived at least 3000 cycles to 10,000 psi. However, two failed after application of only 86 and 110 cycles. Based on present knowledge, it is concluded that some strength degradation resulted from the lapping. Although only 2-3 mils of glass was removed, the depth of surface compression for Chemcor 0312 glass is only about 5 mils. Thus, much of the residual surface compression was lost by the lapping operation and most likely influenced the test results. In view of this shortcoming in the specimen, the fact that 5 of 7 models survived 3000 cycles to 22,500 ft is quite encouraging.

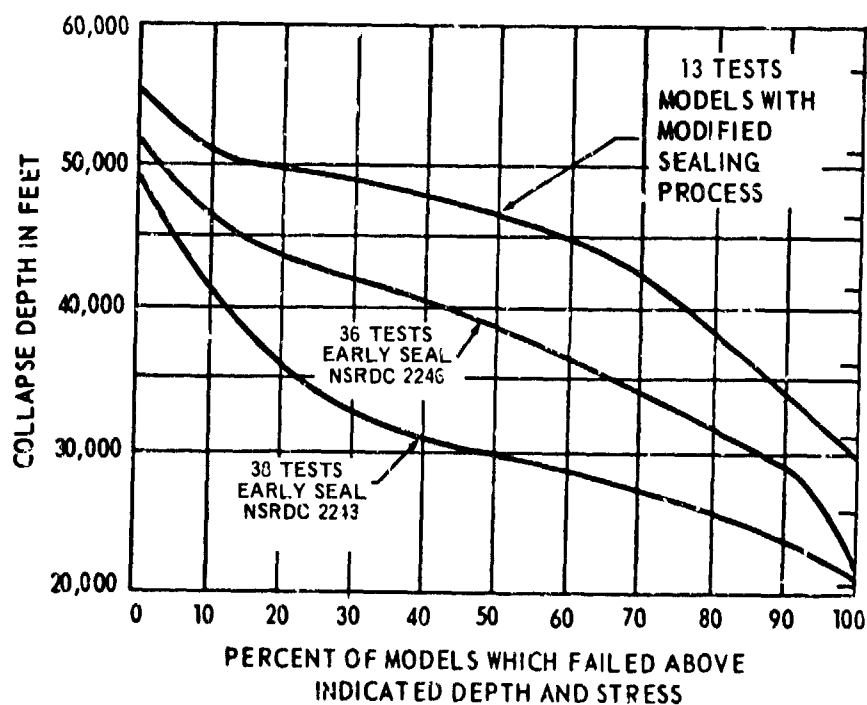
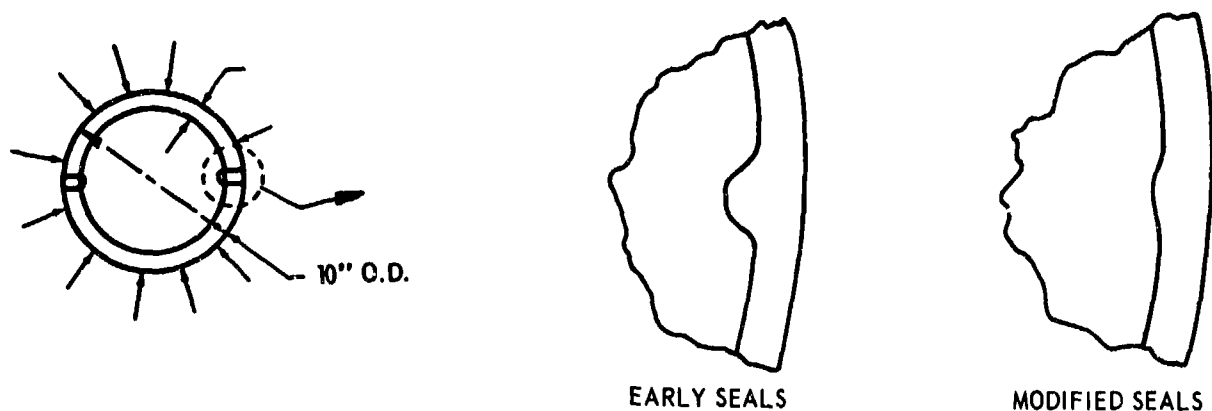


Figure 20 - Summary of Test Results of 10-Inch-Diameter 0.28 Wall Fusion Sealed Annealed Pyrex Glass Spheres



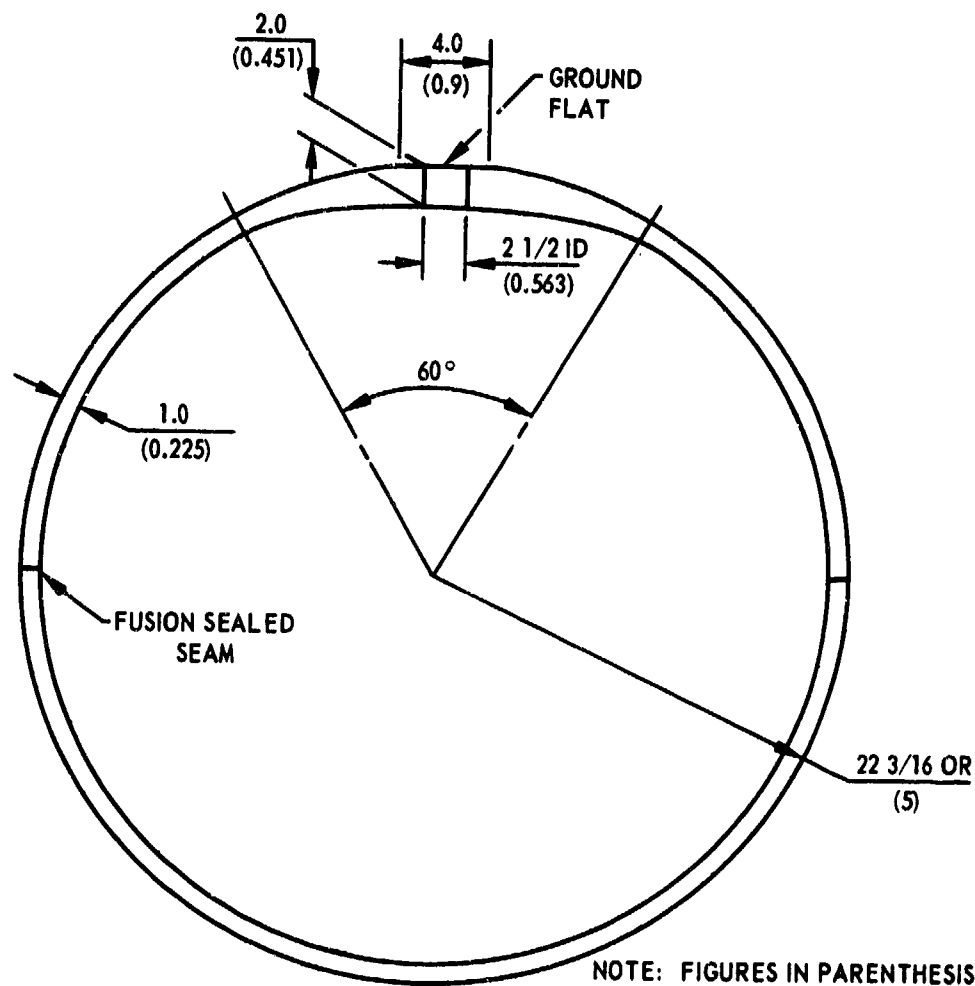
Figure 21a - Earlier Type Seam

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Figure 21b - Modified Type Seam

Figure 21 - Examples of Fusion Sealed Seams



NOTE: FIGURES IN PARENTHESIS ARE  
DIMENSIONS FOR 10 INCH MODEL

Figure 22 - Nominal Model Dimensions for Fusion Sealed  
Spheres with Penetration

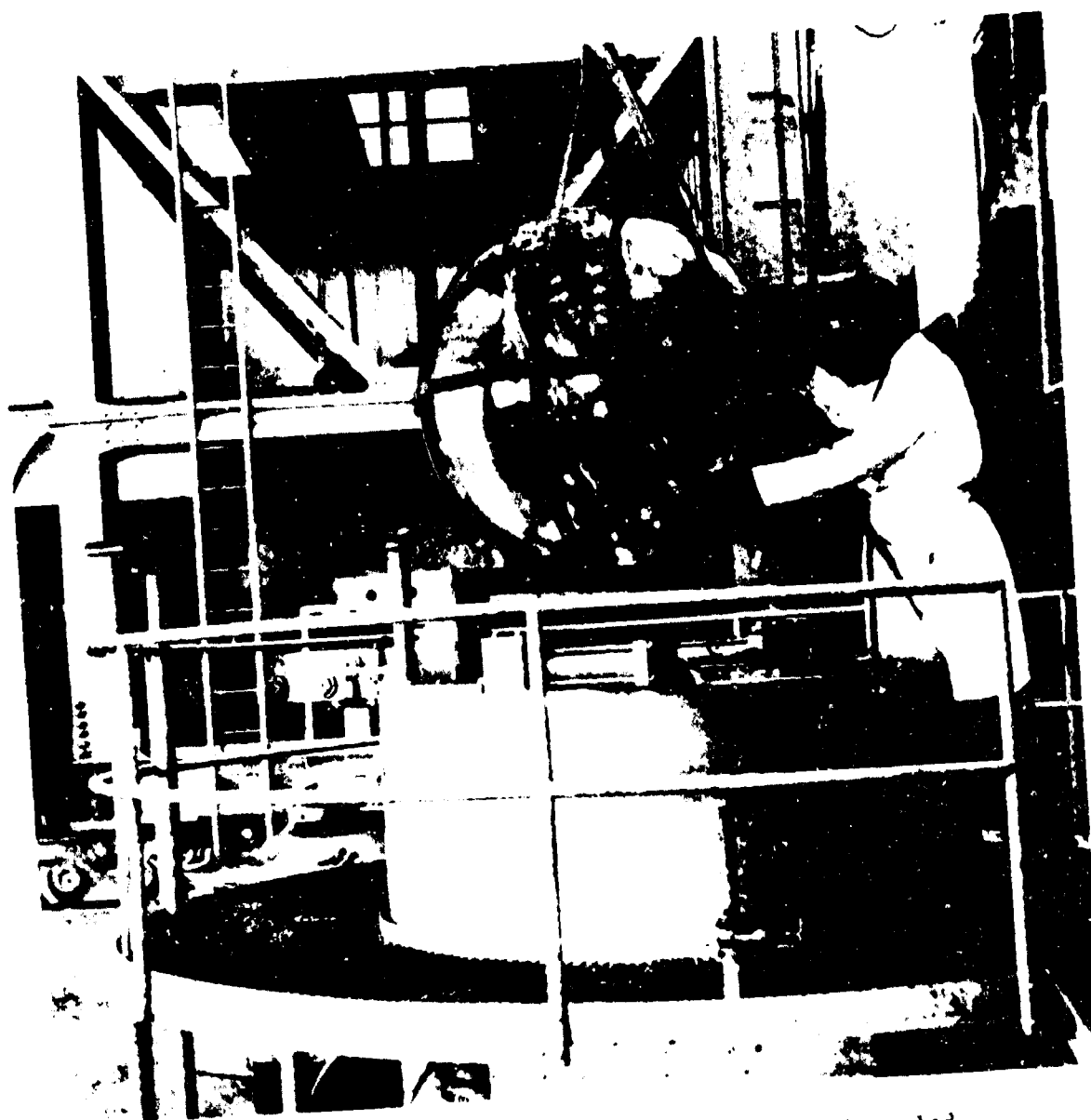


Figure 23 - 44 Inch Diameter Fusion Sealed Annealed  
Glass Sphere

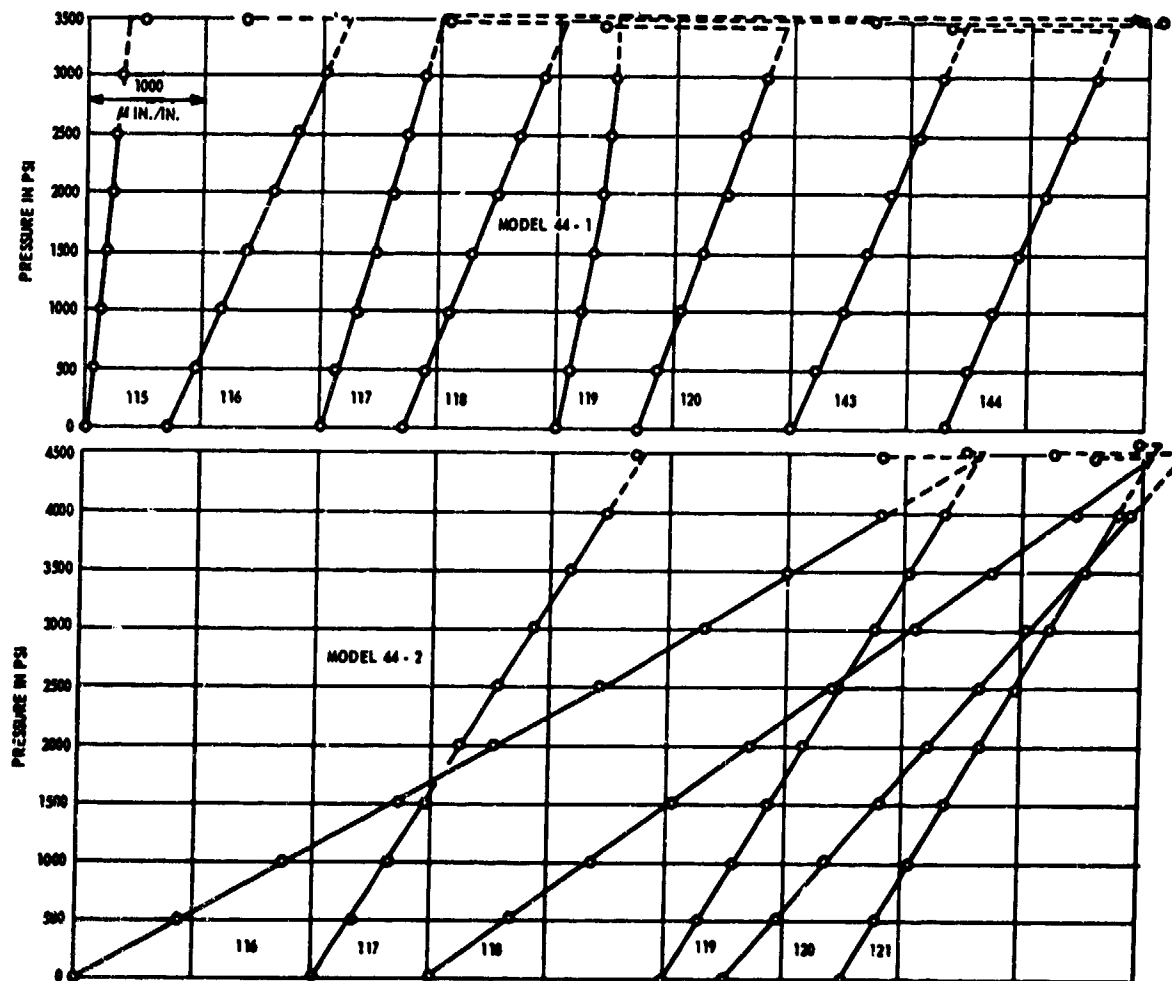


Figure 24 - Pressure Strain Plots for 44 Inch Glass Sphere



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Figure 25 - Damage to Model 44-1 after 3500 psi

Figure 26 - Gage Locations and Strain Sensitivities for 44 Inch Sphere

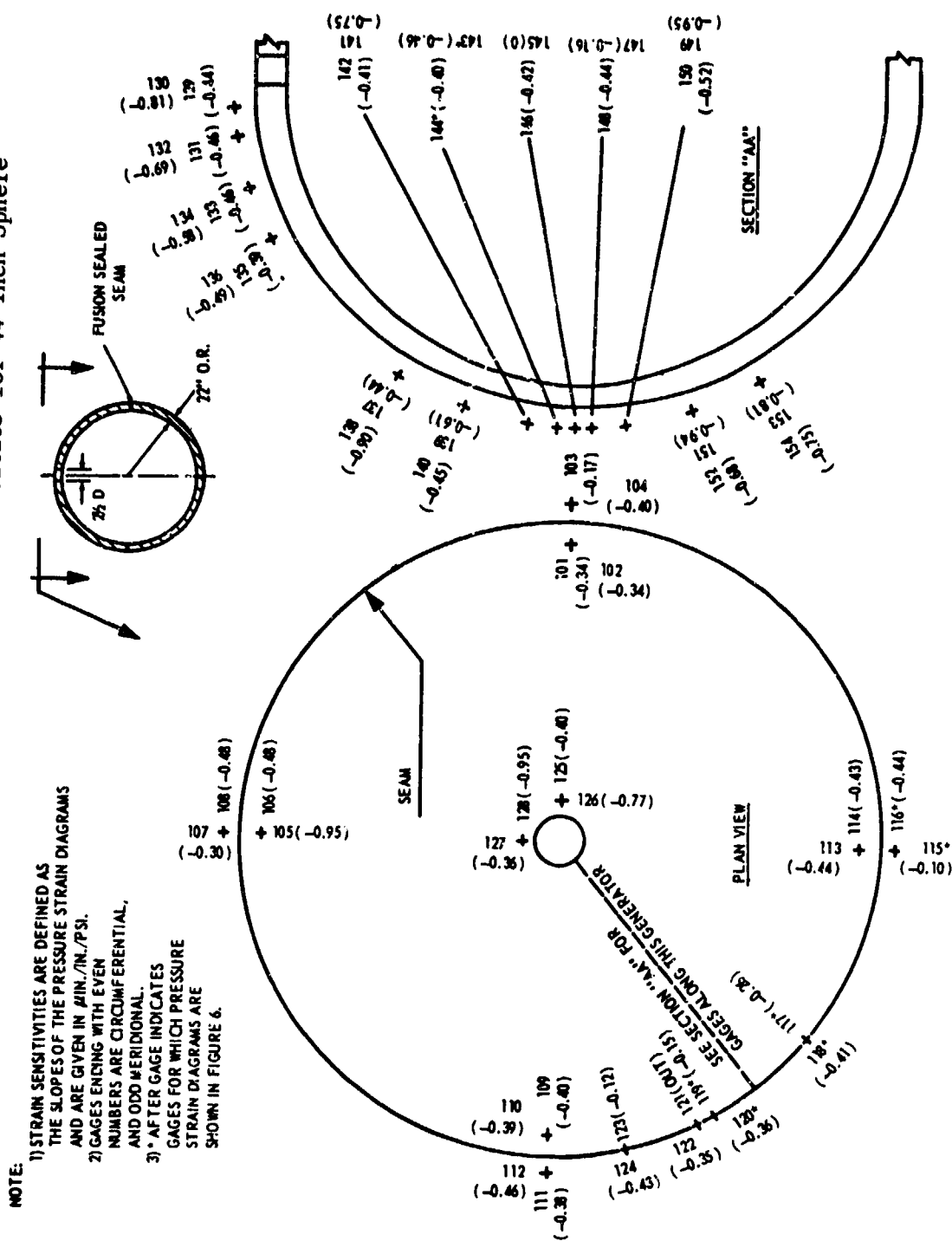


Figure 26a - Model 44-1



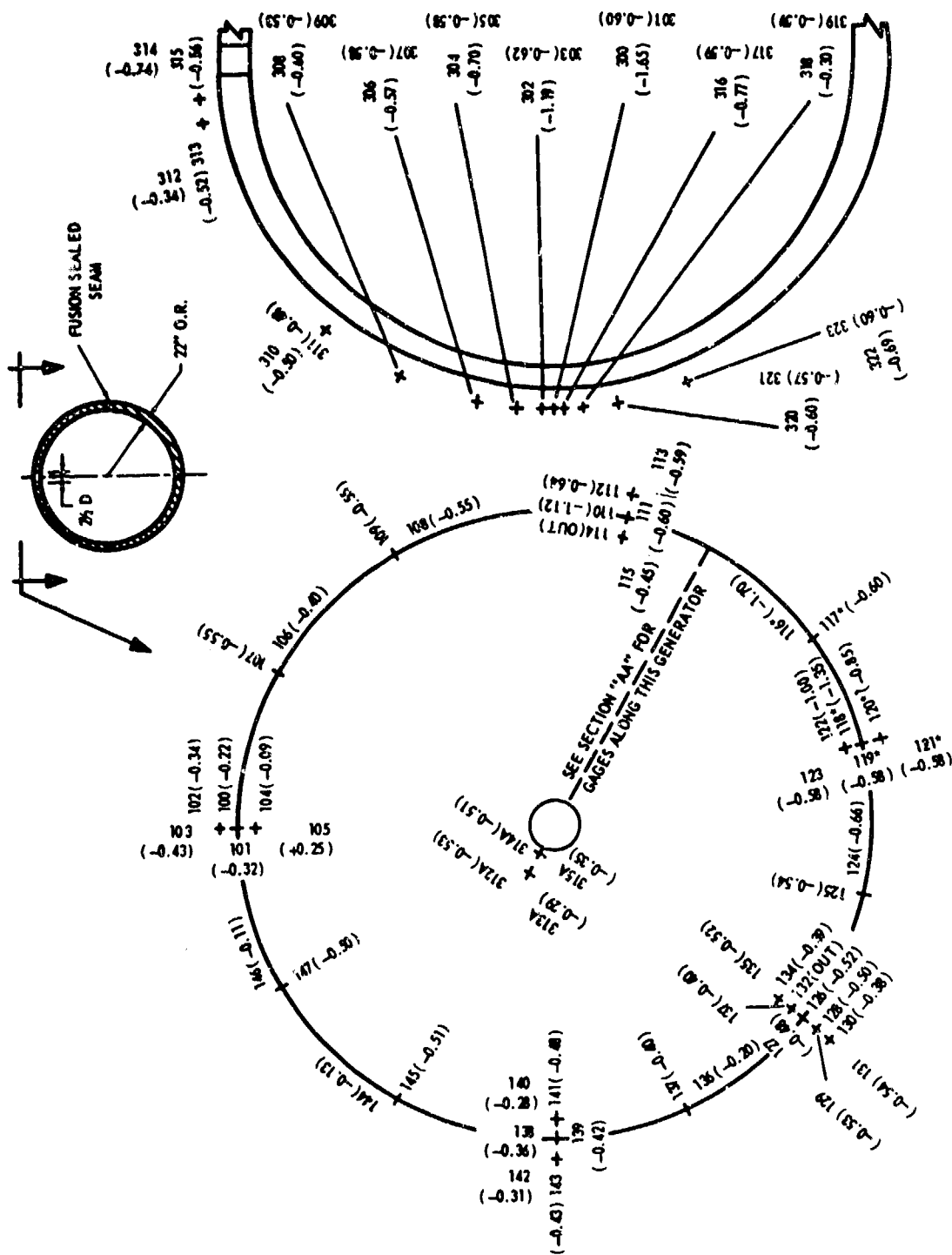


Figure 26b - Model 44-2

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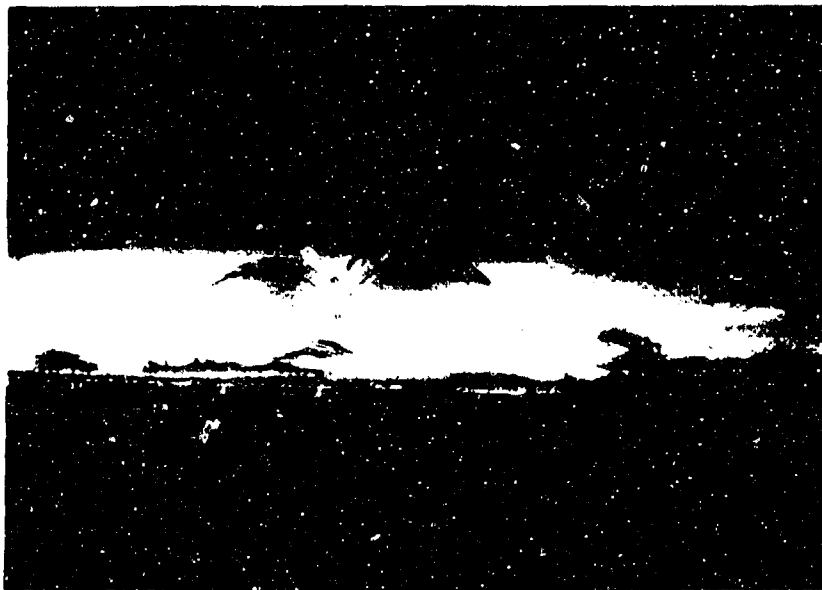
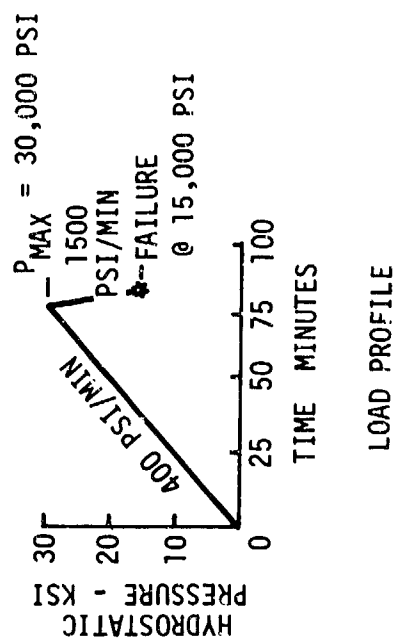
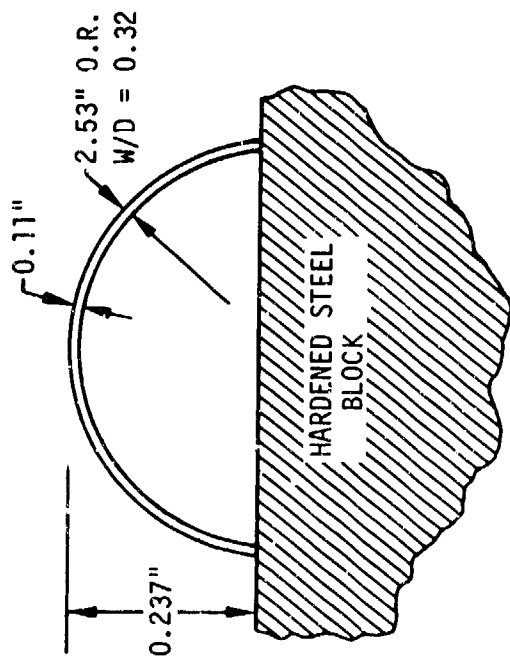


Figure 27a - After 1000 Cycles (3X)



Figure 27b - After 3000 Cycles (3X)

Figure 27 - Damage to Model C-2 After Cycling to 5000 PSI



#### Material Properties:

$$E = 17.3 \times 10^6 \text{ psi}$$

$$\nu = 0.245$$

$$\gamma = 163 \text{ #/ft}^3$$

#### Loads:

Calculated Collapse Pressure - 27,000 psi

Experimental Pressure - 30,000 psi\*

Membrane Stress - 352,000 psi

\* Model did not fail at maximum applied load. Failure occurred during release of pressure. See Load Profile.

Figure 28 - Nominal Model Dimensions and Test Result of 5 Inch Diameter Pyroceram Hemisphere

TABLE 5 - EFFECT OF LOADING RATE AND PRESSURE MEDIUM ON  
COLLAPSE STRENGTH

| Series                                                                  | Model | Experimental Collapse |        | Average Stress in Shell at Collapse |
|-------------------------------------------------------------------------|-------|-----------------------|--------|-------------------------------------|
|                                                                         |       | psi                   | ft     | psi                                 |
| I<br>(Tests in sea water at compressive stress rate of 140,000 psi/min) | 1     | 20,025                | 46,400 | 183,000**                           |
|                                                                         | 2     | 19,250                | 43,300 | 162,000**                           |
|                                                                         | 3     | 14,200                | 31,900 | 126,000                             |
|                                                                         | 4     | 14,100                | 31,700 | 119,000                             |
|                                                                         | 5     | 13,400                | 30,100 | 117,000                             |
|                                                                         | 6     | 12,750                | 28,700 | 112,000                             |
|                                                                         | 7     | 12,625                | 28,400 | 105,000                             |
|                                                                         | 8     | 10,550                | 23,700 | 89,000                              |
|                                                                         | 9     | 9,550                 | 21,500 | 83,000                              |
| II<br>(Tests in sea water at compressive stress rate of 3500 psi/min)   | 10    | 18,500                | 41,600 | 157,000                             |
|                                                                         | 11    | 17,700                | 40,000 | 155,000                             |
|                                                                         | 12    | 15,450                | 34,700 | 136,000                             |
|                                                                         | 13    | 14,300                | 32,200 | 125,000                             |
|                                                                         | 14    | 13,875                | 31,200 | 122,000                             |
|                                                                         | 15    | 13,200                | 29,700 | 115,000                             |
|                                                                         | 16    | 11,800                | 26,500 | 103,000                             |
|                                                                         | 17    | 11,000                | 24,700 | 97,000                              |
|                                                                         | 18    | 10,500                | 23,600 | 91,000                              |
| III<br>(Tests in oil at compressive stress rate of 3500 psi/min)        | 19    | 22,600                | 50,800 | 199,000**                           |
|                                                                         | 20    | 17,125                | 38,600 | 149,000                             |
|                                                                         | 21    | 16,100                | 36,000 | 140,000                             |
|                                                                         | 22    | 15,650                | 35,200 | 138,000                             |
|                                                                         | 23    | 15,300                | 34,400 | 131,000                             |
|                                                                         | 24    | 14,300                | 32,200 | 123,000                             |
|                                                                         | 25    | 13,400                | 30,100 | 117,000                             |
|                                                                         | 26    | 12,550                | 28,300 | 111,000                             |
|                                                                         | 27    | 9,050                 | 20,300 | 81,000                              |
| IV<br>(Tests in sea water at compressive stress rate of 200 psi/min)    | 28*   | 22,010                | 49,500 | 191,000**                           |
|                                                                         | 29    | 16,550                | 37,300 | 142,000                             |
|                                                                         | 30    | 15,710                | 35,300 | 136,000                             |
|                                                                         | 31    | 14,030                | 31,500 | 122,000                             |
|                                                                         | 32    | 13,640                | 30,700 | 118,000                             |
|                                                                         | 33    | 13,390                | 30,100 | 115,000                             |
|                                                                         | 34    | 12,150                | 27,300 | 104,000                             |
|                                                                         | 35    | 11,950                | 26,900 | 103,000                             |
|                                                                         | 36    | 10,550                | 23,700 | 92,000                              |

\*Model was not collapsed.

\*\*Stress levels which may be associated with elastic buckling failure.

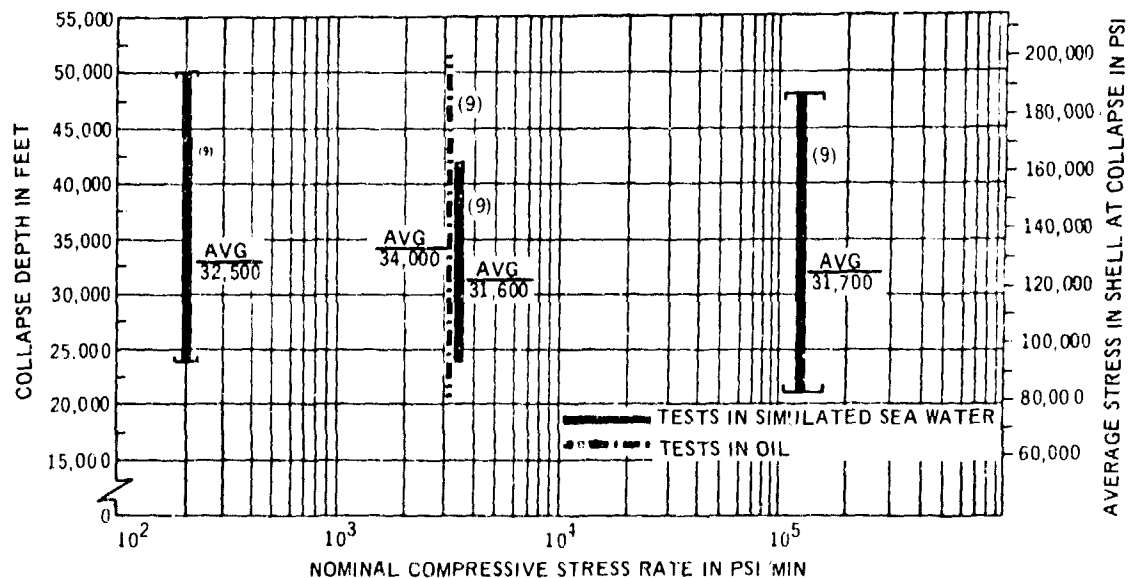


TABLE 6 - COLLAPSE STRENGTH OF 10-INCH-DIAMETER  
0.28 WALL FUSION SEALED ANNEALED PYREX GLASS  
SPHERES WITH MODIFIED SEAMS

| Model                                  | Collapse Pressure |        | Stress* |
|----------------------------------------|-------------------|--------|---------|
|                                        | psi               | ft     |         |
| IFS 7                                  | 13,600            | 30,600 | 119,000 |
| IFS 13                                 | 14,450            | 32,500 | 126,000 |
| IFS 5                                  | 15,200            | 34,200 | 134,000 |
| IFS 4                                  | 18,100            | 40,700 | 160,000 |
| IFS 9                                  | 19,900            | 44,800 | 174,000 |
| IFS 14                                 | 20,500            | 46,000 | 181,000 |
| IFS 12                                 | 20,625            | 46,300 | 179,000 |
| IFS 1                                  | 21,050            | 47,400 | 188,000 |
| IFS 8                                  | 21,425            | 48,300 | 187,000 |
| IFS 6                                  | 26,625            | 48,600 | 190,000 |
| IFS 11                                 | 22,375            | 50,400 | 197,000 |
| IFS 3                                  | 23,150            | 52,100 | 201,000 |
| IFS 10                                 | 25,050            | 56,400 | 222,000 |
| * Based on average measured thickness. |                   |        |         |

TABLE 7 - CYCLIC TESTS OF 10-INCH-DIAMETER 0.28 WALL THICKNESS  
SEALED ANNEALED PYREX GLASS SPHERES

| Model | Seal Type | Run No. | Test                  | Pressure |        |
|-------|-----------|---------|-----------------------|----------|--------|
|       |           |         |                       | psi      | ft     |
| C-1   | Early     | 1       | Proof                 | 13,333   | 30,000 |
|       |           | 2       | Cyclic<br>5000 cycles | 10,000   | 22,500 |
|       |           | 3       | Collapse              | 19,600   | 44,000 |
| C-2   | Early     | 1       | Proof                 | 13,333   | 30,000 |
|       |           | 2       | Cyclic<br>5000 cycles | 10,000   | 22,500 |
|       |           | 3       | Collapse              | 21,090   | 47,600 |
| C-3   | Early     | 1       | Proof                 | 13,333   | 30,000 |
|       |           | 2       | Cyclic<br>5000 cycles | 10,000   | 22,500 |
|       |           | 3       | Collapse              | 16,425   | 37,000 |
| C-4   | Early     | 1       | Proof                 | 13,333   | 30,000 |
|       |           | 2       | Cyclic<br>5000 cycles | 10,000   | 22,500 |
|       |           | 3       | Collapse              | 16,025   | 36,100 |
| 28    | Early     | 1       | Proof                 | 22,010   | 49,500 |
|       |           | 2       | Cyclic<br>5000 cycles | 10,000   | 22,500 |
|       |           | 3       | Collapse              | 22,250   | 50,000 |
| 2A    | Modified  | 1       | Proof                 | 13,333   | 30,000 |
|       |           | 2       | Cyclic<br>5000 cycles | 10,000   | 22,500 |
| 6A    | Modified  | 1       | Proof                 | 13,333   | 30,000 |
|       |           | 2       | Cyclic<br>5000 cycles | 10,000   | 22,500 |
| 9A    | Modified  | 1       | Proof                 | 13,333   | 30,000 |
|       |           | 2       | Cyclic<br>5000 cycles | 10,000   | 22,500 |
| 10A   | Modified  | 1       | Proof                 | 13,333   | 30,000 |
|       |           | 2       | Cyclic<br>5000 cycles | 10,000   | 22,500 |
| 3A    | Modified  | 1       | Proof                 | 13,333   | 30,000 |
|       |           | 2       | Cyclic<br>5000 cycles | 10,000   | 22,500 |

TABLE 8 - COLLAPSE STRENGTH OF 10-INCH-DIAMETER 0.36 WALL FUSION SEALED ANNEALED PYREX GLASS

| Model                                  | Collapse Pressure |        | Stress* |
|----------------------------------------|-------------------|--------|---------|
|                                        | psi               | ft     |         |
| 319                                    | 19,000            | 43,700 | 136,000 |
| 313                                    | 21,925            | 49,400 | 155,000 |
| 314                                    | 22,200            | 50,000 | 155,000 |
| 316                                    | 22,090            | 49,600 | 158,000 |
| 320                                    | 23,000            | 51,700 | 163,000 |
| 317                                    | 23,200            | 52,200 | 164,000 |
| * Based on average measured thickness. |                   |        |         |

TABLE 9 - SUMMARY OF STATIC TESTS OF 10-INCH-DIAMETER FUSION-SEALED ANNEALED PYREX GLASS SPHERES WITH PENETRATIONS

| Model                                                                                                                                                                                                                          | Collapse Pressure   |        | $h_a^1$ (in.) | Average Stress at Collapse (psi) | $P_e^2$ (psi) | $P_{EXP}/P_e$ |
|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------------------|--------|---------------|----------------------------------|---------------|---------------|
|                                                                                                                                                                                                                                | psi                 | ft     |               |                                  |               |               |
| GS-1                                                                                                                                                                                                                           | 15,475              | 34,800 | 0.220         | 180,000                          | 14,300        | 1.08          |
| GS-2                                                                                                                                                                                                                           | 15,550              | 35,000 | 0.232         | 172,000                          | 15,900        | 0.98          |
| GS-3                                                                                                                                                                                                                           | 14,475              | 32,600 | 0.225         | 165,000                          | 14,900        | 0.97          |
| GS-4                                                                                                                                                                                                                           | 15,150 <sup>3</sup> | 34,100 | 0.222         | 174,000                          | 14,600        | 1.04          |
| GS-5                                                                                                                                                                                                                           | 13,333              | 30,000 | 0.223         | 152,000                          | 14,700        | 0.91          |
| <p>1 - Minimum measured thickness.</p> <p>2 - <math>P_e</math> calculated from equation <math>P_e = 0.83 E \left( \frac{h_a^1}{R_o} \right)^2</math> where <math>R_o = 5</math> in.</p> <p>3 - Test conducted in two runs.</p> |                     |        |               |                                  |               |               |

TABLE 10 - STATE CYCLIC TESTS OF 10-INCH-DIAMETER 0.18  
WALL MONOLITHIC ALUMINA SPHERES

STATIC TESTS

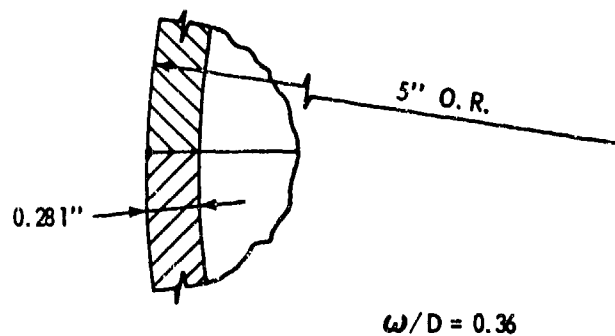
| Model No. | P <sub>3</sub><br>psi | Experimental Pressures |        | Calculated Failure Stress |           |
|-----------|-----------------------|------------------------|--------|---------------------------|-----------|
|           |                       | psi                    | ft     | Average ksi               | Local ksi |
| AL- 92    | 30,080                | 25,400                 | 57,200 | 429                       | 484       |
| AL- 95    | 30,080                | 27,825                 | 62,600 | 468                       | 534       |
| AL- 98    | 27,200                | 28,475                 | 64,000 | 497                       | 572       |
| AL- 99    | 28,510                | 20,400                 | 46,000 | 373                       | 402       |
| AL-105    | 28,070                | 27,125                 | 61,100 | 412                       | 542       |
| AL-106    | 23,860                | 26,875                 | 60,500 | 500                       | 574       |
| AL-108    | 30,080                | 25,500                 | 57,375 | 442                       | 490       |
| AL-109    | 36,030                | 22,450                 | 50,500 | 370                       | 410       |
| AL- 94    | 36,500                | 26,875                 | 60,500 | 410                       | 468       |
| AL-104    | 25,600                | 26,850*                | 60,400 | 395                       | 560       |
| AL-107    | 33,200                | 26,875*                | 60,500 | 395                       | 495       |
| AL- 91    | 28,740                | 20,100                 | 45,300 | 350                       | 395       |
| AL- 93    | 32,160                | 25,875                 | 58,300 | 430                       | 476       |
| AL- 96    | 29,180                | 22,950                 | 51,600 | 385                       | 450       |
| AL- 97    | 34,800                | 20,750                 | 46,700 | 340                       | 370       |
| AL-100    | 27,200                | 26,000                 | 58,500 | 480                       | 520       |
| AL-101    | 29,860                | 26,750                 | 60,000 | 450                       | 510       |
| AL-102    | 31,690                | 25,375                 | 57,000 | 430                       | 480       |
| AL-103    | 30,540                | 25,200                 | 56,800 | 420                       | 480       |

CYCLIC TESTS

| Model  | W/D  | Run | Pressure |        | Stress |       |                                 |
|--------|------|-----|----------|--------|--------|-------|---------------------------------|
|        |      |     | psi      | ft     | avg    | local |                                 |
| AL-104 | 0.38 | 1   | 13,333   | 30,000 | 196    | 285   | Held 13,333 psi for 1 hr        |
|        |      | 2   | 10,000   | 22,500 | 147    | 212   | Cycled 5000 times               |
|        |      | 3   | 26,850   | 60,400 | 395    | 575   | Returned to NSRDC and collapsed |
| AL-107 | 0.38 | 1   | 13,333   | 30,000 | 194    | 245   | Held 13,333 psi for 1 hr        |
|        |      | 2   | 10,000   | 23,500 | 145    | 184   | Cycled 5000 times               |
|        |      | 3   | 26,875   | 60,500 | 390    | 495   | Returned to NSRDC and collapsed |

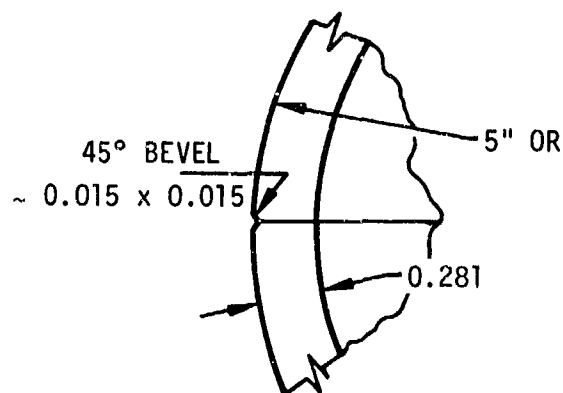


TABLE 11 - SUMMARY OF STATIC TESTS OF CHEMICALLY  
STRENGTHENED HERCULITE II (1080 Na<sup>+</sup>) GLASS  
HEMISPHERES



| Model<br>No. | Collapse Pressure |        | Bearing<br>Stress<br>psi |
|--------------|-------------------|--------|--------------------------|
|              | psi               | ft     |                          |
| HH-1         | 22,800            | 51,400 | 219,000                  |
| HH-2         | 18,800            | 42,400 | 175,000                  |
| HH-3         | 18,750            | 42,300 | 175,000                  |
| HH-4         | 17,300            | 39,000 | 161,000                  |
| HH-5         | 13,550            | 30,500 | 127,000                  |

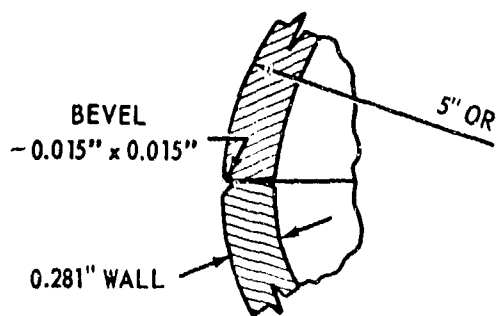
TABLE 12 - TEST RESULTS OF 10-INCH-DIAMETER 0.281 WALL ANNEALED  
PYREX GLASS HEMISPHERICAL SHELLS WITHOUT GASKETS



JOINT CONFIGURATION

| Series 1                                                                                                                                                                                  |                         |                             | Series 2                           |                         |                             |
|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------------------|-----------------------------|------------------------------------|-------------------------|-----------------------------|
| No. 150 Grit Diamond Wheel                                                                                                                                                                |                         |                             | 1200 Mesh Diamond Abrasive         |                         |                             |
| Test No.                                                                                                                                                                                  | Collapse Pressure - psi | Average Bearing Stress* ksi | Test No.                           | Collapse Pressure - psi | Average Bearing Stress* ksi |
| 1                                                                                                                                                                                         | 10,650                  | 96                          | 1                                  | 14,300                  | 134                         |
| 2                                                                                                                                                                                         | 10,350                  | 96                          | 2                                  | 13,625                  | 129                         |
| 3                                                                                                                                                                                         | 10,350                  | 94                          | 3                                  | 13,275                  | 126                         |
| 4                                                                                                                                                                                         | 10,500                  | 96                          | 4                                  | 12,700                  | 118                         |
| 5                                                                                                                                                                                         | 10,300                  | 96                          | 5                                  | 12,575                  | 118                         |
| 6                                                                                                                                                                                         | 10,300                  | 94                          | 6                                  | 12,500                  | 118                         |
| 7                                                                                                                                                                                         | 10,100                  | 92                          | 7                                  | 12,525                  | 115                         |
| 8                                                                                                                                                                                         | 10,000                  | 92                          | 8                                  | 12,450                  | 117                         |
| 9                                                                                                                                                                                         | 9,950                   | 92                          | 9                                  | 12,125                  | 114                         |
| 10                                                                                                                                                                                        | 9,900                   | 91                          | 10                                 | 12,050                  | 113                         |
| 11                                                                                                                                                                                        | 9,625                   | 88                          | 11                                 | 12,000                  | 113                         |
| 12                                                                                                                                                                                        | 9,100                   | 83                          | 12                                 | 11,675                  | 110                         |
| 13                                                                                                                                                                                        | 9,000                   | 83                          | 13                                 | 11,575                  | 106                         |
| 14                                                                                                                                                                                        | 8,950                   | 83                          | 14                                 | 11,400                  | 108                         |
| 15                                                                                                                                                                                        | 8,200                   | 76                          | 15                                 | 11,400                  | 106                         |
| 16                                                                                                                                                                                        | 6,150                   | 53                          | 16                                 | 11,125                  | 103                         |
| 17                                                                                                                                                                                        | 5,075                   | 46                          |                                    |                         |                             |
| No. of Tests - 17                                                                                                                                                                         |                         |                             | No. of Tests - 16                  |                         |                             |
| Avg Collapse Pressure - 9323 psi                                                                                                                                                          |                         |                             | Avg Collapse Pressure - 12,331 psi |                         |                             |
| Avg Collapse Stress - 85 ksi                                                                                                                                                              |                         |                             | Avg Collapse Stress - 113 ksi      |                         |                             |
| * Based on measured thickness at joint. Reduction in thickness by bevelling edges not accounted for. Average bearing stress would be increased by about 10 percent if taken into account. |                         |                             |                                    |                         |                             |

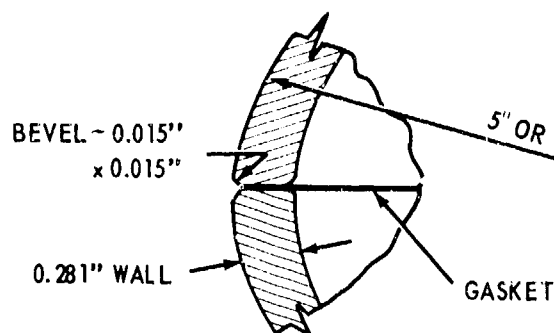
TABLE 13 - TEST RESULTS OF 10-INCH-DIAMETER 0.28 WALL  
ANNEALED PYREX GLASS HEMISPHERES WITH GASKETS



JOINT CONFIGURATION

| Glass Fiber Cloth and Epoxy                                                        |                   |        |                 | Glass Fiber Cloth and Synthetic Rubber                                  |                   |        |                 |
|------------------------------------------------------------------------------------|-------------------|--------|-----------------|-------------------------------------------------------------------------|-------------------|--------|-----------------|
| Test No.                                                                           | Collapse Pressure |        | Collapse Stress | Test No.                                                                | Collapse Pressure |        | Collapse Stress |
|                                                                                    | psi               | ft     |                 |                                                                         | psi               | ft     |                 |
| 1                                                                                  | 21,475            | 48,300 | 196,600         | 1                                                                       | 22,740            | 51,200 | 208,100         |
| 2                                                                                  | 19,350            | 43,500 | 177,100         | 2                                                                       | 21,200            | 47,700 | 194,000         |
| 3                                                                                  | 18,350            | 41,300 | 168,000         | 3                                                                       | 20,825            | 46,900 | 190,600         |
| 4                                                                                  | 12,800            | 28,800 | 117,200         | 4                                                                       | 18,400*           | 41,400 | 168,400         |
| 5                                                                                  | 11,250            | 25,300 | 103,000         | 5                                                                       | 17,900*           | 40,300 | 163,800         |
| 6                                                                                  | 9,375             | 21,100 | 85,800          | 6                                                                       | 17,000*           | 38,200 | 155,600         |
| Avg Collapse Pressure = 15,433 psi<br>Avg Collapse Stress = 141,200 psi            |                   |        |                 | Avg Collapse Pressure = 19,678 psi<br>Avg Collapse Stress = 180,100 psi |                   |        |                 |
| *Tests terminated after drop in pressure noted. Edges of bearing surfaces spalled. |                   |        |                 |                                                                         |                   |        |                 |

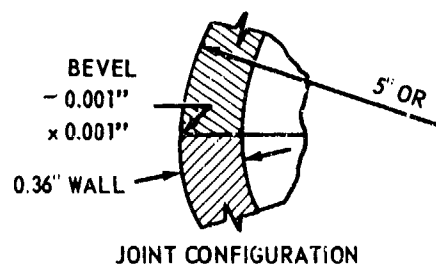
TABLE 14 - SUMMARY OF CYCLIC TESTS OF 10-INCH-DIAMETER  
0.28 WALL ANNEALED PYREX GLASS HEMISPHERES



| Model No. | Gasket Type                          | Proof Pressure |        | Cyclic Pressure |        | Stress psi | No. Cycles to Failure |
|-----------|--------------------------------------|----------------|--------|-----------------|--------|------------|-----------------------|
|           |                                      | psi            | ft     | psi             | ft     |            |                       |
| C-1       | 0.003 in Glass Fiber Cloth and Epoxy | None           | —      | 5,000           | 11,250 | 45,800     | 3,000*                |
| C-2       | 0.003 in Glass Fiber Cloth and Epoxy | None           | —      | 6,000           | 13,500 | 54,900     | 2,015                 |
| C-3       | 0.003 in Glass Fiber Cloth and Epoxy | None           | —      | 7,000           | 15,750 | 64,000     | 197                   |
| C-4       | 0.003 in Glass Fiber Cloth and Epoxy | None           | —      | 8,000           | 18,000 | 73,200     | 150                   |
| C-5       | 0.003 in Glass Fiber Cloth and Epoxy | 13,333         | 30,000 | 10,000          | 22,500 | 91,500     | 706                   |
| H-1       | 0.003 in Glass Fiber Cloth and Hysol | 13,333         | 30,000 | 10,000          | 22,500 | 91,500     | 1                     |
| H-2       | 0.003 in Glass Fiber Cloth and Hysol | None           | —      | 10,000          | 22,500 | 91,500     | 4                     |
| H-3       | 0.003 in Glass Fiber Cloth and Hysol | None           | —      | 7,500           | 16,900 | 68,6000    | 5                     |

\*Heavy damage to inner and outer surfaces of bearing joint observed after 3,000 cycles. No further testing attempted.

TABLE 15 - SUMMARY OF TEST RESULTS OF 10-INCH-DIAMETER  
0.36 WALL PPG 1080 ANNEALED GLASS HEMISPHERICAL SHELLS



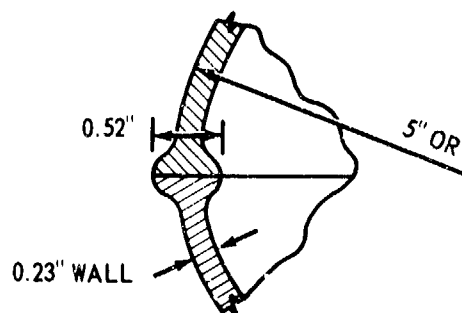
1200 Mesh Diamond Abrasive Finish

| Test No. | Collapse Pressure |        | Stress  |
|----------|-------------------|--------|---------|
|          | psi               | ft     | psi     |
| 1        | 17,950            | 40,400 | 131,000 |
| 2        | 17,600            | 39,600 | 129,000 |
| 3        | 16,950            | 38,100 | 126,000 |

No. 120 Grit Finish

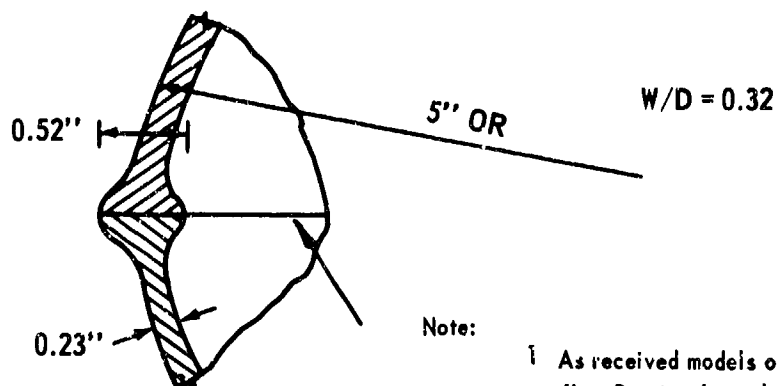
| Test No. | Collapse Pressure |        | Stress  | Remarks                                                                                                                          |
|----------|-------------------|--------|---------|----------------------------------------------------------------------------------------------------------------------------------|
|          | psi               | ft     | psi     |                                                                                                                                  |
| 1        | 21,475            | 48,300 | 158,000 | Loaded at 18,000 psi/min                                                                                                         |
| 2        | 21,100            | 47,500 | 155,000 |                                                                                                                                  |
| 3        | 19,175            | 43,100 | 145,000 |                                                                                                                                  |
| 4        | 19,000            | 42,800 | 144,000 |                                                                                                                                  |
| 5        | 18,075            | 40,700 | 137,000 | Soaked in S. W. 20 days                                                                                                          |
| 6        | 17,100            | 38,500 | 128,000 |                                                                                                                                  |
| 7        | 16,800            | 37,800 | 126,000 |                                                                                                                                  |
| 8        | 16,700            | 37,600 | 126,000 |                                                                                                                                  |
| 9        | 16,800            | 37,800 | 125,000 | Loaded at 20 psi/min                                                                                                             |
| 10       | 16,800            | 37,800 | 123,000 |                                                                                                                                  |
| 11       | 15,200            | 34,200 | 116,000 |                                                                                                                                  |
| 12       | 15,150            | 34,100 | 112,000 |                                                                                                                                  |
| 13       | 14,800            | 33,300 | 110,000 | 2 Runs. 1st run to 15,000 held for 4 hrs.<br>2nd Run collapsed at 15,150 after 5 secs.<br>Loaded at 18,000 psi/min               |
| 14       | 14,800            | 33,300 | 110,000 |                                                                                                                                  |
| 15       | 14,500            | 32,600 | 108,000 |                                                                                                                                  |
| 16       | 14,000            | 31,500 | 105,000 |                                                                                                                                  |
| 17       | 14,000            | 31,500 | 105,000 | 4 Runs. 1 hr. holds after 13,000, 13,500<br>and 14,000. Collapsed on 4th Run at<br>14,500 after 15 min. Loaded at 18,000 psi/min |
| 18       | 13,500            | 30,400 | 99,000  |                                                                                                                                  |
| 19       | 12,000            | 27,000 | 88,000  |                                                                                                                                  |
| 20       | 11,600            | 26,100 | 86,000  |                                                                                                                                  |

TABLE 16 - SUMMARY OF STATIC TESTS OF CHEMCOR HEMISPHERES  
WITH REINFORCED BEARING SURFACES



| Loading Rate<br>psi/min | Model Number | Collapse Pressure |        | Collapse Stress |                    |
|-------------------------|--------------|-------------------|--------|-----------------|--------------------|
|                         |              |                   |        | Membrane<br>psi | Avg Bearing<br>psi |
|                         |              | psi               | ft     |                 |                    |
| 20                      | CH-1         | 19,500            | 43,900 | 217,000         | 100,000            |
|                         | CH-2         | 17,625            | 39,700 | 196,000         | 90,000             |
|                         | CH-3         | 16,500            | 37,100 | 183,000         | 83,000             |
|                         | CH-4         | 12,125            | 27,300 | 135,000         | 65,000             |
|                         | CH-5         | 11,125            | 25,000 | 124,000         | 60,000             |
| 15,000                  | CH-6         | 13,750            | 30,900 | 153,000         | 72,000             |
|                         | CH-7         | 12,275            | 27,660 | 136,000         | 64,000             |
|                         | CH-8         | 11,450            | 25,800 | 127,000         | 60,000             |
|                         | CH-9         | 10,650            | 24,000 | 118,000         | 58,000             |
|                         | CH-10        | 8,875             | 20,000 | 99,000          | 46,000             |

TABLE 17 - SUMMARY OF CYCLIC TESTS OF CHEMCOR 0312 HEMISPHERES  
WITH REINFORCED BEARING SURFACES



| TEST<br>NUMBER | PROOF<br>PRESSURE<br>psi | CYCLIC<br>PRESSURE<br>psi |     | NUMBER<br>CYCLES | REMARKS                                                                                  |
|----------------|--------------------------|---------------------------|-----|------------------|------------------------------------------------------------------------------------------|
|                |                          | MAX                       | MIN |                  |                                                                                          |
| 1              | NONE                     | 10,000                    | 200 | 5000             | CYCLIC TESTS STOPPED AFTER<br>4000 CYCLES. MODEL STATI-<br>CALLY COLLAPSED AT 13,300 PSI |
| 2              | NONE                     | 10,000                    | 200 | 5000             |                                                                                          |
| 3              | NONE                     | 10,000                    | 200 | 5000             |                                                                                          |
| 4              | 13,333                   | 10,000                    | 200 | 4000             |                                                                                          |
| 5              | NONE                     | 10,000                    | 200 | 3300             | COLLAPSED                                                                                |
| 6              | NONE                     | 10,000                    | 200 | 86               | COLLAPSED                                                                                |
| 7              | NONE                     | 10,000                    | 200 | 110              | COLLAPSED                                                                                |

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